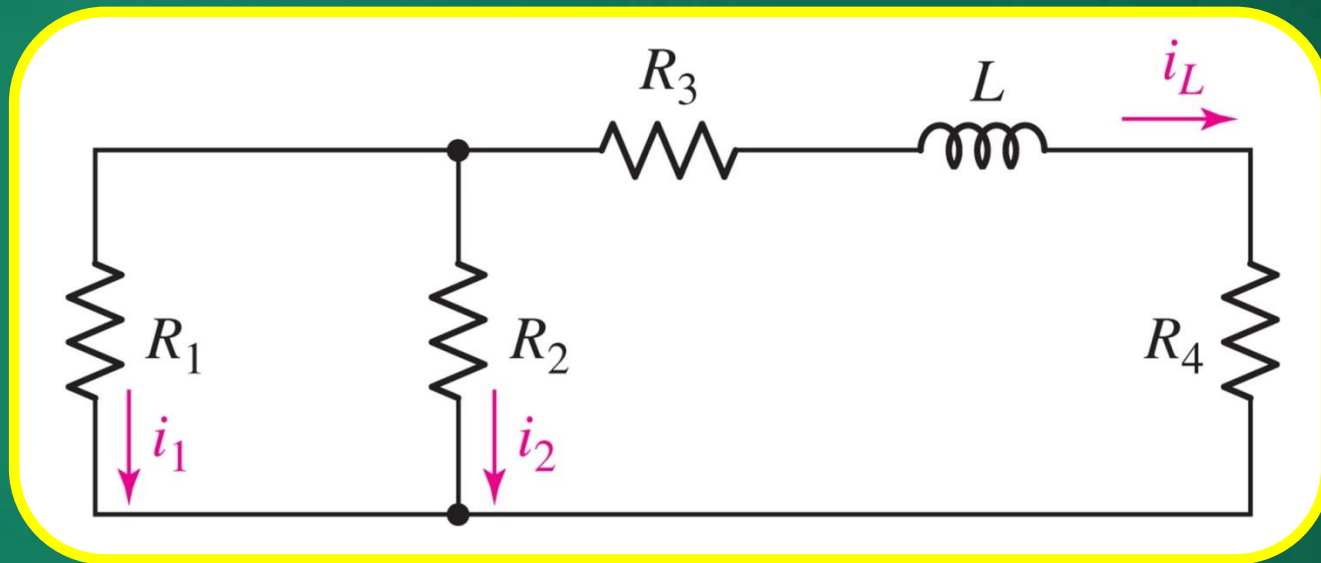


Electrical Science - I

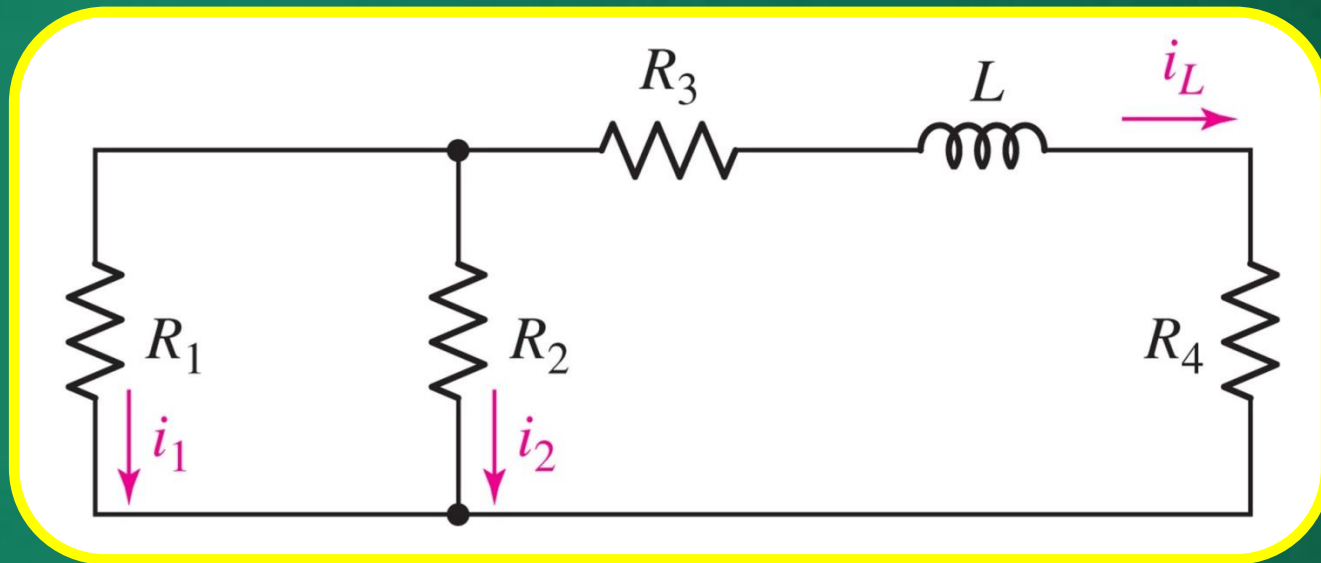
(IEC-102)

