\*) Vectors & Matrices callection of the wordinates of a point in space. geometrically, ray connecting origin to the point. · vector quantified using magnitude and direction magnibude: \((x1) 2 H(x2)2 rector representation root of the sum of the square of the coordinates of the point represented / × ×; \* by the rector norm of possible to have same mag, but absolutely the vector different directions. cudidean some direction and different magnitude. for ex. points on the line, y=x. Eudidean space: space in any finite no. of dimensions, in which points are designated by coordinates. (One for each dimension) distance computed using the cuclidean distance formula

( ) adding 1 vectors (even subtraction) point wise addition giving another same for a dimensions genetrically, subtraction would be addition of the revisce of the vector to be subtracted. (.) multiplying 2 vectors (dot product) -> elementwise, resultant: scalar  $\begin{bmatrix} -2 \\ 1 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 1.5 \end{bmatrix} = -2 + 1.5$ U= [U, U2] (R2) rector belong to 2 coordinate system. R" for a coordinate system dot product (U,V) . U.V = UT transpose vector in direction (0) unit vector: any vector of magnitude 1, ex. (1,0), or (0,1) vector in the same direction as a given direction. but whose magnitude = 1. dividing the rector by its own magnitude  $(2,1.5) = \frac{(2,1.5)}{2.5} = \frac{1}{2.5} \begin{bmatrix} 2 \\ 1.5 \end{bmatrix} = \begin{bmatrix} 0.8 \\ 0.6 \end{bmatrix}$ 

(.) projecting a vector outo another

projection of 
$$\vec{x}$$
 on  $\vec{y}$ .

projection of  $\vec{x}$  on  $\vec{y}$ .

projection  $\vec{x}$  =  $\begin{pmatrix} \vec{x} \cdot \vec{y} \\ |\vec{y}| \end{pmatrix} \vec{y}$ 

Frojection  $\vec{y}$ 

conscience tion as  $\vec{y}$ 

scaled down or scaled up version

of  $\vec{y}$ 

0. project 
$$\vec{x} = [2, 2]$$
 on  $\vec{y} = [0, 1]$ 

$$prof_{\vec{y}}\vec{x} = \frac{2}{1}[0] = [0]$$

Q. project = [1,2,5] on y = [2,2,1]

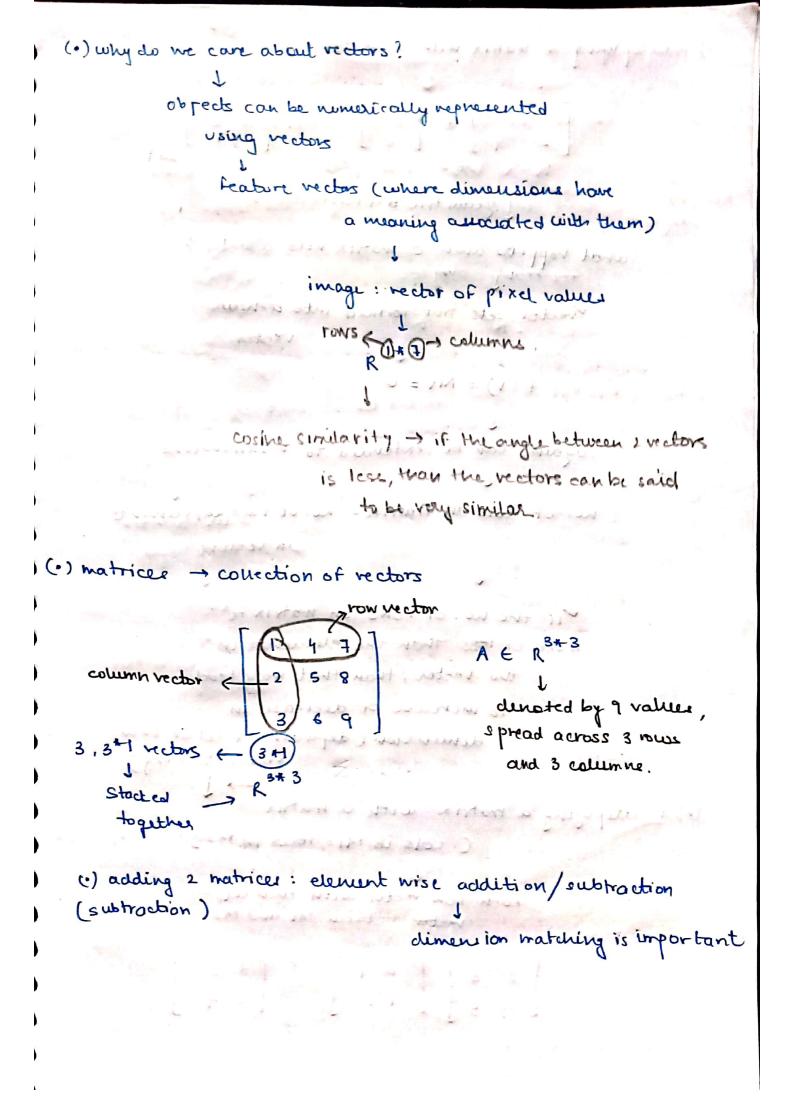
$$prof_{\vec{y}}, \vec{x} = \frac{11}{q} \cdot \begin{bmatrix} 2 \\ 2 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} \frac{22}{q}, \frac{22}{q}, \frac{11}{q} \end{bmatrix}$$

