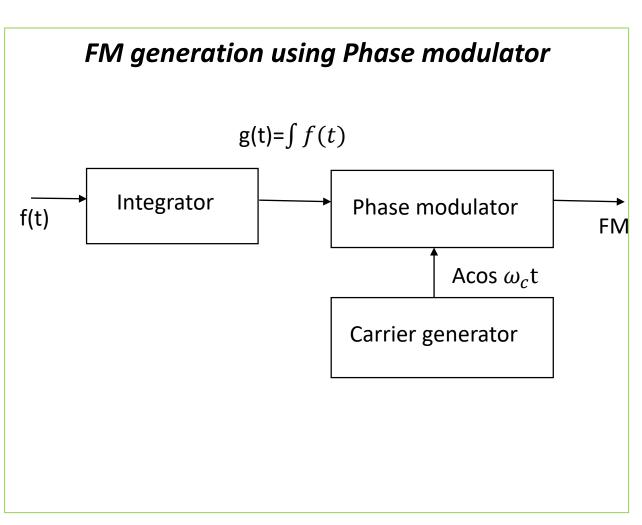
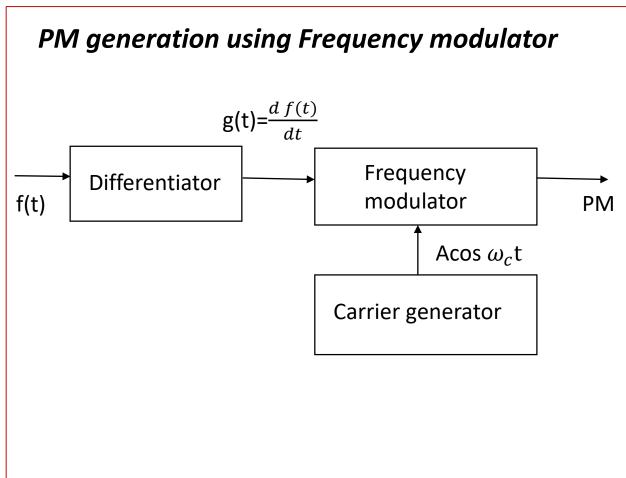
Relationship between PM and FM





Transmission bandwidth of FM signal

- Bandwidth= $2n\omega_m$ where n is the number of sidebands $n{\approx}m_f$
- BW=2 $m_f \omega_m$ =2 $\Delta \omega$ =2 Δf

Bandwidth using Carson's rule

$$BW=2(\Delta\omega+\omega_m)=2(\Delta f+f_m)$$

Depending upon the value of $\Delta\omega$, FM is classified as narrowband FM (NBFM) and wideband FM (WBFM)

Bandwidth of PM signal

BW(PM)
$$\approx 2\Delta\omega$$

= 2K_pE_mω_m

Modulation index of PM signal

$$m_p = K_p E_m = \theta_d$$

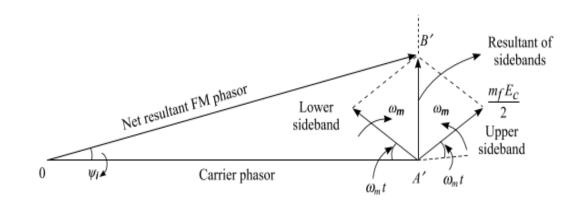


Figure: Phasor diagram of FM

Comparison between NBFM and WBFM

NBFM

- Frequency deviation is very small
- $BW = 2\omega_m$
- K_f is very small
- BW is narrow
- m_f is very small
- Only two sidebands

