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MAJOR PROJECT-1 PROGRESS REPORT

**Implementation of Graphical Neural Network (GNN) on
Benchmark Dataset**

Submitted in partial fulfillment of the requirement for the award of the degree of

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Under the guidance of

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Declaration

This is to certify that the Major project-1 report titled “**Implementation of Graphical Neural Network (GNN) on Benchmark Dataset**” which is submitted by me in partial fulfillment of the requirement for the award of degree M.Tech. in Computer Science to USICT, GGSIP University, Dwarka, Delhi, comprises only my original work, and due acknowledgment has been made in the text to all other material used.

Date:

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Certificate

This is to certify that the Major project-1 report entitled **“Implementation of Graphical Neural Network (GNN) on Benchmark Dataset”** submitted by Sashwat Ranjan Shukla in partial fulfillment of the requirement for the award of the degree M.Tech CSE at USICT, GGSIP University, Dwarka, Delhi, is to the best of my knowledge, a record of the candidate’s own work conducted under my supervision.

Date:

Supervisor

Prof. C S Rai

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1. Abstract

We explore the implementation and performance of Graph Neural Networks (GNNs) on well-established benchmark datasets traditionally used for image classification tasks, such as MNIST, Fashion MNIST, CIFAR-10, and CIFAR-100. While these datasets are commonly addressed using Convolutional Neural Networks (CNNs), we propose to treat images as graph structures, where pixels or regions are represented as nodes, and relationships between them form the edges. By transforming the image data into graph representations, we aim to assess the effectiveness of GNN architectures in handling spatial and structural information inherent in visual data.

We compare the performance of various GNN models, such as Graph Convolutional Networks (GCNs), Graph Attention Networks (GATs), with traditional CNN-based models to evaluate their accuracy, computational efficiency, and robustness. Additionally, we experiment with different strategies for constructing the graph structure from image data, such as using superpixels, grid-based representations, and feature maps from pre-trained CNNs.

Our results suggest that GNNs offer a promising way to capture long-range dependencies and contextual relationships within images, something that traditional models may overlook. By examining the balance between computational complexity and accuracy, we provide practical insights into when and where GNNs can be most effective for image classification tasks. Through our experiments, we also report the accuracy and loss metrics across the benchmark datasets, showing how GNNs perform compared to traditional models. This research opens up new opportunities for applying GNNs in fields where understanding the structural properties of data is key to achieving better performance.

2. Introduction

Convolutional Neural Networks (CNNs) have been the backbone of image classification tasks for years, excelling in popular benchmarks like MNIST, Fashion MNIST, CIFAR-10, and CIFAR-100. Their strength lies in their ability to detect local patterns, helping them recognize objects and features in images. However, one limitation of CNNs is that they often miss out on capturing long-range dependencies and more complex relationships across different regions of an image.[1]

Graph Neural Networks (GNNs) offer a fresh perspective. Unlike CNNs, which focus on local patterns, GNNs are designed to capture complex connections by representing data as graphs, where nodes represent elements (like pixels) and edges represent relationships between them. While GNNs have been widely used in fields like social networks and molecular biology, they haven't been explored much in image classification tasks.[2]

In this study, we aim to see how GNNs can be applied to well-known image benchmarks. By transforming images into graph representations—treating pixels or regions as nodes—we explore whether GNNs can better capture the long-range dependencies and relationships that CNNs might miss.[3] We experiment with different GNN models, including Graph Convolutional Networks (GCNs), Graph Attention Networks (GATs), comparing their performance to CNNs.

Beyond simply testing their accuracy, we also look at the loss and overall performance of each approach. Our goal is to offer new insights into how GNNs can be used for image classification, shedding light on when and why GNNs might provide an advantage, especially when understanding the structure within data is critical for better results.

3. What is a Graph Neural Network?

The concept of GNN was first proposed by Gori in 2005 and Scarselli in [2004, 2009]. For simplicity, Scarselli in 2009 proposed a model, which aims to extend existing neural networks for processing graph-structured data.[4]

A Graphical Neural Network (GNN) is a specialized type of neural network designed to process and learn from graph-structured data. In contrast to traditional neural networks that operate on grid-like data, GNNs are tailored to handle data represented as nodes interconnected by edges, such as social networks, citation networks, and molecular structures.[5]