Lecture-07

General RL Circuits

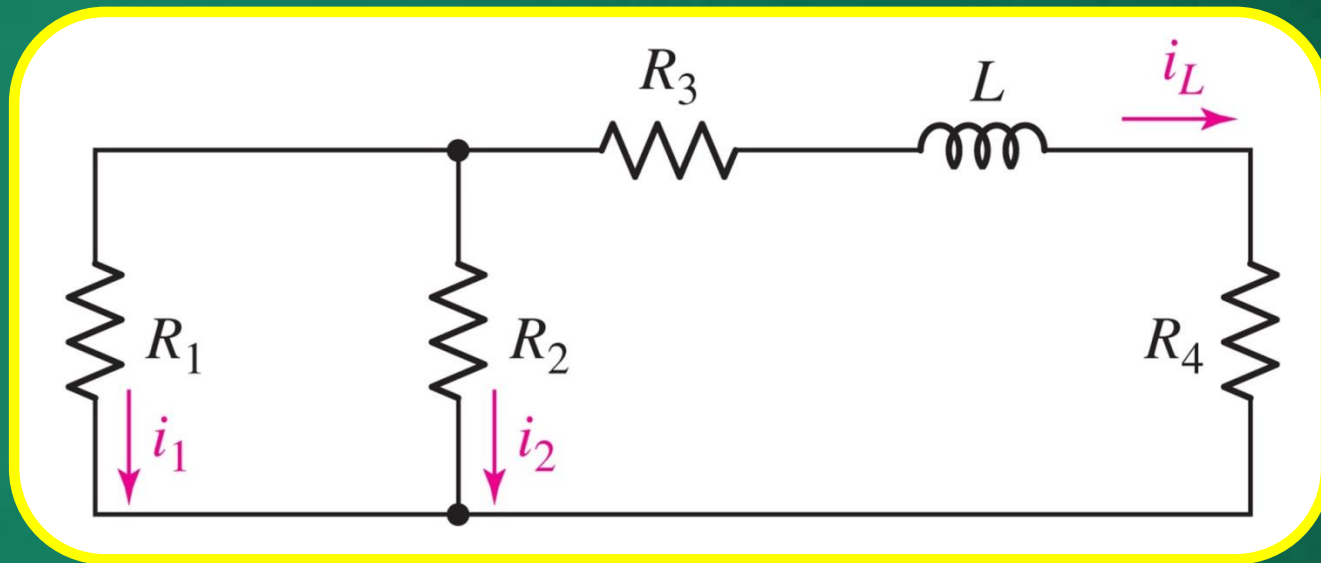


General RL Circuits



The time constant of a single-inductor circuit will be $\tau = L/R_{eq}$ where R_{eq} is the resistance seen by the inductor.

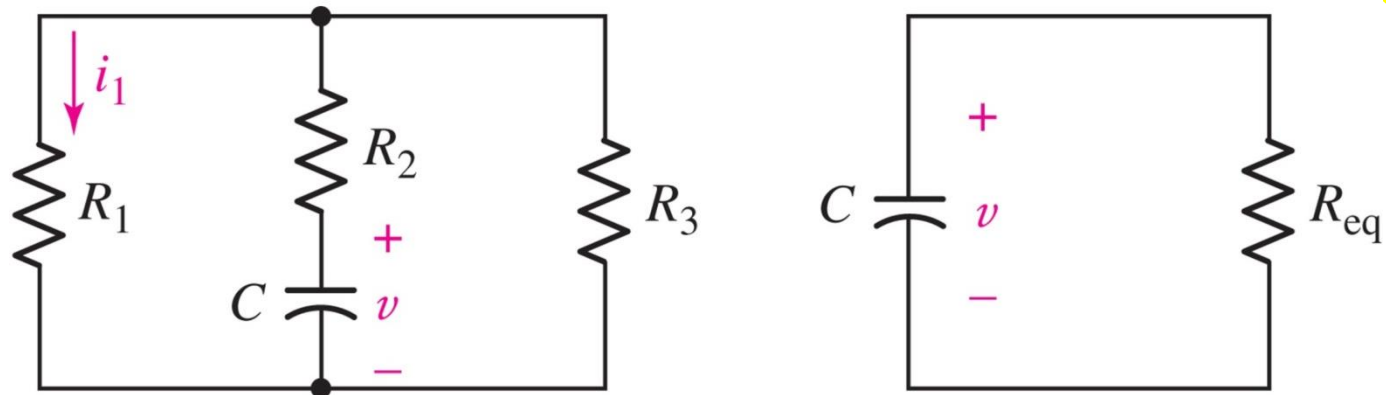
General RL Circuits



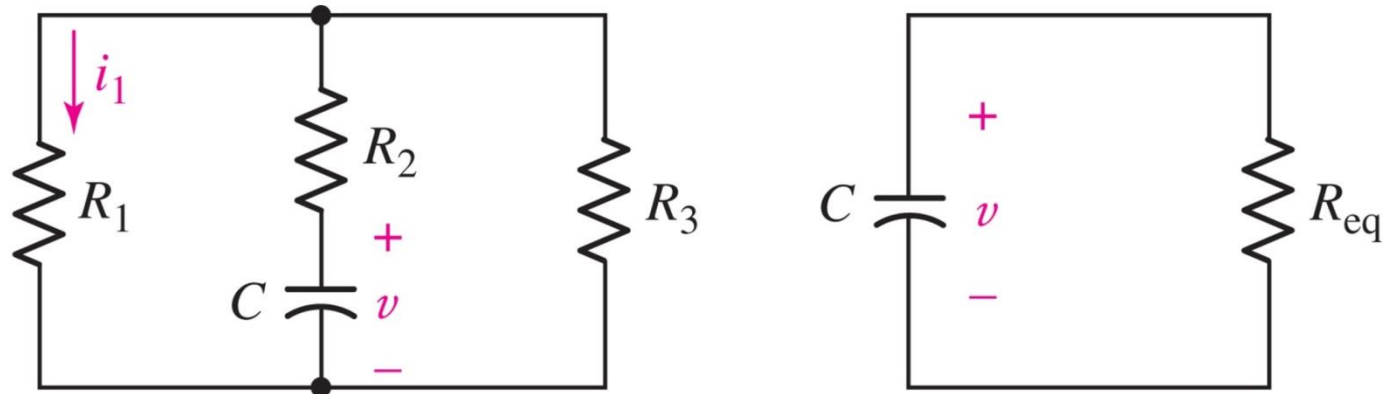
The time constant of a single-inductor circuit will be $\tau = L/R_{eq}$ where R_{eq} is the resistance seen by the inductor.

