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This cookbook integrates various topics in probability theory and statistics, based on literature [1, 6, 3] and in-class material from courses of the statistics department at the University of California in Berkeley but also influenced by others [4, 5]. If you find errors or have suggestions for improvements, please get in touch at <http://statistics.zone/>.