Graph Neural Networks (GNNs) are a powerful class of neural networks designed to operate on graph-structured data, enabling the modeling of complex relationships and interactions. By learning representations of nodes and edges in a graph, GNNs can capture both local and global structural information, making them suitable for a wide range of tasks across various domains. With applications ranging from social network analysis to drug discovery and recommendation systems, [1]GNNs have emerged as a versatile tool for solving real-world problems involving interconnected data. GNNs have gained popularity due to their effectiveness in tasks involving structured data such as social networks, molecular graphs, recommendation systems, and more. In GNNs, each node in a graph represents an entity, and the edges between nodes represent relationships or connections between those entities. The goal of a GNN is to learn representations of nodes that capture both the node's own features and the features of its neighboring nodes in the graph.[4]

Graph Neural Networks are recurrent networks with vector-valued nodes h_i whose states are iteratively updated by trainable nonlinear functions that depend on the states of neighbor nodes $h_j : j \in N_i$ on a specified graph. The form of these functions is canonical, i.e., shared by all graph edges, but the function can also depend on the properties of each edge.[5] The function is parameterized by a neural network whose weights are shared across all edges. Eventually, the states of the nodes are interpreted by another trainable ‘readout’ network. Once trained, the entire GNN can be reused on different graphs without alteration, simply by running it on a different graph with different inputs. Our work builds on a specific type of GNN, the Gated Graph Neural Networks (GG-NNs), which adds a Gated Recurrent Unit (GRU) at each node to integrate incoming information with past states.

The versatility of GNNs is reflected in their wide-ranging applications across diverse domains. In social network analysis, GNNs facilitate community detection, influence prediction, and anomaly detection by uncovering hidden patterns and structures within the network.[6] In recommendation systems, GNNs leverage the graph structure of user-item interactions to deliver personalized recommendations, enhancing user satisfaction and engagement.

The landscape of GNN research is continuously evolving, with researchers developing increasingly sophisticated architectures and algorithms to tackle new challenges and domains. Graph Convolutional Networks (GCNs), Graph Attention Networks (GATs), are just a few examples of the diverse array of GNN architectures that have demonstrated remarkable performance across various applications.[7] As our understanding of GNNs deepens and their capabilities expand, they promise to revolutionize how we analyze, interpret, and extract insights from graph-structured data, driving innovation and discovery across countless fields.

Graph Convolutional Networks (GCNs): GCNs are one of the earliest and most popular architectures for GNNs. They extend convolutional neural networks (CNNs) to graph-structured data by performing message-passing operations, where each node aggregates