$$R_{eq} = R_3 + R_4 + R_1 R_2 / (R_1 + R_2)$$

General RC Circuits

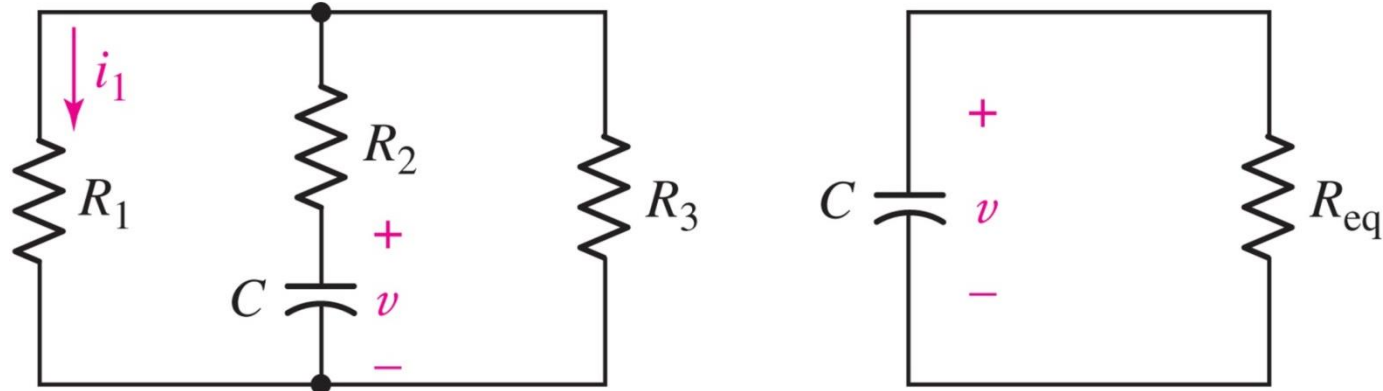


General RC Circuits



The time constant of a single-capacitor circuit will be $\tau = R_{eq}C$ where R_{eq} is the resistance seen by the capacitor.

General RC Circuits



The time constant of a single-capacitor circuit will be $\tau = R_{eq}C$ where R_{eq} is the resistance seen by the capacitor.

$$R_{eq} = R_2 + R_1 R_3 / (R_1 + R_3)$$

1st Order Response Observations

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- The voltage across a capacitor or current through an inductor is the same **prior to and after** switching at $t = 0$.

1st Order Response Observations

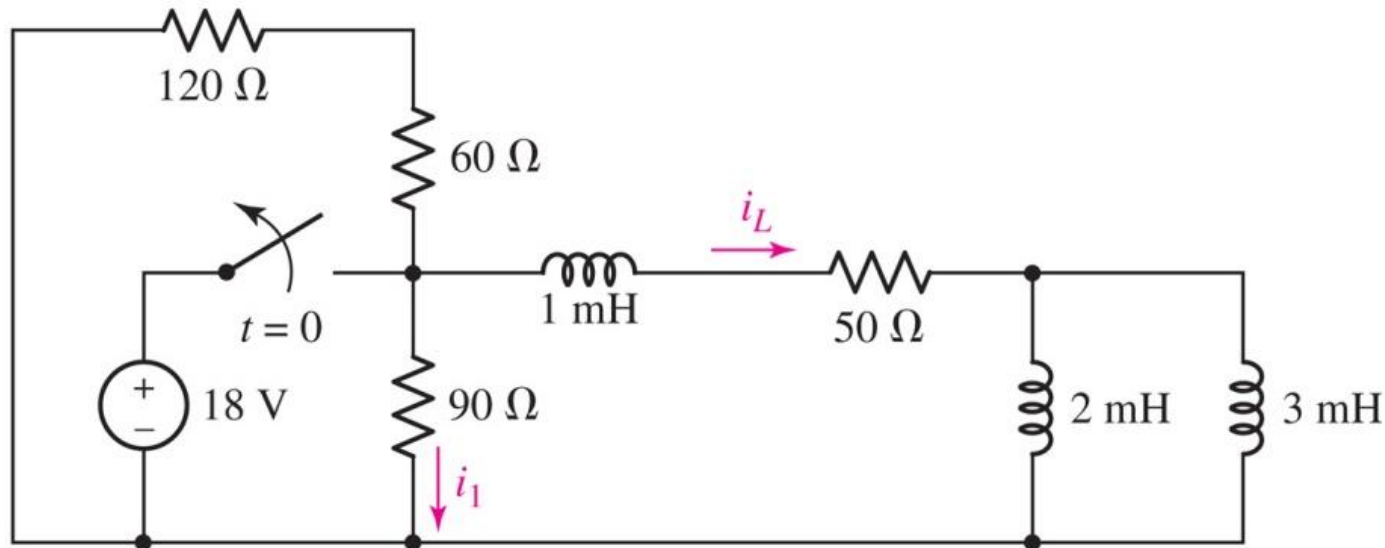
- The voltage across a capacitor or current through an inductor is the same **prior to and after** switching at $t = 0$.
- Resistor voltage (or current) prior to the switch $v(0^-)$ can be different from the voltage after the switch $v(0^+)$.

1st Order Response Observations

- The voltage across a capacitor or current through an inductor is the same **prior to and after** switching at $t = 0$.
- Resistor voltage (or current) prior to the switch $v(0^-)$ can be different from the voltage after the switch $v(0^+)$.
- All voltages and currents in an RC or RL circuit follow the same natural response $e^{-t/\tau}$.

