CS 198 Codebreaking at Cal Spring 2023 Homework

HW9

Question 1

Briefly explain why quantum computers pose a threat to cryptography.

Question 2

Let $L \subset \mathbb{R}^2$ be the lattice given by the basis $v_1 = (213, -437)$ and $v_2 = (312, 105)$ and let w = (43127, 11349).

HINT: We recommend doing Lab 9 before doing these questions, as the functions there can help with the computational parts of this problem.

- 1. Use Babai's algorithm to find a vector v that is close to w. Compute the distance ||v w||.
- 2. What is the Hadamard ratio of this basis? Do you think this represents a good basis or a bad basis?
- 3. Show that the vectors $v_1' = (2937, -1555)$ and $v_2' = (11223, -5888)$ are also a basis for L by finding the unimodular matrix U that transforms $\{v_1, v_2\}$ into $\{v_1', v_2'\}$. Recall that a unimodular matrix is one with integer entries and a determinant equal to 1. *HINT: Setup a system of linear equations and solve.*
- 4. Use Babai's algorithm to find a short vector v' that is close to w using this new basis. Compare the norm of this vector to the one you found in part a).
- 5. Compute the Hadamard ratio of this new basis, and conclude whether or not $\{v'_1, v'_2\}$ is a good basis.

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