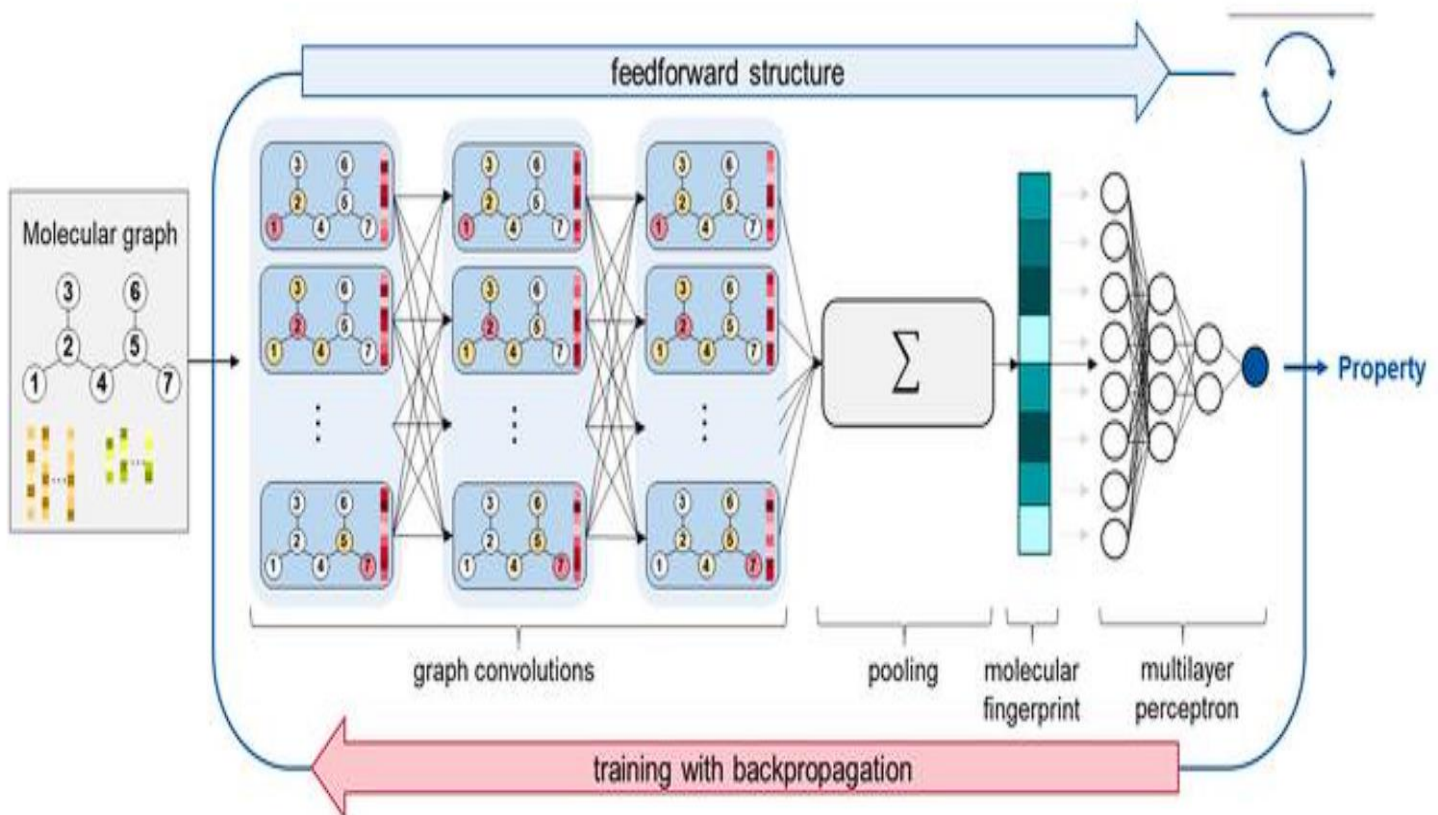


Figure 1: Data Flow diagram of GNN[2]

information from its neighbors. This aggregation process is typically performed through graph convolutional layers. Graph Convolutional Networks (GCNs) are a class of neural networks designed specifically to operate on graph-structured data. Unlike traditional neural networks that work well with grid-like data such as images, GCNs excel at tasks involving relational data represented as graphs. In a graph, nodes represent entities, and edges represent relationships between them.[8][9]

One of the key advantages of GCNs is their ability to learn from both the node features and the graph structure itself. By leveraging information from neighboring nodes, GCNs can generate meaningful representations for each node in the graph, enabling tasks such as node classification, link prediction, and graph classification.

4. Steps to Make a Graph in Graph Neural Network.

1. Image to Graph Representation

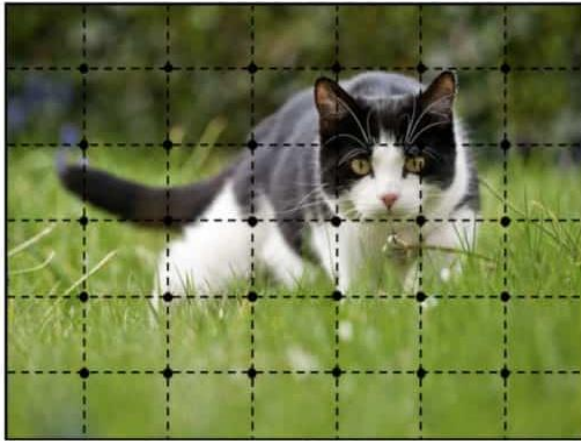
The first step is converting image data into a graph structure, where each node corresponds to a part of the image (such as a pixel, superpixel, or feature), and edges represent relationships between those nodes.[10][6]

Node Definition

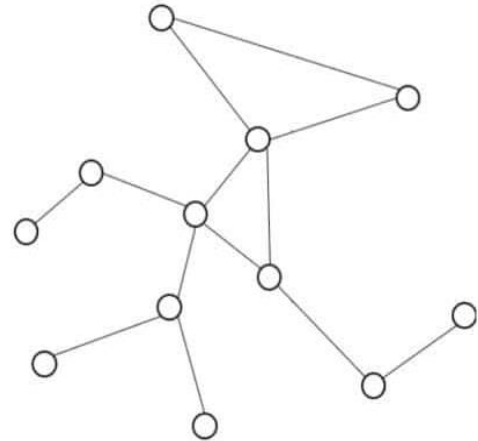
- **Pixels as Nodes:** Each pixel in the image can be considered a node. This approach works for small images like MNIST or CIFAR-10 where each pixel can be treated as a distinct node.
- **Superpixels as Nodes:** For larger images (like CIFAR-10 or CIFAR-100), superpixels offer a good trade-off. Superpixels are created by grouping adjacent pixels with similar colors or textures, which reduces the node count and computation. Common algorithms for superpixel segmentation include SLIC (Simple Linear Iterative Clustering) and Felzenszwalb's algorithm.