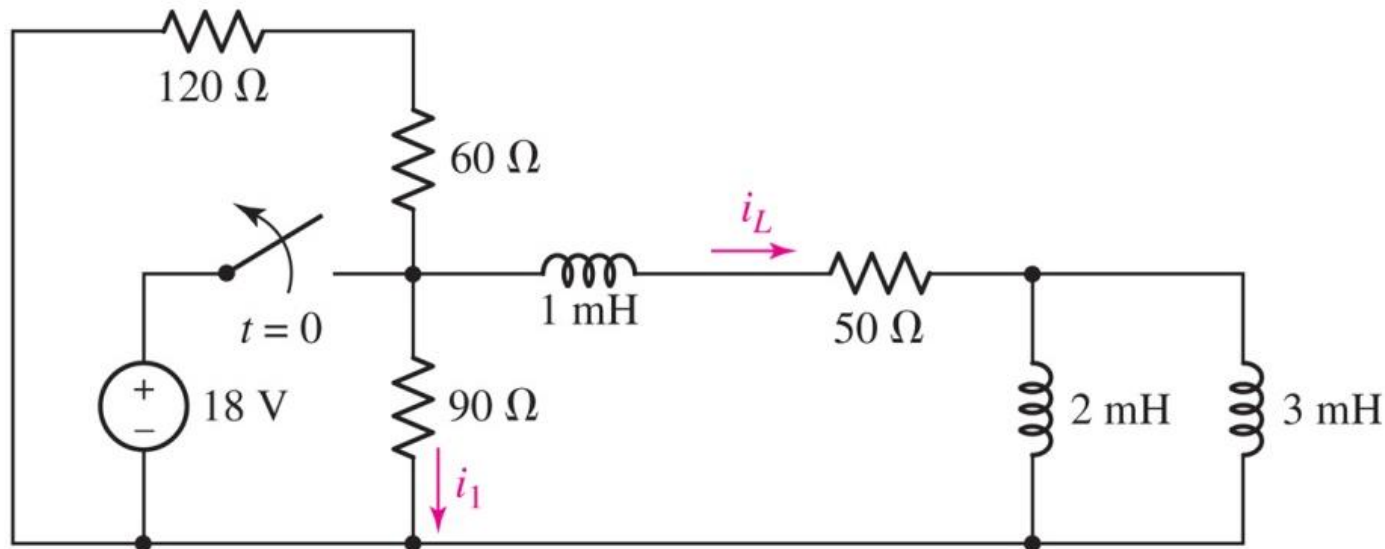
Example: L and R Current

Find τ , $i_1(t)$ and $i_L(t)$ for $t \geq 0$. Given that the circuit is in steady state at $t = 0^-$.



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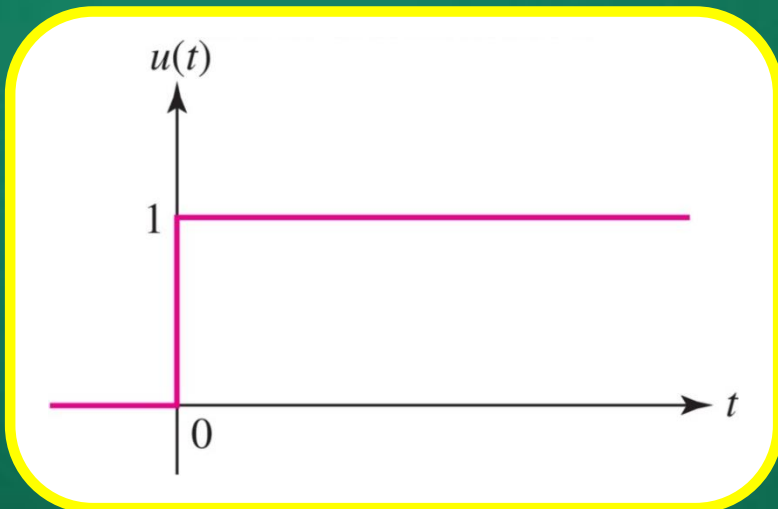
Answer: $\tau = 20 \mu\text{s}$; $i_1 = -0.24e^{-t/\tau}$; $i_L = 0.36e^{-t/\tau}$ for $t \geq 0$

The Unit Step Function

The unit-step function $u(t)$ is a convenient notation to represent change.

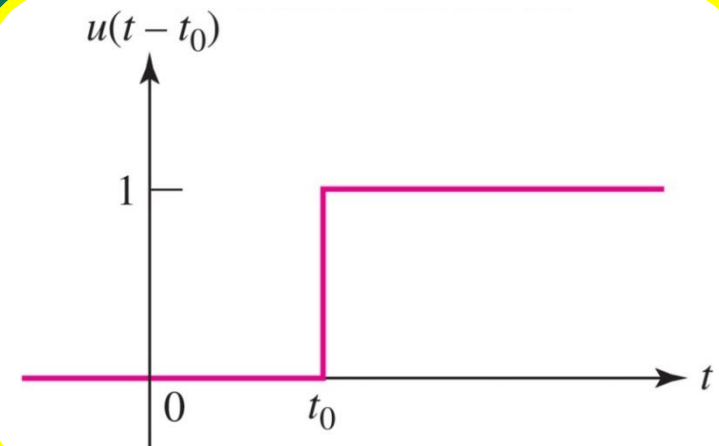
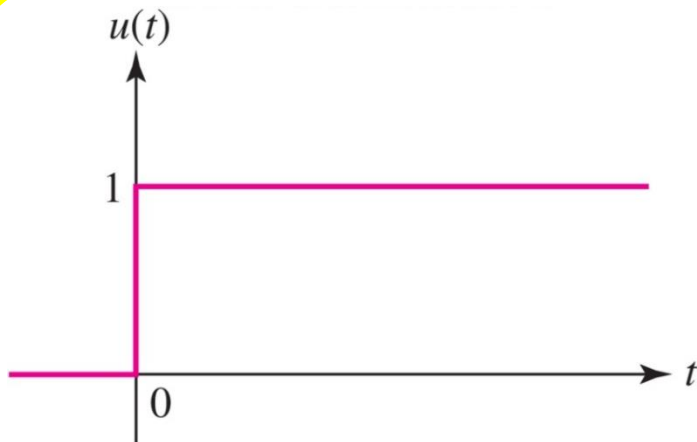
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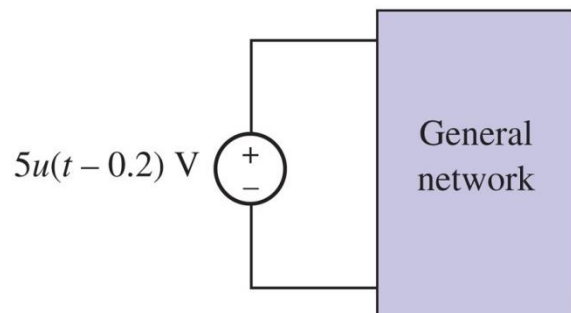


