Shi-Tomashi

filip.reichl, tomas.adam, lucia.szalonova, roman.varga

December 2019

1 Pseudocode

Taylor Series:
$$T(x,y) \approx f(u,v) + (x-u)f_x(u,v) + (y-v) f_y(u,v) + ...$$

Rewriting the shifted intesity using the above formula:

$$I(x+u, y+v) \approx I(x,y) + \partial I_{(x,y)} / \partial_x \quad u + \partial I_{(x,y)} / \partial_y \quad v$$

Let:
$$\partial I_{(x,y)}/\partial x = I_x$$
 and $\partial I_{(x,y)}/\partial y = I_y$

i.e. I_x and I_y are image derivatives in the X and Y directions respectively.

then

$$\mathbf{E}(\mathbf{u},\!\mathbf{v}) = \boldsymbol{\Sigma}\; \boldsymbol{\omega}(x,y)\; [I(x,y) \! + \! \mathbf{I}_x\; \mathbf{u} \, + \, I_y\; \mathbf{v}$$
 - $\mathbf{I}(\mathbf{x},\!\mathbf{y})]^2$

$$E(\mathbf{u}, \mathbf{v}) = \Sigma \,\omega(x, y) \,[\mathbf{I}_x \mathbf{u} + I_y \mathbf{v}]^2$$

Expanding,
$$E(u,v) = \sum \omega(x,y) [I_x^2 u^2 + I_y^2 * v^2 + 2 I_x I_y u v]$$

Taking u,v out and re-write in Matrix notation give us:

$$E(u,v) \approx (u,v)M(xy)$$

Here,
$$M = \omega(x, y) * \begin{pmatrix} \sum I_x^2 & \sum I_x I_y \\ \sum I_x I_y & \sum I_y^2 \end{pmatrix}$$

$$R = min(\lambda 1, \lambda 2)$$

$$\det M = \lambda 1 \lambda 2$$

trace M =
$$\lambda 1 + \lambda 2$$