WBFM

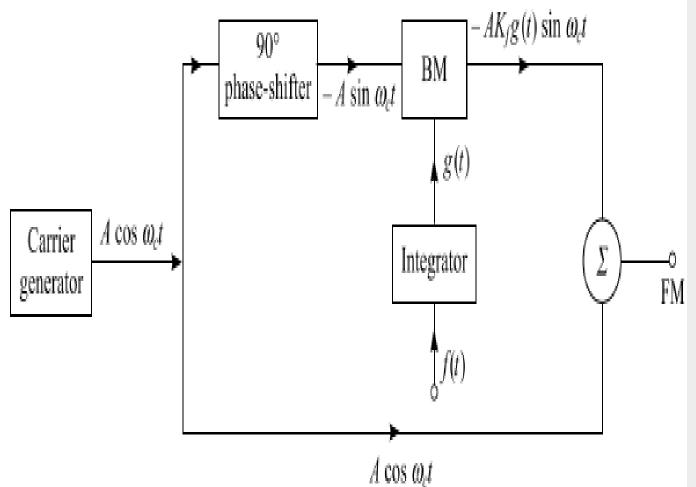
- Frequency deviation is very large
- $BW = 2\Delta\omega$
- K_f is very large
- BW is wide
- m_f is very large
- 'n' number of sidebands

International regulation for FM signal

- The following values are prescribed by CCIR (Consultative Committee for International Radio) for commercial FM broadcast stations.
 - * Maximum frequency deviation $\pm 75 KHz$.
 - * Frequency stability of the carrier $\pm 2KHz$.
 - * Allowable bandwidth per channel = 200KHz.

Power content in FM signal $\frac{A^2}{2}$

Generation of Narrowband FM



Carrier signal Acos ω_c t Phase shifted carrier - $A\sin \omega_c t$ Message signal $f(t) = E_m \cos \omega_m t$ g(t)= $\int f(t) = \int f(t) = \int E_m \cos \omega_m t$ $=\frac{E_m}{\omega_m}\sin\omega_m t$

Output of balanced modulator is

-Asin
$$\omega_c$$
t * $\frac{E_m}{\omega_m}$ sin ω_m t

- $A\sin \omega_c t * \frac{E_m}{\omega_m} \sin \omega_m t$ $\emptyset_{NBFM}(t) = A\cos \omega_c t - KA \frac{E_m}{\omega_m} \sin \omega_m t \sin \omega_c t$

Let
$$K \frac{E_m}{\omega_m} = m_f$$

 $\emptyset_{NBFM}(t) = A\cos \omega_c t - Am_f \sin \omega_m t \sin \omega_c t$

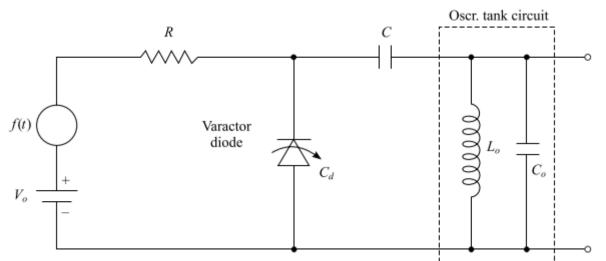
Varactor diode FM modulation

Principle of Operation:

- Modulating signal directly modulates the carrier that is generated by an electronic circuit.
- The oscillator circuit involves a parallel circuit.
- Frequency of oscillation of the carrier generator is

$$\omega_c = \frac{1}{\sqrt{LC}}$$

• The Carrier frequency ω_c can be made to vary according to the modulating signal f(t), if L or C is varied according to f(t).



Operation:

- Varactor diode is a semiconductor diode whose junction capacitance changes with the applied d.c bias voltage.
- The varactor diode is shunted with the oscillator tank circuit.
- $C < C_d$ to keep the r.f voltage from the oscillator across the diode small as compared to V_o , the polarizing voltage.
- X_c at highest modulating frequency is kept large as compared to R.
- V_o is reverse bias voltage across the varactor diode.

• The capacitance C_d of the diode is given by $C_d = K \sqrt{V_D}$ (1) Where V_D is the total instantaneous voltage across the diode K the proportionality constant.

$$V = V_o + f(t) \tag{2}$$

- The total capacitance of the oscillator tank circuit is $(C_o + C_d)$
- The instantaneous frequency of oscillation

$$\omega_i = \frac{1}{\sqrt{L_o(C_o + C_d)}} \tag{3}$$

• Sub (1) in (3), we get
$$\omega_i = \sqrt[4]{\frac{1}{L_o(C_o + K\sqrt{V_D})}}$$
 (4)

• ω_i is dependent on V_D which in turn depends on the modulating signal f(t).