The Unit Step Function

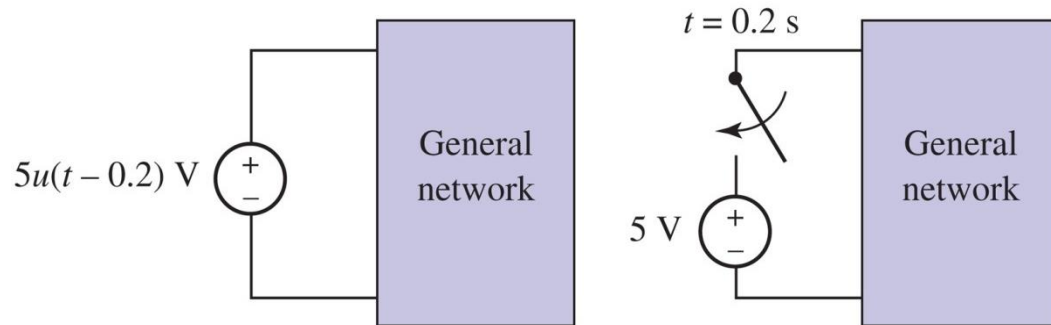
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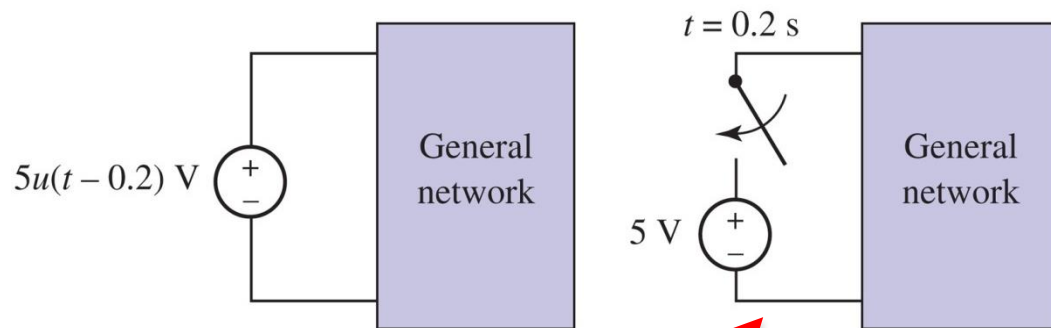
Switches and Steps



Switches and Steps

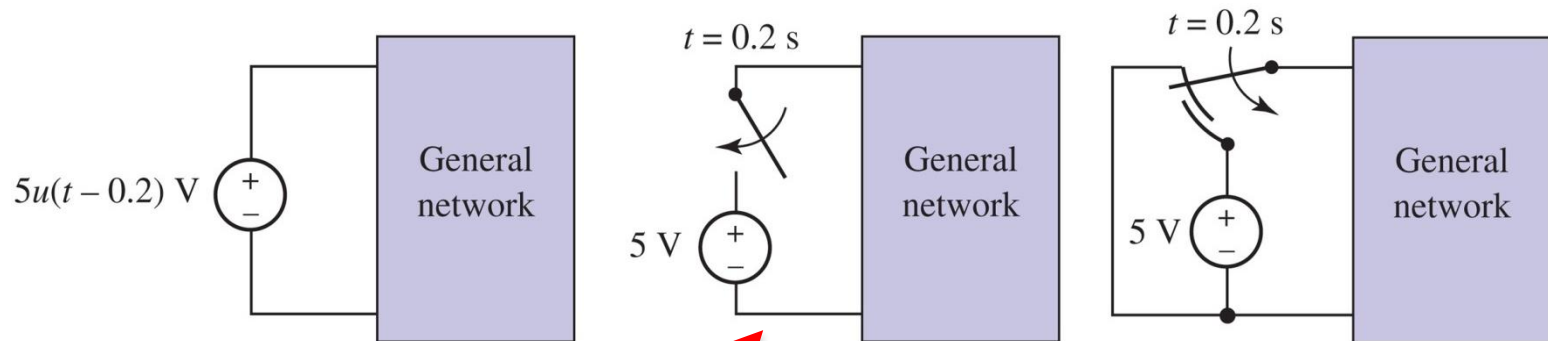


Switches and Steps



A single-throw switch shown is open circuit for $t < 0$, not short circuit.

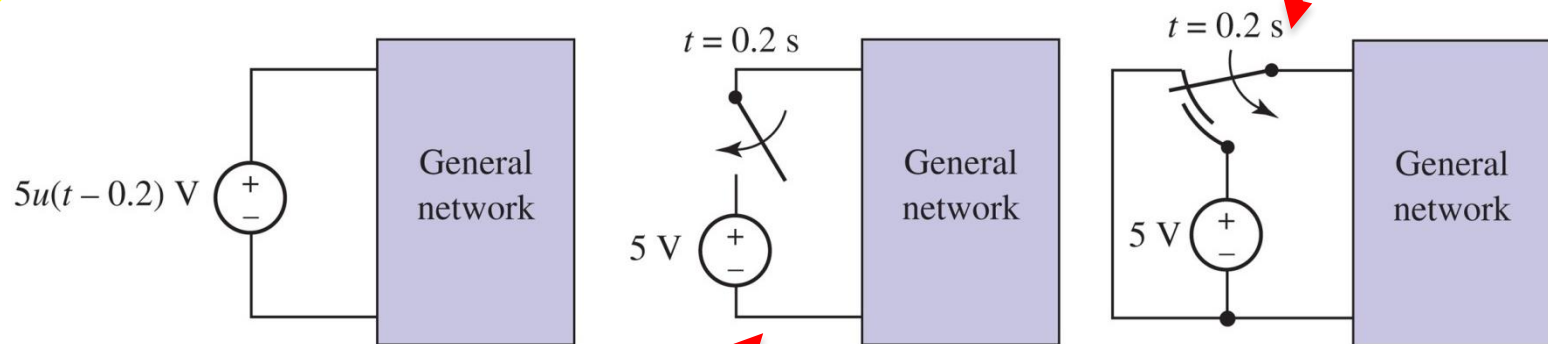
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Switches and Steps

