

## Week 4 – Problem Set

7/10 分 (70%)

测验, 10 个问题



通过所需分数: 80% 或更高

每隔 8 小时, 您最多可以重新进行 3 次 此测验。

[返回到第 4 周](#)[重新测试](#)

1 / 1 分

1。

An attacker intercepts the following ciphertext (hex encoded):

20814804c1767293b99f1d9cab3bc3e7 ac1e37bfb15599e5f40eef805488281d

He knows that the plaintext is the ASCII encoding of the message "Pay Bob 100\$" (excluding the quotes). He also knows that the cipher used is CBC encryption with a random IV using AES as the underlying block cipher.

Show that the attacker can change the ciphertext so that it will decrypt to "Pay Bob 500\$". What is the resulting ciphertext (hex encoded)?

This shows that CBC provides no integrity.

20814804c1767293bd9f1d9cab3bc3e7 ac1e3

**正确答案**

You got it!



0 / 1 分

2。

Let  $(E, D)$  be an encryption system with key space  $K$ , messagespace  $\{0, 1\}^n$  and ciphertext space  $\{0, 1\}^s$ . Suppose  $(E, D)$ 

provides authenticated encryption. Which of the following systems

provide authenticated encryption: (as usual, we use  $\parallel$  to denote

string concatenation)





$$E'((k_1, k_2), m) = E(k_2, E(k_1, m)) \quad \text{and}$$

## Week 4 - Problem Set

测验, 10 个问题

$$D'((k_1, k_2), c) = \begin{cases} D(k_1, D(k_2, c)) & \text{if } D(k_2, c) \neq \perp \\ \perp & \text{otherwise} \end{cases}$$

7/10 分 (70%)

正确

$(E', D')$  provides authenticated encryption because an attack on  $(E', D')$

gives an attack on  $(E, D)$ . It's an interesting exercise to work out

the ciphertext integrity attack on  $(E, D)$  given a ciphertext integrity

attacker on  $(E', D')$ .



$$E'(k, m) = [c \leftarrow E(k, m), \text{ output } (c, c)] \quad \text{and}$$

$$D'(k, (c_1, c_2)) = \begin{cases} D(k, c_1) & \text{if } c_1 = c_2 \\ \perp & \text{otherwise} \end{cases}$$

这应该被选择



$$E'(k, m) = (E(k, m), H(m)) \quad \text{and}$$

$$D'(k, (c, h)) = \begin{cases} D(k, c) & \text{if } H(D(k, c)) = h \\ \perp & \text{otherwise} \end{cases}$$

(here  $H$  is some collision resistant hash function)

未选择的是正确的



$$E'(k, m) = (E(k, m), E(k, m)) \quad \text{and}$$

$$D'(k, (c_1, c_2)) = D(k, c_1)$$

这个选项的答案不正确

This system does not provide ciphertext integrity. The attacker

can query for  $E'(k, 0^n)$  to obtain  $(c_1, c_2)$ . It then outputs

$(c_1, 0^s)$  and wins the ciphertext integrity game.



1 / 1 分

## Week 4 – Problem Set

测验, 10 个问题

7/10 分 (70%)

3.

If you need to build an application that needs to encrypt multiple messages using a single key, what encryption

method should you use? (for now, we ignore the question of key generation and management)

- ☐ use a standard implementation of randomized counter mode.
- ☐ use a standard implementation of CBC encryption with a random IV.
- ☐ implement OCB by yourself
- ☒ use a standard implementation of one of the authenticated encryption modes GCM, CCM, EAX or OCB.



正确



1 / 1 分

4.

Let  $(E, D)$  be a symmetric encryption system with message space  $M$  (think of  $M$  as only consisting for short messages, say 32 bytes).

Define the following MAC  $(S, V)$  for messages in  $M$ :

$$S(k, m) := E(k, m) \quad ; \quad V(k, m, t) := \begin{cases} 1 & \text{if } D(k, t) = m \\ 0 & \text{otherwise} \end{cases}$$

What is the property that the encryption system  $(E, D)$  needs to satisfy for this MAC system to be secure?