- Distortion due to non-linearity:
- From (4) it is understood that ω_i does not change linearly with V_D .
- This non-linearity produces distortion due to the frequency variations caused by the higher harmonics of the modulating frequency.
- Assume that the oscillator tank circuit comprises only the diode capacitance \mathcal{C}_d and \mathcal{C}_o is absent.

$$\omega_i = \frac{1}{\sqrt{L_o K \sqrt{V_D}}} = \frac{V_D^{\frac{1}{4}}}{(L_o K)^{\frac{1}{2}}}$$
 (5)

The R.H.S of the above equation can be represented by a Taylor series about the polarizing voltage V_o as given below.

$$\frac{V_D^{\frac{1}{4}}}{\frac{1}{(L_o K)^{\frac{1}{2}}}} = \frac{V_o^{\frac{1}{4}}}{\frac{1}{4}} + \frac{(V_D - V_O)}{\frac{3}{2} \cdot \frac{1}{2}} - \frac{3(V_D - V_O)^2}{\frac{7}{2} \cdot \frac{1}{2}}$$

$$(6)$$

• The higher order terms can be neglected if $(V_D - V_o)$ is small.

• Let
$$(V_D - V_o) = \Delta V = f(t) = V_m \sin \omega_m t$$
 (7)
 $(V_D - V_o)^2 = V_m^2 \sin^2 \omega_m t = \frac{V_m^2}{2} (1 - \cos 2\omega_m t)$ (8)

• Sub (7) and (8) in (6)

$$\omega_{i} = \frac{V_{D}^{\frac{1}{4}}}{(L_{o}K)^{\frac{1}{2}}} = \frac{V_{o}^{\frac{1}{4}}}{(L_{o}K)^{\frac{1}{2}}} + \frac{V_{m}\sin\omega_{m}t}{4(L_{o}KV_{o}^{\frac{3}{2}})^{\frac{1}{2}}} - \frac{3V_{m}^{2}}{32(L_{o}KV_{o}^{\frac{3}{2}})^{\frac{1}{2}}} + \frac{3V_{m}^{2}\cos2\omega_{m}t}{32(L_{o}KV_{o}^{\frac{3}{2}})^{\frac{1}{2}}}$$
(9)

• % second harmonic distortion is the ratio of amplitude of the $cos2\omega_m$ term and the fundamental term

9 second harmonic distortion =
$$\frac{3V_m}{V_o}$$
 x 100

By adjusting proper ratio of V_m and V_o second harmonic distortion may be reduced.

Ignoring the effect of second harmonic of f(t)

$$\omega_{i} = \frac{V_{o}^{\frac{1}{4}}}{(L_{o}K)^{\frac{1}{2}}} + \frac{V_{m}\sin\omega_{m}t}{4(L_{o}KV_{o}^{\frac{3}{2}})^{\frac{1}{2}}} = \omega_{c} + (\Delta\omega)\sin\omega_{m}t$$

$$(L_0 K)^2 \quad 4(L_0 K V_0^2)^2$$
Modulation index $m_f = \frac{V_m}{4\omega_m (L_0 K V_0^{\frac{3}{2}})^{\frac{1}{2}}}$