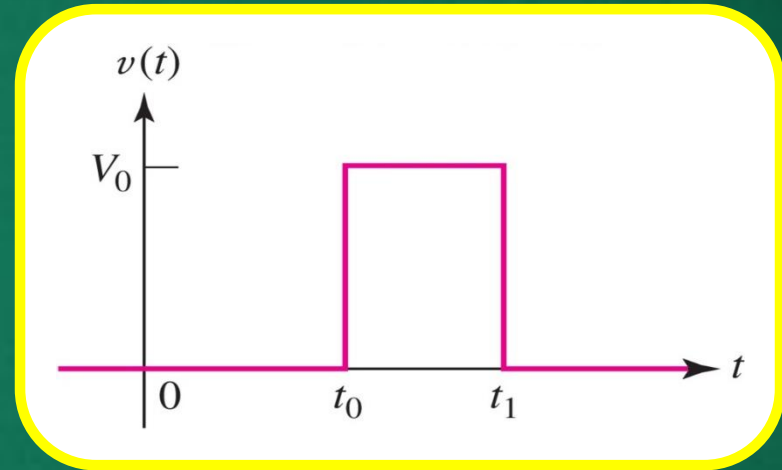
The unit step models a double-throw switch.



A single-throw switch shown is open circuit for $t < 0$, not short circuit.

Modeling Pulses using $u(t)$

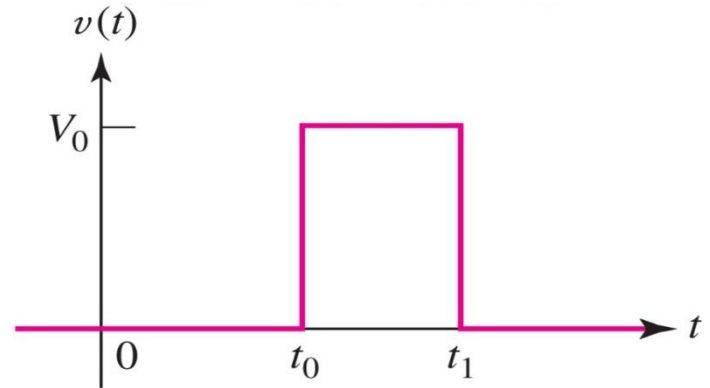
Rectangular pulse



Modeling Pulses using $u(t)$

Rectangular pulse

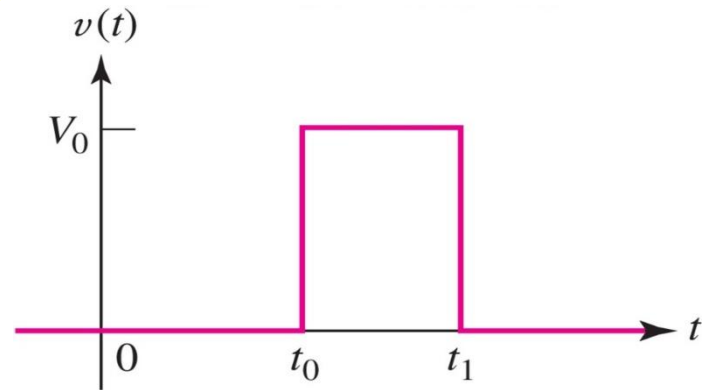
$$v(t) = V_0[u(t-t_0) - u(t-t_1)]$$



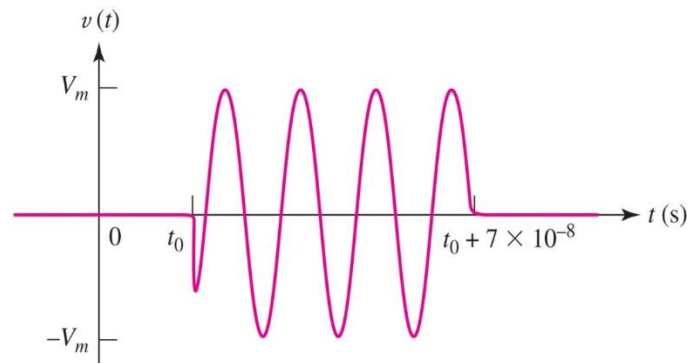
Modeling Pulses using $u(t)$

Rectangular pulse

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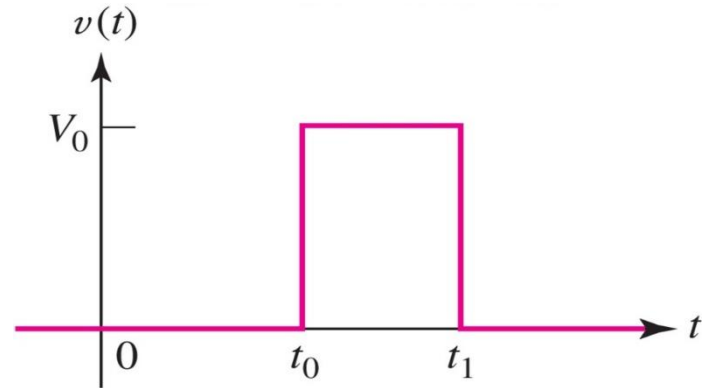
Pulsed sine wave