- ☒ ciphertext integrity



正确

Indeed, ciphertext integrity prevents existential forgery under a chosen message attack.



perfect secrecy



semantic security

## Week 4 – Problem Set

7/10 分 (70%)

测验, 10 个问题



semantic security under a chosen plaintext attack



1 / 1 分

5.

In Key Derivation we discussed how to derive session keys

from a shared secret. The problem is what to do when the shared

secret is non-uniform. In this question we show that using a PRF with

a *non-uniform* key may result in non-uniform values. This shows thatsession keys cannot be derived by directly using a *non-uniform*

secret as a key in a PRF. Instead, one has to use a key derivation

function like HKDF.

Suppose  $k$  is a *non-uniform* secret key sampled from the key space  $\{0, 1\}^{256}$ .

In particular,  $k$  is sampled uniformly from the set of all keys whose most significant

128 bits are all 0. In other words,  $k$  is chosen uniformly from a small subset of the key space. More precisely,

$$\text{for all } c \in \{0, 1\}^{256} : \Pr[k = c] = \begin{cases} 1/2^{128} & \text{if } \text{MSB}_{128}(c) = 0^{128} \\ 0 & \text{otherwise} \end{cases}$$

Let  $F(k, x)$  be a secure PRF with input space  $\{0, 1\}^{256}$ . Which

of the following is a secure PRF when the key  $k$  is uniform in the

key space  $\{0, 1\}^{256}$ , but is insecure when the key is sampled from the *non-uniform*

distribution described above?



$$F'(k, x) = \begin{cases} F(k, x) & \text{if } \text{MSB}_{128}(k) \neq 0^{128} \\ 1^{256} & \text{otherwise} \end{cases}$$



正确

$F'(k, x)$  is a secure PRF because for a uniform key  $k$  the

probability that  $\text{MSB}_{128}(k) = 0^{128}$  is negligible.

## Week 4 – Problem Set

测验, 10 个问题

7/10 分 (70%)

However, for the \*non-uniform\* key  $k$  this PRF always outputs 1

and is therefore completely insecure. This PRF cannot be used as a

key derivation function for the distribution of keys described in the problem.

☐  $F'(k, x) = \begin{cases} F(k, x) & \text{if } \text{MSB}_{128}(k) \neq 1^{128} \\ 1^{256} & \text{otherwise} \end{cases}$

☐  $F'(k, x) = \begin{cases} F(k, x) & \text{if } \text{MSB}_{128}(k) \neq 1^{128} \\ 0^{256} & \text{otherwise} \end{cases}$

☐  $F'(k, x) = F(k, x)$



0 / 1 分

6.

In what settings is it acceptable to use *deterministic* authenticated encryption (DAE) like SIV?

- ☐ when the encryption key is used to encrypt only one message.
- ☒ when a fixed message is repeatedly encrypted using a single key.

**这个选项的答案不正确**

This would be insecure because an attacker can tell that all the resulting ciphertexts are an encryption of the same message.

- ☐ to individually encrypt many packets in a voice conversation with a single key.
- ☐ to encrypt many records in a database with a single key when the same record may repeat multiple times.



0 / 1 分

7.

Let  $E(k, x)$  be a secure block cipher. Consider the following

## Week 4 - Problem Set

Tweakable block cipher:

7/10 分 (70%)

测验, 10 个问题

$$E'((k_1, k_2), t, x) = E(k_1, x) \oplus E(k_2, t) .$$

Is this tweakable block cipher secure?