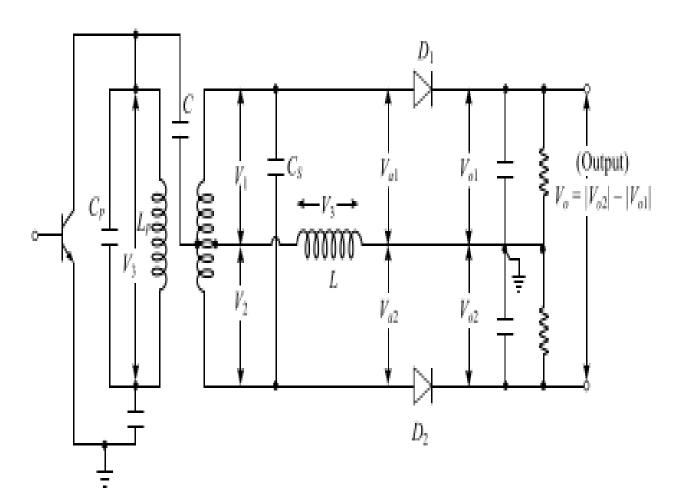
Demodulation of FM signals

- The process of recovering the modulating signal from a modulated carrier is known as demodulation.
- The detector performs the modulation in two steps.
 - FM signal is converted to its corresponding AM signal using frequency dependent circuits (frequency discriminators)
 - The original message signal is recovered from this AM signal by using linear diode detector.

Types of FM discriminators

- 1)Slope detector
 - Simple slope detector or single-tuned discriminator circuit
 - Balanced slope detector or stagger tuned discriminator circuit
- 2)Phase Difference discriminator
 - Foster-Seeley discriminator
 - Ratio detector

Foster-Seeley discriminator



Operation:

- The circuit has inductively coupled doubledtuned circuit
- The primary and secondary are tuned to the same frequency (f_{if})
- Centre of secondary is connected to the collector end of primary through a capacitor C.

Functions of capacitor C

- Blocks d.c from primary to secondary
- Couples the primary signal frequency to center-tapping of secondary.
- The primary voltage V_3 appears across the inductance L.
- The center-tapping of the transformer has equal and opposite winding.
- Hence V_1 and V_2 are equal in magnitude but opposite in phase.

Foster-Seeley discriminator Contd...

• The radio frequency voltages V_{a1} and V_{a2} applied to the diodes D_1 and D_2 are

$$V_{a1} = V_3 + V_1$$
 and $V_{a2} = V_3 - V_2$

- Voltages V_{a1} and V_{a2} depend on the phasor relation between V_1, V_2, V_3 .
- The phasor position of V_1 and V_2 are always equal and are in phase opposition.
- The phase position of V_1 and V_2 relative to V_3 will depend on the tuned secondary at the resonance or off resonance.

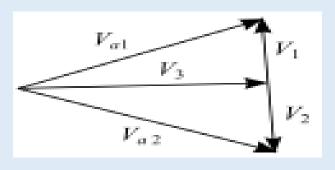
Foster-Seeley discriminator Contd..

At resonance

Off resonance

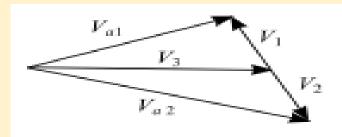
$f_{input} = f_{if}$

- V_3 in phase quadrature with V_1 and V_2 .
- The resultant voltages V_{a1} and V_{a2} are equal in magnitude.



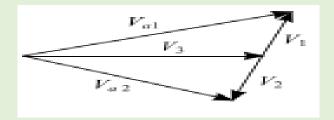
${f}_{input} > {f}_{if}$ by an amount $\frac{{f}_{if}}{2{Q}_{s}}$

- Phase difference between V_3 and V_1 is 45 degrees.
- Since V_2 is in phase opposition with V_1 , phase difference between V_3 and V_2 is 135 degrees.
- The magnitude of V_{a1} is reduced whereas V_{a2} is increased.



$f_{input} < f_{if}$ by an amount $\frac{f_{if}}{2Q_s}$

- Phase difference between V_3 and V_2 is 45 degrees.
- Since V_2 is in phase opposition with V_1 , phase difference between V_3 and V_1 is 135 degrees.
- The magnitude of V_{a1} is increased whereas V_{a2} is decreased.



Foster-Seeley discriminator Contd..

