

Unit - I

1) A vector A is represented by components (A_x, A_y, A_z) , (A_r, A_ϕ, A_z) and (A_r, A_θ, A_ϕ) in three co-ordinate systems. If $A_x = A_y = A_z = 1$ and $\theta = \phi = 45^\circ$ the radial component of the vector A in spherical co-ordinate and cylindrical co-ordinates are related as

- a) less than cylindrical
- b) greater than cylindrical
- c) equal to cylindrical
- d) not related to cylindrical

2) The vector transformation between cylindrical and spherical co-ordinates is given as,

$$a) \begin{bmatrix} A_r \\ A_\theta \\ A_\phi \end{bmatrix} = \begin{bmatrix} \sin\theta & 0 & \cos\theta \\ \cos\theta & 0 & -\sin\theta \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} A_\rho \\ A_\phi \\ A_z \end{bmatrix}$$

$$b) \begin{bmatrix} A_r \\ A_\theta \\ A_\phi \end{bmatrix} = \begin{bmatrix} \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \\ \cos\theta & -\sin\theta & 0 \end{bmatrix} \begin{bmatrix} A_\rho \\ A_\phi \\ A_z \end{bmatrix}$$

$$c) \begin{bmatrix} A_r \\ A_\theta \\ A_\phi \end{bmatrix} = \begin{bmatrix} \sin\phi & \cos\phi & 0 \\ 0 & 0 & 1 \\ \cos\phi & -\sin\phi & 0 \end{bmatrix} \begin{bmatrix} A_\rho \\ A_\phi \\ A_z \end{bmatrix}$$

$$d) \begin{bmatrix} A_r \\ A_\theta \\ A_\phi \end{bmatrix} = \begin{bmatrix} \sin\phi & 0 & \cos\phi \\ \cos\phi & 0 & -\sin\phi \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} A_\rho \\ A_\phi \\ A_z \end{bmatrix}$$

3) The vectors $C = (3\vec{e}_x + \vec{e}_y + \sqrt{2}\vec{e}_z)$ and $D = 6\sqrt{2}\vec{e}_x + 4\sqrt{2}\vec{e}_y$ are.

- a) parallel
- b) perpendicular
- c) at an angle 42°
- d) unrelated.

4) The force F_1 , on the charge Q_1 , due to second charge Q_2 is given by,

a) $F_1 = \frac{Q_1 Q_2}{4\pi\epsilon_0 R_{21}^3} \vec{r}_{21}$

b) $F_1 = \frac{Q_1 Q_2}{4\pi\epsilon_0 R_{21}^3} \cdot \vec{R}_{21}$

c) $F_1 = \frac{Q_1 Q_2}{2\pi\epsilon_0 R_{21}^3} \vec{r}_{21}$

d) $F_1 = \frac{Q_1 Q_2}{2\pi\epsilon_0 R_{21}^3} \cdot \vec{R}_{21}$

5) The electric field intensity, $\vec{E} = -\text{grad}(V)$, along the direction of ϕ in spherical co-ordinates is given by,

a) $E_\phi = \frac{2p}{2\pi\epsilon_0 r^3} \sin\theta$

b) $E_\phi = \frac{2p}{4\pi\epsilon_0 r^3} \cos\theta$

c) $E_\phi = 0$

d) $E_\phi = 1$

6) The electric field intensity, E between two infinite sheets of charge with density ρ_s located at $x = \pm 1$ respectively is

a) $\vec{E} = \frac{1}{2\epsilon_0} \vec{a}_n$

b) $\vec{E} = \frac{-1}{2\epsilon_0} \vec{a}_n$

c) $\vec{E} = 0$

d) $\vec{E} = -\frac{\rho_s}{\epsilon_0} \vec{a}_x$

7) Gauss's law for electrostatics can be mathematically represented as

a) $\vec{D} \cdot d\vec{S} = Q_{enc}$

b) $\int \psi \cdot d\vec{S} = Q_{enc}$

c) $\psi = Q_{enc}$

d) $\vec{D} = Q_{enc}$

8) The electric field E is _____ to the electric equipotential lines

a) normal

c) opposite

b) tangential

d) unrelated

9) The electric flux density D is _____ to the electric flux lines

a) normal

c) opposite

b) tangential

d) unrelated

10) When a potential difference is applied to human heart, its behaviour can be modelled as that of electric dipole. Abnormal hearts can be detected by mapping:

- a) equipotential surfaces
- b) electric flux lines
- c) electric fields
- d) all of the above

11) A Gaussian surface within a metallic spherical shell of inner and outer radii R_1 and R_2 contains charge Q placed at the center. The normal component of \vec{D} at the Gaussian surface will be

