The value of  $\oint_C \frac{z^2}{(z-2)^2} dz$  where C is the circle |z| = 3 is

- a. 0
- b. 2*πi*
- c.  $4\pi i$
- d. 8πi
- O a
- O b
- $\bigcirc$  o
- $\bigcirc$

The zero's of  $f(z) = \frac{z^2+1}{1-z^2}$  are

- a. 0
- b. ±*i*
- c. ±1
- d. 1
- a
- $\bigcirc$  t
- $\bigcap$  c

The annular region for the function  $f(z) = \frac{1}{z^2 - z - 6}$  is

- a. 0 < |z| < 1
- b. 1 < |z| < 2
- c. 2 < |z| < 3
- d. |z| < 3
- $\bigcirc$  b
- $\bigcirc$

The invariant point of the transformation  $w = \frac{1}{z+2i}$  is

- a. z = i
- b. z = -i
- c. z = 1
- d. z = -1
- ( ) t
- $\bigcirc$
- $\bigcirc$

A single valued continuous function f(z) = u + iv is analytic in a region R if it satisfy the C-R equations at each point and also possess one of the following

- a.  $u_x = v_y$
- b.  $v_x = u_y$
- c. continuous $u_x$ ,  $u_y$  in a region R
- d. continuous  $u_x$ ,  $u_y$ ,  $v_x$ ,  $v_y$  at each point of the region R
- ( ) b
- $\bigcirc$  c

If the integral  $\oint_0^{2\pi} \frac{d\theta}{5+3\cos\theta} = \oint_C^{\Box} f(z)dz$ , C is |z| = 1, then

- (A)  $z = -\frac{1}{3}$  lies inside C and
- (B) z = 3 lies outside C. Which of the following is true.
  - a. Both A and B
  - b. Only A
  - c. Only B
  - d. Neither A nor B
- ( ) a
- $\bigcirc$  b
- ( ) d

The bilinear transformation that maps the points  $z = 0,1,\infty$  into the points w = -5, -1,3 respectively is

- a.  $w = \frac{3z-5}{z-1}$
- b.  $w = \frac{3z-5}{z+1}$
- c.  $w = \frac{2z+5}{z+1}$
- d.  $w = \frac{z-5}{z+1}$
- ( ) a
- $\bigcirc$  b

\*

Let z = a is a simple pole for f(z) and  $b = \lim_{z \to a} (z - a) f(z)$ , then

- a. b is a simple pole
- b. b is removable singularity
- c. b is a residue at a of order n
- d. b is a residue at z = a
- ( ) a
- 0
- C

!

Find an analytic function f(z) whose real part is  $u = e^x \sin y$ 

- a.  $e^z + c$
- $b. e^z + c$
- c.  $-(1+i)e^z + c$
- $d. -ie^z + c$
- $\bigcirc$  b
- $\bigcirc$

Under the mapping  $w = \frac{1}{z}$ , the image of  $|z| \le 1$  is

- a.  $|w| \ge 1$
- b. |w| = 1
- c.|w| > 1
- d. |w 1| = 1
- 6
- ( ) b
- $\bigcirc$

If  $f(z) = \frac{-1}{(z-1)} - 2[1 + (z-1) + (z-1)^2 + ...]$  then the residue of f(z) at z = 1 is

- a. 1
- b. -1
- c. 0
- d. -2
- ( ) t

If 
$$w = z + \frac{1}{z}$$
 then  $\frac{dw}{dz}$  is

- $a.1 + \frac{1}{z^2}$
- b.  $1 \frac{1}{z^2}$
- c.  $1 + \frac{1}{z}$
- d.  $1 \frac{1}{z}$
- ( ) a
- ( t

The mapping w = z + c gives

- a. Translation
- b. Rotation
- c. inversion
- d. reflection
- ( a
- ( ) t
- $\bigcirc$
- $\bigcap$

The value of  $\oint_C \frac{e^{-z}}{z+1} dz$  where C is the circle  $|z| = \frac{1}{3} is$ 