- Thus the amplitude of V_{a1} and V_{a2} will vary with the instantaneous frequency f as shown in figure 1 (a).
- The RF voltage V_{a1} and V_{a2} are separately rectified by the diodes D_1 and D_2 to produce voltages V_{o1} and V_{o2} that represent the amplitude variations of V_{a1} and V_{a2} .
- The output voltage is given by $V_0 = |V_{o2}| |V_{o1}|$.
- The discriminator characteristics is zero at resonance, positive above resonance and negative below resonance.
- It is linear for the region between the peaks of V_{a1} and V_{a2} and this range is the peak separation region which should be more than twice the frequency deviation .

Disadvantage

- Any variation in amplitude of the input FM signal due to noise modifies the discriminator characteristics as shown in figure 2 (b).
- The undesired frequency components corresponding to amplitude variations lead to distorted output.
- Distortions can be reduced by using a limiter in FM receiver.

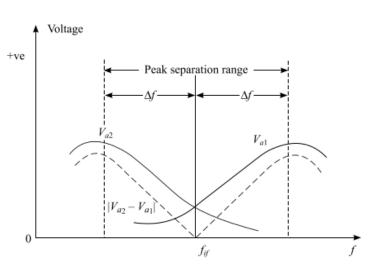


Figure 1 (a): Discriminator Characteristics

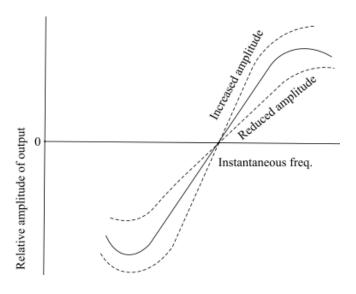


Figure 1 (b): Discriminator Characteristics

- 3) A modulating Signal Scosalis x103t, angle modulates a carrier Acoswet.
 - i) Find the modulation index and the bandwidth for a) the FM system b) the PM system
 - ii) Determine the change on the bandwidth and tre modulation index for both FM and PM of for is reduced to 5KHB. Assume Kp=Kg=15KHB1:

Solution:

- i) Given Em = SV, fm = 15KHB
- a) FM system:

$$mf = \frac{75}{15}$$

DIM System

Frequency deviation
$$\Delta f = KpEm fm$$

$$\Delta f = 1125 \text{ mHz}$$

BM= S (Vittu) = SVt

$$m_p = kp Em = 15 \times 10^3 \times 5$$

$$m_p = 75 \text{ KHg}$$

11) NOW fm = 5 KHg

FOX FM:

$$mf = \frac{\Delta f}{fm} = \frac{75}{5}$$

$$BW = 2(0f + fm) = 2(75 + 5)$$

FM modulation index changes considerably with a charge in the modulating frequency, but the bardwidth charges only slightly.

For pm system:

$$\Delta f = Kp Em fm = 15 \times 10^3 \times 5 \times 5 \times 10^3$$

In PM, the BW charges considerably with charge in Im but mp remains uncharged.

A Semi conductor junction diode is used to modulate the frequency of an oscillator. The junction capacitance is the total tuning capacitance of the oscillator tank Circuit. When a did bias voltage of 15 v is applied to the diode, the oscillator frequency generated is 5 ming. If a single-tone modulating voltage A similation to distortion find a) the percentage search harmonic distortion and b) the frequency modulation index.

solution:

In The polarizing voltage
$$V_0 = 15V$$

$$f_C = 5 \text{ mHg} = \frac{\omega}{\omega_C} = \frac{15V4}{10\pi \cdot 10^6}$$
(Lok) $V_0 = \frac{V_0^{1/4}}{\omega_C} = \frac{15V4}{10\pi \cdot 10^6}$

a) 1. 2nd harronic distortion = 3 Vm x 100

b) modulation index

$$m_f = \frac{Vm}{4 \log (L_0 k V_0^{3/2})^{\frac{1}{2}}} = \frac{Vm}{4 \log (L_0 k)^{\frac{1}{2}} V_0^{\frac{3}{4}}}$$

$$m_f = \frac{4 \times 10 \pi \times 10^6}{4 \times 12560 \times (15)^{\frac{1}{4}} \times (15)^{\frac{1}{4}}}$$