( ) angle blw 2 vectors 
$$\Rightarrow \vec{x} \cdot \vec{y} = x y \cos \theta$$

$$\cos^{-1}\left(\frac{\vec{x} \cdot \vec{y}}{|x| \cdot |y|}\right) = 0$$

(.) orthogonal vectors  $\rightarrow$  vectors that are  $\perp$  to each other.  $\vec{x}^2 \cdot \vec{y} = 0$ 



(.) multiplying a matrix with a vector

$$\begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix} * \begin{bmatrix} 5 \\ c \end{bmatrix} = \begin{bmatrix} 23 \\ 34 \end{bmatrix}$$

$$2 * 2$$

$$2 * 1$$

I geometric o interpretation

what happens when a matrix hits a vector?

Vector gets transformed into a new vector

f (v) = Mv = U

again, can be extended to a dimensions

no. of cols in matrix = no. of rows in rector

1

more or tess than the elements in
the vector, than that may lead
to increase or decrease in
dimension (depending on color now
rector stacking)

( cols in MI = rows in M2)

each now vector with each cel vector between MI and M2.

$$\begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} 3 & 2 \\ 5 & 4 \end{bmatrix}.$$

(+) alternate way of multiplying matrices?

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} = \begin{bmatrix} a_{11} & x & b_{11} & + & a_{12} & x & b_{21} \\ a_{21} & x & b_{11} & + & a_{22} & x & b_{21} \end{bmatrix}$$

$$= \begin{bmatrix} a_{11} & x & b_{11} & + & a_{22} & x & b_{21} \\ a_{21} & x & b_{11} & + & a_{22} & x & b_{21} \end{bmatrix}$$

$$= \begin{bmatrix} a_{11} & x & b_{11} & + & a_{22} & x & b_{21} \\ a_{21} & x & b_{21} & + & a_{22} & x & b_{21} \end{bmatrix}$$

multiplication of resp. vector element with column of matrix and then addition (vector)

1

during combination  $\leftarrow y = mx_1 + nx_2$ of inputs  $b_{11} \begin{bmatrix} a_{11} \\ a_{21} \end{bmatrix}$   $b_{21} \begin{bmatrix} a_{12} \\ a_{21} \end{bmatrix}$  case the elector

in this case, the ofp can

be called the linear

combination of the cols of the natrix, where the coefficients are the clements of the rector

1

extending this to a matrix, each column in the 2nd matrix would represent the linear combination with that particular column rector

$$\begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} * \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}$$

$$b_{11} * \begin{bmatrix} a_{11} \\ a_{21} \end{bmatrix} + b_{21} * \begin{bmatrix} a_{12} \\ a_{22} \end{bmatrix} \rightarrow \text{ first col.}$$

$$b_{12} * \begin{bmatrix} a_{11} \\ a_{21} \end{bmatrix} + b_{22} * \begin{bmatrix} a_{12} \\ a_{12} \end{bmatrix} \rightarrow \text{ Second col.}$$

$$a_{21} = b_{22} * \begin{bmatrix} a_{12} \\ a_{21} \end{bmatrix} + b_{22} * \begin{bmatrix} a_{12} \\ a_{21} \end{bmatrix} \rightarrow \text{ Second col.}$$

(.) Why dowe care about matrices? are of the most common operation in DL (trial resultant sample vector dimension) for many samples edded for (3+4) \*(4+1) +(8+1) each sange (3#1) a divation for hext layer No. of camples in the dataset () Linear combination V1, V2 , . . . . , Vn in Kn add all vectors, which could be individually scaled up or scaled down. CIY + C2 V2 + C3 V3 + ... + CHVH  $\vec{a} = \begin{bmatrix} 1 \\ 2 \end{bmatrix} \vec{b} = \begin{bmatrix} 0 \\ 3 \end{bmatrix}$  $8\vec{a}' + (-2\vec{b}') = \begin{bmatrix} 3 \\ 6 \end{bmatrix} - \begin{bmatrix} 0 \\ 6 \end{bmatrix} \cdot \begin{bmatrix} 3 \\ 0 \end{bmatrix}$ 

(.) any point of the R2 can be shown to be a linear combination of a and b.

(r) span of the rectors a and b' equals R2 (all rectors in R2) i. e. any vector in R2 can be represented as a linear combination of a and b'.

not any two vectors can have a span of K2.

span(0) = 0 (only vector I canget as the linear combination of 0 is 0 itsect)

span (a'): au metors possible by scaling this vector

two non-colinear vectors can have a span of K2.

most common vectors: 1, f (basis of R2)

span: space of all the vectors that can be nep resented by the linear combination of the rectors.

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