

**MANIPAL UNIVERSITY JAIPUR**  
**SCHOOL OF COMPUTING AND IT**  
**B.Tech. III Semester Second Sessional Examinations, November 2017**  
**Branch: CSE / IT / CCE**  
**MA1307-Engineering Mathematics-III**  
**(OPEN BOOK)**

Duration: 1 hour

Max. Marks: 15

**Instructions:**

- All questions are compulsory.
- Missing data if any may be assumed suitably.
- Maximum three units of Books/Spiral Bound Notes/ Note Books are allowed.

1.	How many permutations can be made with the letters of the word “MANIPAL” under the following conditions: (i) Vowels occur together (ii) All Vowels are together and all Consonants are together (iii) Vowels and consonants occur alternately	[3]																																																	
2.	Is $A = \left\{ \begin{bmatrix} 1 & m \\ 0 & 1 \end{bmatrix} / m \in N \right\}$ a Monoid with respect to multiplication of matrices? Justify your answer.	[2]																																																	
3.	Fill the missing entries in the following multiplication table of a group $(\{1, 5, 7, 11, 13, 17\}, \times_{18})$ <table><tr><td><math>\times_{18}</math></td><td>1</td><td>5</td><td>7</td><td>11</td><td>13</td><td>17</td></tr><tr><td>1</td><td>1</td><td>—</td><td>—</td><td>—</td><td>—</td><td>—</td></tr><tr><td>5</td><td>—</td><td>7</td><td>—</td><td>1</td><td>—</td><td>—</td></tr><tr><td>7</td><td>—</td><td>17</td><td>13</td><td>—</td><td>—</td><td>11</td></tr><tr><td>11</td><td>—</td><td>—</td><td>5</td><td>13</td><td>17</td><td>—</td></tr><tr><td>13</td><td>—</td><td>11</td><td>1</td><td>—</td><td>7</td><td>—</td></tr><tr><td>17</td><td>—</td><td>13</td><td>—</td><td>7</td><td>5</td><td>—</td></tr></table> Further calculate the order of elements 17 and 7. Also find the <u>subgroup</u> generated by 13.	$\times_{18}$	1	5	7	11	13	17	1	1	—	—	—	—	—	5	—	7	—	1	—	—	7	—	17	13	—	—	11	11	—	—	5	13	17	—	13	—	11	1	—	7	—	17	—	13	—	7	5	—	[4]
$\times_{18}$	1	5	7	11	13	17																																													
1	1	—	—	—	—	—																																													
5	—	7	—	1	—	—																																													
7	—	17	13	—	—	11																																													
11	—	—	5	13	17	—																																													
13	—	11	1	—	7	—																																													
17	—	13	—	7	5	—																																													
4.	Let $f = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 2 & 1 & 4 & 3 \end{pmatrix}$ and $g = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 3 & 1 & 4 & 2 \end{pmatrix}$ be the element of permutation group $S_4$ . Compute $f^{-1}og^{-1}$ . What is the nature of permutations $f$ and $g$ (even/odd)?	[3]																																																	
5.	Simplify the following Boolean expression $(x' + y).(yz')'.z'$ and hence find Conjunctive Normal Form	[3]																																																	