☐ no because for  $t \neq t'$  we have

$$E'((k_1, k_2), t, 0) \oplus E'((k_1, k_2), t, 1) = E'((k_1, k_2), t', 0) \oplus E'((k_1, k_2), t', 1)$$

☐ no because for  $t \neq t'$  we have

$$E'((k_1, k_2), t, 0) \oplus E'((k_1, k_2), t', 1) = E'((k_1, k_2), t', 1) \oplus E'((k_1, k_2), t', 0)$$

☒ no because for  $x \neq x'$  and  $t \neq t'$  we have

$$E'((k_1, k_2), t, x) \oplus E'((k_1, k_2), t', x) = E'((k_1, k_2), t, x') \oplus E'((k_1, k_2), t', x)$$



这个选项的答案不正确

This relation doesn't hold for  $E'$ .

☐ no because for  $x \neq x'$  we have

$$E'((k_1, k_2), 0, x) \oplus E'((k_1, k_2), 0, x) = E'((k_1, k_2), 0, x') \oplus E'((k_1, k_2), 0, x')$$

☐ yes, it is secure assuming  $E$  is a secure block cipher.



1 / 1 分

8.

In Format Preserving Encryption we discussed format preserving encryption

## Week 4 – Problem Set

测验, 10 个问题

7/10 分 (70%)

where a PRP is defined on a domain  $\{0, \dots, s-1\}$  for some pre-specified value of  $s$ .

Recall that the construction we presented worked in two steps, where the second step worked by iterating the PRP until the output fell into the set  $\{0, \dots, s-1\}$ .

Suppose we try to build a format preserving credit card encryption system from AES using *only* the second step. That is, we start with a PRP with domain  $\{0, 1\}^{128}$  from which we want to build a PRP with domain  $10^{16}$ . If we only used step (2), how many iterations of AES would be needed in expectation for each evaluation of the PRP with domain  $10^{16}$ ?

- ☐  $2^{128}$
- ☐ 2
- ☒  $2^{128}/10^{16} \approx 3.4 \times 10^{22}$
- ☐

正确

On every iteration we have a probability of  $10^{16}/2^{128}$  of falling into the set  $\{0, \dots, 10^{16}\}$  and therefore in expectation we will need  $2^{128}/10^{16}$  iterations. This should explain why step (1) is needed.

- ☐  $10^{16}/2^{128}$



1 / 1 分

9.

Let  $(E, D)$  be a secure tweakable block cipher.

## Week 4 – Problem Set

7/10 分 (70%)

测验, 10 个问题

Define the following MAC  $(S, V)$ :

$$S(k, m) := E(k, m, 0) \quad ; \quad V(k, m, \text{tag}) := \begin{cases} 1 & \text{if } E(k, m, 0) = \text{tag} \\ 0 & \text{otherwise} \end{cases}$$

In other words, the message  $m$  is used as the tweak and the plaintext given to  $E$  is always set to 0.

Is this MAC secure?

☐ it depends on the tweakable block cipher.

☒ yes

正确

A tweakable block cipher is indistinguishable from a

collection of random permutations. The chosen message attack on the

MAC gives the attacker the image of 0 under a number of the

permutations in the family. But that tells the attacker nothing about

the image of 0 under some other member of the family.

☐ no



1 / 1 分

10.

In [CBC Padding Attacks](#) we discussed padding oracle attacks. These chosen-ciphertext attacks can break poor implementations of MAC-then-encrypt.

Consider a system that implements MAC-then-encrypt where encryption is done using CBC with a random IV using AES as the block cipher. Suppose the system is vulnerable to a padding oracle attack. An attacker intercepts a 64-byte ciphertext  $c$  (the first 16 bytes of  $c$  are the IV and the remaining 48 bytes are the encrypted payload). How many chosen ciphertext queries would the attacker need *in the worst case* in order to decrypt the entire 48 byte payload? Recall that padding oracle attacks decrypt the payload one byte at a time.

☒ 12288

正确



## Week 4 - Problem Set

测验, 10 个问题

Correct. Padding oracle attacks decrypt the payload one byte at a time. For each byte the attacker needs no more than 256 guesses in the worst case. Since there are 48 bytes total, the number queries needed is  $256 \times 48 = 12288$ .

7/10 分 (70%)

- ☐ 256
  - ☐ 1024
  - ☐ 48
  - ☐ 16384
- 