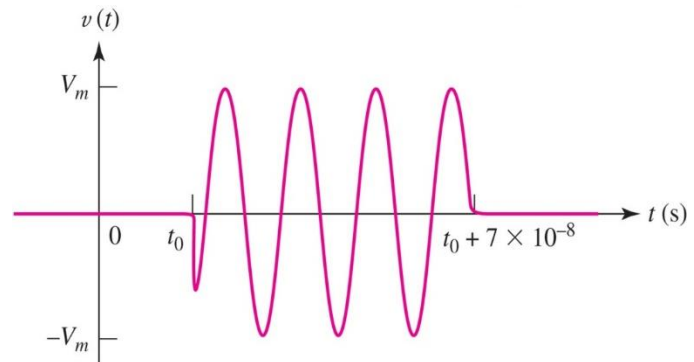
Modeling Pulses using $u(t)$

Rectangular pulse

$$v(t) = V_0[u(t-t_0) - u(t-t_1)]$$



Pulsed sine wave

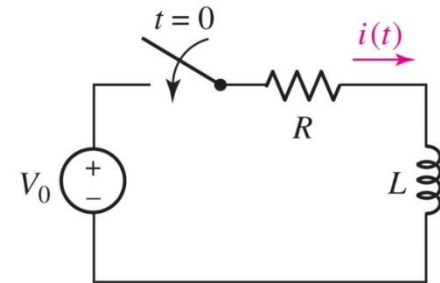


$$v(t) = V_m \sin(\omega_0 t)[u(t-t_0) - u(t-t_1)] \text{ where } t_1 = t_0 + 7 \times 10^{-8} \text{ s}$$

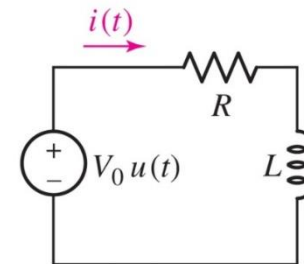
Driven RL and RC Circuits

Driven RL Circuits

The two circuits shown both have $i(t) = 0$ for $t < 0$ and are also the same for $t > 0$.



(a)

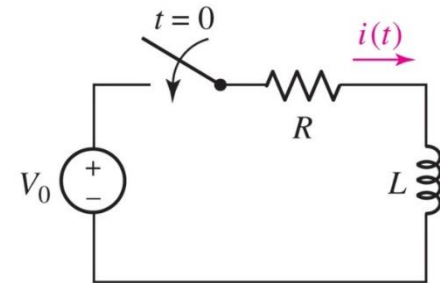


(b)

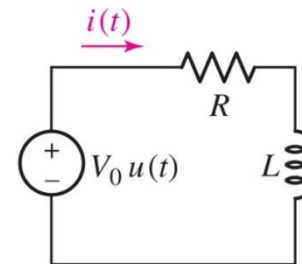
Driven RL Circuits

The two circuits shown both have $i(t) = 0$ for $t < 0$ and are also the same for $t > 0$.

Find both the natural response and the forced response due to the source V_0



(a)

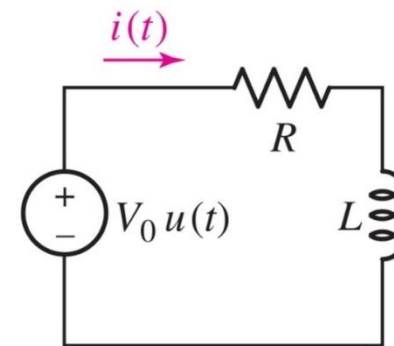
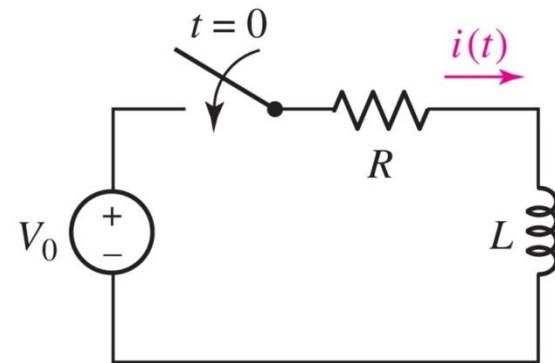


(b)

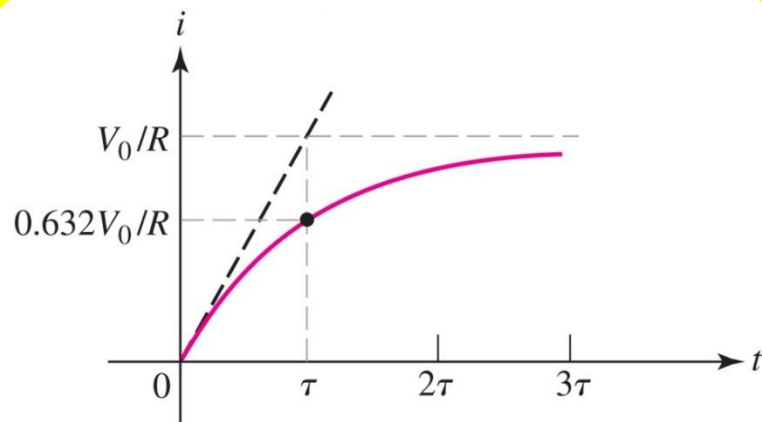
Driven RL Circuits

The total response is the combination of the natural response and the forced response.

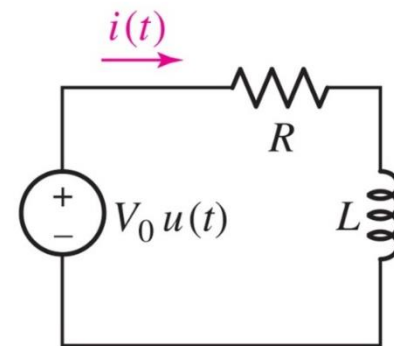
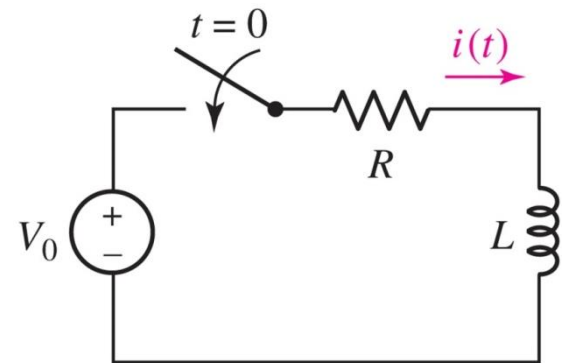
$$i(t) = \frac{V_0}{R} \left(1 - e^{-Rt/L}\right) u(t)$$



