
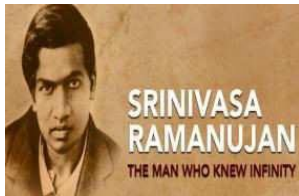


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|  | SRM Institute of Science and Technology Kattankulathur | |  |
| | DEPARTMENT OF MATHEMATICS | | |
| | 18MAB101T Calculus and Linear Algebra | | |
| | UNIT –I Matrices | | |
| Sl.No. | Tutorial Sheet -2 | Answers | |
| Part – A | | | |
| 1 | Verify Cayley Hamilton theorem and find A^4 when $A = \begin{bmatrix} 1 & 2 \\ 2 & -1 \end{bmatrix}$. | $A^4 = \begin{bmatrix} 25 & 0 \\ 0 & 25 \end{bmatrix}$ | |
| 2 | Two eigen values of the matrix $A = \begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$ are equal to 1 each. Find the eigen values of A^{-1} | $A = 1, 1, 5$ $A^{-1} = 1, 1, 1/5$ | |
| 3 | The matrix A is $\begin{bmatrix} -1 & 0 & 0 \\ 2 & -3 & 0 \\ 1 & 4 & 2 \end{bmatrix}$. Find the eigen values of A^2 | $A = -1, 3, 2$ $A^2 = 1, 9, 4$ | |
| 4 | Verify Cayley Hamilton theorem and find A^{-1} when $A = \begin{bmatrix} 3 & 1 & 1 \\ -1 & 5 & -1 \\ 1 & -1 & 3 \end{bmatrix}$. | $A^{-1} = 1/20 \begin{bmatrix} 7 & -2 & -3 \\ 1 & 4 & 1 \\ -2 & 2 & 8 \end{bmatrix}$ | |
| 5 | Verify Cayley Hamilton theorem and find A^{-1} when $A = \begin{bmatrix} 1 & -1 & 1 \\ 0 & 1 & 0 \\ 2 & 0 & 3 \end{bmatrix}$ | $A^{-1} = \begin{bmatrix} 3 & 3 & -1 \\ 0 & 1 & 0 \\ -2 & -2 & 1 \end{bmatrix}$ | |
| 6 | Obtain the matrix $A^6 - 25A^2 + 122A$ where $A = \begin{bmatrix} 0 & 0 & 2 \\ 2 & 1 & 0 \\ -1 & -1 & 3 \end{bmatrix}$. | Ans $\begin{bmatrix} -34 & 0 & -20 \\ -20 & -54 & 0 \\ 10 & 10 & -74 \end{bmatrix}$ | |
| 7 | If $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$, Prove that $A^3 - 3A^2 - 9A - 5I = 0$. Hence find A^4 and A^{-1} . | $A^4 = \begin{bmatrix} 209 & 208 & 208 \\ 208 & 209 & 208 \\ 208 & 208 & 209 \end{bmatrix}$ | |
| 8 | Diagonalise the matrix $A = \begin{bmatrix} 2 & 1 & -1 \\ 1 & 1 & -2 \\ -1 & -2 & 1 \end{bmatrix}$ when | $A^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ | |