
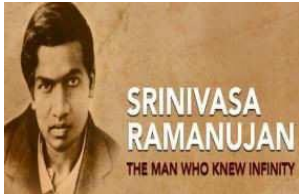


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|  | SRM Institute of Science and Technology Kattankulathur | |  |
| | DEPARTMENT OF MATHEMATICS | | |
| | 18MAB101T Calculus and Linear Algebra | | |
| | UNIT –I Matrices | | |
| Sl.No. | Tutorial Sheet -1 | Answers | |
| Part – A | | | |
| 1 | If $A = \begin{pmatrix} 3 & 5 & 3 \\ 0 & 4 & 6 \\ 0 & 0 & 1 \end{pmatrix}$, find the eigenvalues of (i) A (ii) A^{-1} (iii) adj A (iv) A^3 | (i) 3,4,1 (ii) $1/3, 1/4, 1$ (iii) 12, 4, 3 (iv) 27, 64, 1 | |
| 2 | Two of the eigenvalues of $A = \begin{pmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{pmatrix}$ are 1 and 2. Find the eigenvalues of A^2 . | 1, 4, 9 | |
| 3 | Find the sum and product of the eigenvalues of the matrix $A = \begin{pmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{pmatrix}$ | -1, 45 | |
| 4 | Find the eigenvalues and eigenvectors of the matrix $A = \begin{pmatrix} 4 & 1 \\ 3 & 2 \end{pmatrix}$ | 1, 5 $\begin{pmatrix} 1 \\ -3 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ | |
| 5 | Find the characteristic equation of $A = \begin{pmatrix} 3 & -1 & 1 \\ -1 & 5 & -1 \\ 1 & -1 & 3 \end{pmatrix}$ | $\lambda^3 - 11\lambda^2 + 36\lambda - 36 = 0$ | |
| Part – B | | | |
| 6 | Find the eigenvalues and eigenvectors of $\begin{pmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{pmatrix}$ | 2, 3, 5 $\begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 3 \\ 2 \\ 1 \end{pmatrix}$ | |
| 7 | Find the eigenvalues and eigenvectors of $\begin{pmatrix} 2 & 1 & 1 \\ 2 & 3 & 2 \\ 3 & 3 & 4 \end{pmatrix}$ | 1, 1, 7 $\begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix}, \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$ | |
| 8 | Find the eigenvalues and eigenvectors of $\begin{pmatrix} 6 & -6 & 5 \\ 14 & -13 & 10 \\ 7 & -6 & 4 \end{pmatrix}$ | -1, -1, -1 $\begin{pmatrix} 0 \\ 5 \\ 6 \end{pmatrix}, \begin{pmatrix} 5 \\ 0 \\ -7 \end{pmatrix}, \begin{pmatrix} 6 \\ 7 \\ 0 \end{pmatrix}$ | |

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| 9 | Find the eigenvalues and eigenvectors of $\begin{pmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{pmatrix}$ | 0, 3, 15 $\begin{pmatrix} 1 \\ 2 \\ 2 \end{pmatrix}, \begin{pmatrix} 2 \\ 1 \\ -2 \end{pmatrix}, \begin{pmatrix} 2 \\ -2 \\ 1 \end{pmatrix}$ |
| 10 | Find the eigenvalues and eigenvectors of $\begin{pmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{pmatrix}$ | 8, 2, 2 $\begin{pmatrix} 2 \\ -1 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}$ |