

SRM INSTITUTE OF SCIENCE AND TECHNOLOGY
DEPARTMENT OF MATHEMATICS
18MAB201T/Transforms and Boundary value problems
UNIT II – FOURIER SERIES
TUTORIAL SHEET -1

PART B Questions

1. State Dirichlet condition's for a given function to expand in Fourier series.
2. Find a_1 for the periodic function $f(x) = \begin{cases} \sin x, 0 < x < \pi \\ 0, \pi < x < 2\pi \end{cases}$
3. Find a_0 for the periodic function $f(x) = e^{-x}, 0 < x < 2\pi$.
4. Find a_n for the Fourier series of periodicity 3 for $f(x) = 2x - x^2$ in $0 < x < 3$
5. Find half –range cosine series for $f(x) = x, 0 < x < \pi$

PART C Questions

6. Find the Fourier series to represent $(x - x^2)$ in the interval $[-\pi, \pi]$. Deduce the value of $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \dots$
7. Obtain the Fourier series expansion for $f(x) = x^2$ in $-\pi < x < \pi$ and hence the sum of the series $\frac{1}{1^4} + \frac{1}{2^4} + \frac{1}{3^4} + \dots$
8. If $f(x) = \begin{cases} \sin x, 0 < x < \frac{\pi}{4} \\ \cos x, \frac{\pi}{4} < x < \frac{\pi}{2} \end{cases}$. Express $f(x)$ in a series of sines.
9. Find the Fourier series for $f(x) = |\cos x|$ in $-\pi < x < \pi$ of periodicity 2π .
10. Find the Fourier series for $f(x) = |\sin x|$ in $-\pi < x < \pi$ of periodicity 2π .

Tutorial Sheet-1

Answers

Part-A

1. State any three condition

2. $a_1 = 0$

3. $a_0 = \frac{1 - e^{-2\pi}}{\pi}$.

4. $a_n = \frac{-9}{n^2 \pi^2}$

5. $a_n = \begin{cases} \frac{-4}{\pi n^2}; & \text{if } n \text{ is odd} \\ 0 & \text{if } n \text{ is even} \end{cases}$

Part - B

6. $f(x) = \frac{-\pi^2}{3} + \sum_{n=1}^{\infty} \frac{-4(-1)^n}{n^2} \cos nx + \sum_{n=1}^{\infty} \frac{-2(-1)^n}{n} \sin nx$ and $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \dots = \frac{\pi^2}{3}$

7. $f(x) = \frac{\pi^2}{3} + 4 \sum_{n=1}^{\infty} \frac{(-1)^n}{n^2} \cos nx$ and $\frac{1}{1^4} + \frac{1}{2^4} + \frac{1}{3^4} + \dots = \frac{\pi^4}{90}$

8. $f(x) = \frac{4\sqrt{2}}{\pi} \left\{ \frac{\sin 2x}{1.3} - \frac{\sin 6x}{5.7} + \frac{\sin 10x}{9.11} - \dots \right\}$

9. $f(x) = \frac{2}{\pi} - \frac{4}{\pi} \sum_{n=2}^{\infty} \frac{1}{n^2 - 1} \cos \left(\frac{n\pi}{2} \right) \cos nx$

10. $f(x) = \frac{2}{\pi} - \frac{4}{\pi} \sum_{n=1}^{\infty} \frac{1}{(4n^2 - 1)} \cos 2nx$