

SRM INSTITUTE OF SCIENCE AND TECHNOLOGY

DEPARTMENT OF MATHEMATICS

18MAB201T/Transforms and Boundary value problems

UNIT III - APPLICATIONS OF PARTIAL DIFFERENTIAL EQUATIONS

TUTORIAL SHEET -1

PART-B QUESTIONS

1. Classify the equation $x^2 f_{xx} + (1 - y^2) f_{yy} = 0$.
2. Classify the equation $(1 + x^2) f_{xx} + (5 + 2x^2) f_{xy} + (4 + x^2) f_{yy} = 2 \sin(x + y)$.
3. Classify the equation $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = f(x, y)$.
4. Write down the assumptions made in deriving one-dimensional wave equations.

PART-C QUESTIONS

4. A tightly stretched string with fixed end points $x = 0$ and $x = l$ is initially in a position given by $y(x, 0) = y_0 \sin\left(\frac{\pi x}{l}\right)$. If it is released from rest from this position, find the displacement y at any time and at any distance from the end $x = 0$.
5. An elastic string is stretched between two fixed points at a distance π apart. In its initial position the string is in the shape of the curve $f(x) = k(\sin x - \sin^3 x)$. Obtain $y(x, t)$ the vertical displacement if y satisfies the equation $\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 y}{\partial x^2}$.
6. Find the solution of the wave equation $\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 y}{\partial x^2}$, corresponding to the triangular initial

$$\text{deflection } f(x) = \begin{cases} \frac{2kx}{l}, 0 < x < \frac{l}{2} \\ \frac{2k}{l}(l - x), \frac{l}{2} < x < l \end{cases} \quad \text{and the initial velocity is zero.}$$