- a. 0
- b.  $2\pi ie$
- c.  $\frac{\pi}{2}ie$
- d. πie
- ( a
- ( ) t
- $\bigcirc$
- $\bigcirc$  c

The Laurent's series expansion  $-\frac{1}{2}\sum \frac{(z+2)^n}{4^n} - \sum \frac{3^n}{(z+2)^n}$  for the function

 $f(z) = \frac{z}{(z-1)(z-2)}$  is valid in the region

- a. |z+2| < 3
- b. 1 < |z + 2| < 2
- c. 3 < |z+2| < 4
- d. |z+2| > 4
- ( b
- $\bigcirc$  d

\*

Let  $C_1: |z-a| = R_1$  and  $C_2: |z-a| = R_2$  be two concentric circles  $(R_2 < R_1)$ , the annular region is defined as

- a. Within  $C_1$
- b. Within  $C_2$
- c. Within  $C_2$  and outside  $C_1$
- d. Within  $C_1$  and outside  $C_2$
- ( ) a
- ( ) b
- $\bigcirc$

If f(z) is analytic inside and on C, then the value of  $\oint_C \frac{f(z)}{(z-a)^5} dz$ , where C is the simple closed curve and a is any point within C is

- a.  $2\pi i \frac{f^{v}(a)}{5!}$
- b.  $2\pi i f(a)$
- c.  $2\pi i \frac{f^{iv}(a)}{4!}$
- d. 0
- ( b
- $\bigcirc$

The region in which  $f(z) = (x - y)^2 + 2i(x + y)$  is analytic

- a. x + y = 1
- b. x = 1
- c. x y = 1
- d. y = 1
- ( ) a
- $\bigcirc$  b
- 0
- $\bigcirc$  d

\*

Let C: |z - a| = r be a circle, the f(z) can be expanded as a Taylor's series if

- a. f(z) is a function on C
- b. f(z) is an analytic function within C
- c. f(z) is not an analytic function within C
- d. f(z) is an analytic function outside C
- ( ) t
- $\bigcirc$

The value of the integral  $\oint_C e^z dz$  where |z| = 1 is

- a.  $2\pi i$
- b.  $\frac{\pi}{2}i$
- c. *πi*
- d. 0
- ( ) a
- $\bigcirc$  b

 $\nabla^2 \{ \log |f(z)| \} =$ 

- a. 2
- b.0
- c. 1
- d. 3
- ( ) a
- $\bigcirc$  b
- O 0

The value of  $\oint_C \frac{e^{2z}}{(z+1)^3} dz$  where C is the circle |z| = 2 is

- a. 0
- b.  $2\pi i e^{-2}$
- c. 8πie<sup>-2</sup>
- d.  $4\pi i e^{-2}$
- ( ) b

If f(z) is not analytic at  $z = z_0$  and there exists  $\lim_{z \to z_0} f(z)$  and is finite then

- a. The point  $z = z_0$  is isolated singularity of f(z)
- b. The point  $z = z_0$  is a removable singularity of f(z)
- c. The point  $z = z_0$  is essential singularity of f(z)
- d. The point  $z = z_0$  is non isolated singularity of f(z)
- ( a
- $\bigcirc$  t

Critical point of the map  $w^2 = (z - \alpha)(z - \beta)$  are

a. 
$$z = \frac{1}{2}(\alpha + \beta)$$

b. 
$$z = \frac{\alpha\beta}{2}$$

c. 
$$z = (\alpha + \beta)$$

d. 
$$z = \frac{1}{2}(\alpha - \beta)$$

- ( ) a
- ( ) b
- $\bigcirc$

If  $\oint_C \frac{e^z}{z^2} dz = 0$ , then C is

- a. |z| = 1
- b. |z 1| = 2
- c. |z 2| = 1
- d. |z| = 2
- ( ) a
- ( ) b
- O 0
- $\bigcirc$

The invariant points of the transformation  $w = \frac{2z-5}{z+4}$  are

- a.  $z = \pm i$
- b.  $-1 \pm 2i$
- c.  $1 \pm 2i$
- d.  $-1 \pm i$
- ( b
- $\bigcirc$
- $\bigcirc$  c