Driven RL Circuits

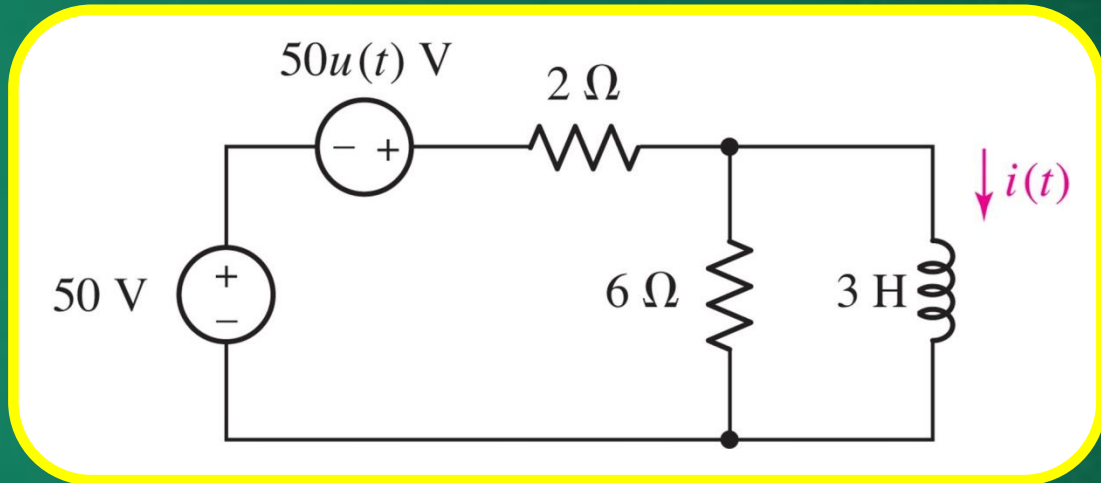


$$i(t) = \frac{V_0}{R} (1 - e^{-Rt/L}) u(t)$$



Example: RL Circuit with Step

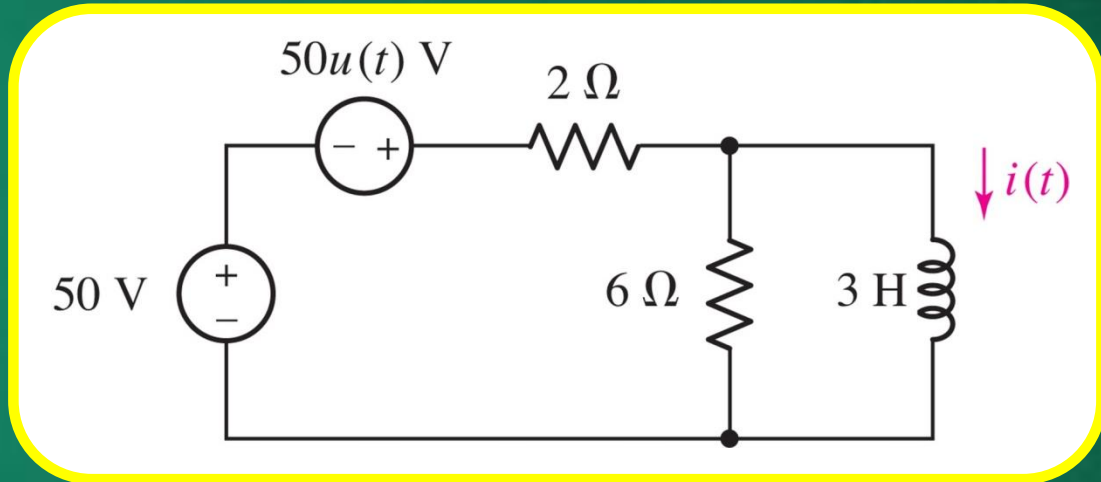
Find $i(t)$ for
 $t \geq 0$.



Given that the circuit is in steady state at $t = 0^-$

Example: RL Circuit with Step

Find $i(t)$ for
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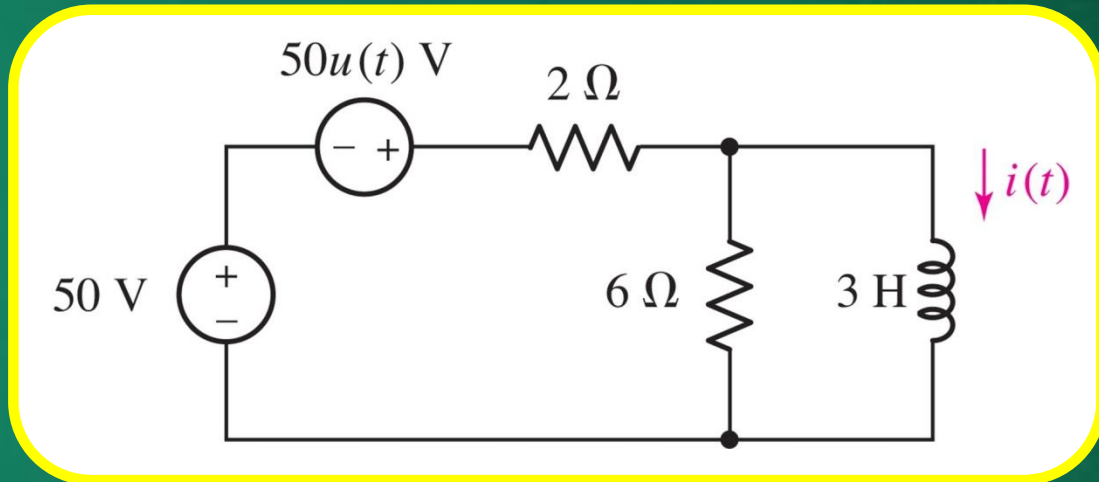


Given that the circuit is in steady state at $t = 0^-$

$$i(t) = 25 + 25(1 - e^{-t/2})u(t) \text{ A}$$

Example: RL Circuit with Step

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