- a) zero
- b) $\frac{Q}{4\pi R_1^2}$
- c) $\frac{Q}{4\pi R_2^2}$
- d) $\frac{Q}{4\pi (R_1 - R_2)^2}$

12) Two concentric hollow spheres of radii R_1 and R_2 ($R_1 > R_2$) have respective charges Q_1 & Q_2 distributed uniformly over their surfaces. The electric flux density \vec{D} at a Gaussian surface of radius ' r ' such that ($R_1 > r > R_2$) will be

- a) $\frac{Q_1}{4\pi R_1^2}$
- b) $\frac{Q_1}{4\pi r^2}$
- c) $\frac{Q_2}{4\pi R_2^2}$
- d) $\frac{Q_2}{4\pi r^2}$

13) Usually a collection of positive charges is considered for constructing a Gaussian surface. If a Gaussian surface encloses a collection of negative charges, then for such a surface

(5)

- a) the normal component of D will become zero
- b) the normal component of D will point inwards
- c) the normal component of D will point outwards
- d) the normal component of D will become infinity

4) The divergence of a vector in spherical co-ordinates is given by,

$$\nabla \cdot \vec{A} = \frac{1}{r^2} \frac{\partial(r^2 A_r)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial(A_\theta \sin \theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial A_\phi}{\partial \phi}$$

The operator ∇ is given by,

$$a) \frac{1}{r^2} \frac{\partial(r^2)}{\partial r} + \frac{1}{r \sin \theta} \frac{\partial(\sin \theta)}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi}$$

$$b) \frac{1}{r^2} \frac{\partial(r^2)}{\partial r} \vec{a}_r + \frac{1}{r \sin \theta} \frac{\partial(\sin \theta)}{\partial \theta} \vec{a}_\theta + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} \vec{a}_\phi$$

$$c) \frac{\partial}{\partial r} + \frac{1}{r} \frac{\partial}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi}$$

$$d) \frac{\partial}{\partial r} \vec{a}_r + \frac{1}{r} \frac{\partial}{\partial \theta} \vec{a}_\theta + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} \vec{a}_\phi$$

15) The potential gradient in cylindrical co-ordinate system is given by,

a) $\frac{\partial V}{\partial r} + \frac{\partial V}{r \partial \phi} + \frac{\partial V}{\partial z}$

b) $\frac{\partial V}{\partial r} \vec{a}_r + \frac{\partial V}{r \partial \phi} \vec{a}_\phi + \frac{\partial V}{\partial z} \vec{a}_z$

c) $\frac{1}{r} \frac{\partial V}{\partial r} \vec{a}_r + \frac{1}{r} \frac{\partial V}{\partial \phi} \vec{a}_\phi + \frac{1}{r} \frac{\partial V}{\partial z} \vec{a}_z$

d) $\frac{1}{r \partial \phi} \cdot \frac{\partial V}{\partial r} \vec{a}_r + \frac{1}{r} \frac{\partial V}{\partial \phi} \vec{a}_\phi + \frac{1}{r \partial \phi} \frac{\partial V}{\partial z} \vec{a}_z$

16) The relationship between electric field intensity, E and potential V is given by,

a) $\vec{E} = -\nabla V$

b) $V = -\nabla \cdot \vec{E}$

c) $V = -\nabla \times \vec{E}$

d) $\vec{E} = \nabla V$

17) In an electric circuit, the energy store in the field of a capacitor is given by,

a) $W_E = \frac{1}{2} CV^3$

b) $W_E = \frac{1}{2} CV^2$

c) $W_E = \frac{1}{4} CV^2$

d) $W_E = \frac{1}{3} CV^2$

(18) The potential V due to a point charge (7) is given by,

a) $V = \frac{Q_1 Q_2}{4\pi \epsilon_0 r^2}$

b) $V = \frac{Q_1 Q_2}{2\pi \epsilon_0 r^2}$

c) $V = \frac{Q}{4\pi \epsilon_0 r}$

d) $V = \frac{Q_1 Q_2}{2\pi \epsilon_0 r}$

(19) The relation between the electric flux density \vec{D} and electric field intensity, \vec{E} is given by,

a) $\vec{E} = \epsilon \vec{D}$

b) $\vec{E} = \frac{\vec{D}}{\epsilon}$

c) $\vec{E} = \frac{\vec{D}}{\rho \epsilon}$

d) $\vec{E} = \frac{\rho \vec{D}}{\epsilon}$

(20) The dielectric dipole moment 'P', of charge Q and distance 'd' is given by,

a) $P = Qd$

b) $d = QP$

c) $Q = P \cdot d$

d) $Q = P \cdot d^2$