Let z = a is a pole of order m for f(z), then the residue is

- a.  $\lim_{z \to a} [(z a)f(z)]$
- b.  $\lim_{z \to a} [(z a)f''(z)]$
- c.  $\lim_{z \to a} \frac{1}{(m-1)!} \frac{d^{m-1}}{dz^{m-1}} [(z a)^m f(z)]$
- d.  $\lim_{z \to a} \frac{1}{m!} \frac{d^m}{dz^m} [(z-a)^m f(z)]$
- O a
- ( ) b

The points at which the function  $f(z) = \frac{1}{1+z^2}$  fails to be analytic are

a. 
$$z = \pm 1$$

b. 
$$z = \pm i$$

c. 
$$z = \pm 2$$

d. 
$$z = 1$$

- ( ) a
- ( l
- $\bigcirc$
- $\bigcirc$

The value of  $\oint_C \frac{1}{2z-3} dz$  where C is the circle |z| = 1 is

- a. 0
- b.  $2\pi i$
- c.  $\frac{\pi}{2}i$
- d. *πi*
- ( ) a
- $\bigcirc$  b
- $\bigcirc$  c

Find the analytic function f(z) where  $v = x^4 - 6x^2y^2 + y^4$ 

- a.  $iz^4 + c$
- b.  $iz^3 + c$
- $c. -iz^4 + c$
- $d. -iz^3 + c$
- ( ) a
- ( ) b
- $\bigcirc$  c

If u(x, y) is a real part of analytic function and satisfies  $u_{xx} + u_{yy} = 0$ , then u is

- a. Harmonic
- b. Analytic
- c. Differentiable
- d. continuous
- •
- ( t
- $\bigcirc$  c
- $\bigcirc$  d

\*

The residue of  $f(z) = \frac{z}{z^2 + 1}$  at z = i is

- a. 1
- b. -1
- c. 0
- d. 1/2
- a
- ( ) b
- C

!

Expansion of  $\frac{\sin z}{(z-\pi)}$  in Taylor's series about  $z=\pi$  is

a. 
$$\frac{(z-\pi)}{1!} - \frac{(z-\pi)^3}{3!} + \frac{(z-\pi)^5}{5!} - \dots$$

b. 
$$\frac{(z-\pi)^2}{2!} - \frac{(z-\pi)^4}{4!} + \frac{(z-\pi)^6}{6!} - \dots$$

c. 
$$-1 + \frac{(z-\pi)^2}{3!} - \frac{(z-\pi)^4}{5!} + \dots$$

d. 
$$\frac{(z-\pi)}{2!} + \frac{(z-\pi)^3}{4!} - \frac{(z-\pi)^5}{6!} + \dots$$

- ( ) a
- ( ) b
- 0 0
- $\bigcirc$  c

The critical points of the transformation  $w = \frac{1}{2} \left( z + \frac{1}{z} \right)$ 

- a.  $z = \pm 1$
- b.  $z = \pm i$
- c.  $z = \pm 2$
- d. z = 1
- ( ) a
- ( ) b
- $\bigcirc$  c
- $\bigcirc$  c

In Cauchy's Lemma for contour integration, if f(z) be continuous function such that  $|zf(z)| \to 0$  as  $|z| \to \infty$ , for C is the circle |z| = R, then

- a.  $\oint_C f(z)dz \to \infty$  as  $R \to \infty$ .
- b.  $\oint_C f(z)dz \to 0 \text{ as } R \to \infty.$ c.  $\oint_C f(z)dz \to 0 \text{ as } R \to 0.$ d.  $\oint_C f(z)dz \to \infty \text{ as } R \to 0.$

If u + iv is analytic then v - iu is

- a. analytic
- b. not analytic
- c. analytic only at the origin
- d. analytic expect at the origin
- ( ) a
- ( ) b
- O c
- $\bigcirc$  c

If f(z) = u + iv is analytic at a point then which of the following is not true?

- a.  $u_x = v_y$  at the point
- b.  $u_y = -v_x$  at the point
- c.  $u_{xx} + u_{yy} \neq 0$  at the point
- d.  $u_x$ ,  $u_y$ ,  $v_x$ ,  $v_y$  are continuous at the point
- ( ) b

If f(z) = u + iv is an analytic function of z then the Cauchy Riemann equations is

- a.  $u_x = v_{y, u_y} = v_x$
- b.  $u_x = v_{y}, u_y = -v_x$
- c.  $u_x = -v_{y}, u_y = -v_x$
- d.  $u_x = -v_{y_x} u_y = v_x$
- b
- $\bigcirc$

If f(z) is analytic inside and on C, then the value of  $\oint_C \frac{f(z)}{z-a} dz$ , where C is the simple closed curve and a is any point within C is

- a. f(a)
- b.  $2\pi i f(a)$
- c.  $\pi i f(a)$
- d. 0
- ( ) a
- ( ) b
- $\bigcirc$

The bilinear transformation which maps the points  $\infty$ , i, 0 into 0, i,  $\infty$  respectively is

- a. w = z
- b. w = -z
- c.  $w = -\frac{1}{z}$
- d.  $w = \frac{1}{z}$
- ( a
- ( ) b
- 0
- $\bigcirc$

If  $f(z) = r^2(\cos 2\theta + i\sin p\theta)$  is analytic, then the value of p is

- a.  $\frac{1}{2}$
- b. 0
- c. 2
- d. 1
- ( ) b
- C

 $f(z) = |z|^2$  is analytic at

- a. at the origin
- b. at infinity
- c. at all points of z-plane
- d. nowhere
- ( ) a
- $\bigcirc$  t
- $\bigcirc$  c

w = log z is

- a. analytic at all points
- b. not analytic at the origin
- c. nowhere analytic
- d. analytic at infinity
- ( ) t
- $\bigcirc$

Construction of an analytic functions f(z) when real part is given using Milne's Thomson method  $u_x = \phi_1(x, y)$ ,  $u_y = \phi_2(x, y)$ ,

$$v_x = \Psi_2(x, y), v_y = \Psi_1(x, y)$$

a. 
$$f(z) = \int [\phi_1(z, 0) - i\phi_2(z, 0)]dz + c$$

b. 
$$f(z) = \int [\phi_1(z, 0) + i\phi_2(z, 0)]dz + c$$

c. 
$$f(z) = \int [\Psi_1(z, 0) + i\Psi_2(z, 0)]dz + c$$

d. 
$$f(z) = \int [\Psi_1(z, 0) - i\Psi_2(z, 0)]dz + c$$

- ( ) b

The residue of  $f(z) = \frac{z}{(z-1)^2}$  at z = 1 is

- a.  $\pi$
- b. 1
- c. -1
- d. 0
- ( b
- $\bigcirc$  c

The part  $\sum_{n=1}^{\infty} b_n (z-a)^{-n}$  consisting of negative integral powers of (z-a) is called as

- a. The analytic part of the Laurent's series
- b. The principal part of the Laurent's series
- c. The real part of the Laurent's series
- d. The imaginary part of the Laurent's series
- ( ) k
- $\bigcirc$
- $\bigcap$

If  $f(z) = \frac{\sin z}{z}$ , then

- a. z = 0 is a simple pole
- b. z = 0 is a pole of order 2
- c. z = 0 is a removable singularity
- d. z = 0 is a zero of f(z)
- ( ) a
- $\bigcirc$  b
- $\bigcap$

If f(z) is analytic with the real part  $e^x \cos y$  then f'(z) is equal to

- a. cosz
- $b. e^z$
- c.  $e^z$
- d. sinz
- ( ) a
- $\bigcirc$  b
- $\bigcirc$  c

\*
A continuous curve which does not have a point of self-intersection is called
a. Curve
b. Closed curve
c. Simple closed curve
d. Multiple curve

a

b

c

d

Page 2 of 2

Back

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