Assign Node Features: Each node needs a feature vector to describe it, which could be:

- **Pixel Intensity or RGB Values:** For pixel-based graphs, features can be grayscale intensity or RGB values. For example, an RGB image node might have a feature vector $[R, G, B]$.
- **Extracted Features:** For complex tasks, features can be extracted from a pre-trained CNN model like ResNet or VGG. This results in rich, high-dimensional feature embeddings for each node, capturing more nuanced patterns in the image.



An Image



A graph

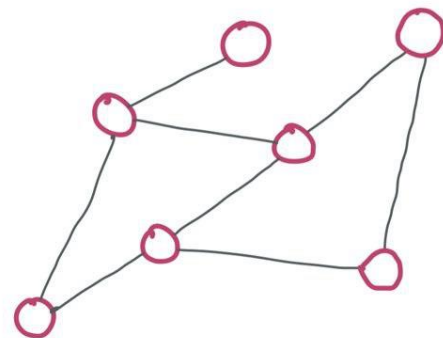
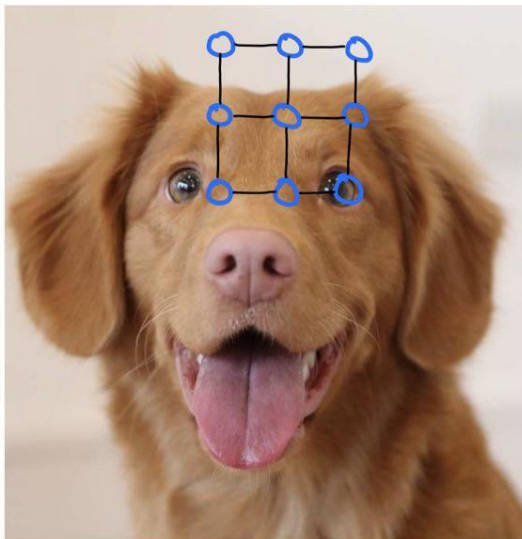


Figure 2: Graph Representation of Cat and Dog[11]

Edge Definition

- **Adjacency Based on Distance:** Nodes (pixels or superpixels) can be connected if they are spatially close to each other. For example, you can connect a node to its immediate neighbors using a fixed grid structure (e.g., 4-nearest or 8-nearest neighbors).
- **Feature Similarity:** Another approach is to connect nodes based on the similarity of their features (color, intensity, texture, etc.). Nodes that have similar properties can have higher edge weights.[12]

- **Edge Weighting:** Assign weights to edges based on the spatial distance between nodes or similarity of features. Closer or more similar nodes have stronger (higher-weighted) edges, reflecting the likelihood of a shared class or label in image regions.

Graph Construction

- Build an adjacency matrix representing the edges (connections) between nodes. The adjacency matrix can be binary (connected or not) or weighted based on the distance or similarity between nodes.
- Optionally, you can create a **feature matrix** for the nodes, where each node has attributes such as pixel intensity, color values, or features extracted by pre-trained CNNs.

2. Build the Adjacency Matrix

The adjacency matrix A represents the structure of the graph and captures node connectivity. This matrix has dimensions $N \times N$, where N is the number of nodes, and each entry $A[i][j]$ indicates if there's an edge between nodes i and j :

- **Binary Representation:** $A[i][j] = 1$ if nodes i and j are connected and 0 otherwise. This approach works for unweighted graphs.
- **Weighted Representation:** For weighted graphs, $A[i][j]$ is the weight of the edge, reflecting distance or similarity between nodes. Higher weights indicate closer proximity or greater similarity.
- **Add Self-Loops:** To include each node's own features during graph convolutions, a self-loop is added to each node. This is done by adding an identity matrix I to the adjacency matrix, resulting in $A' = A + I$.

3. Train the GNN Model

- **Loss Function:** Use a loss function like cross-entropy for classification. This loss function will compare the predicted class probabilities with the true labels.
- **Optimization:** Use backpropagation to optimize the GNN's parameters. Common optimizers include Adam and SGD.[9][12]
- **Evaluation:** After training, evaluate the model's performance using standard metrics like accuracy, precision, recall, and F1-score on a test dataset.

4. Classification with the GNN

After the graph convolutional layers, use a **readout** or **pooling layer** to aggregate node features into a single global feature vector for the entire image. There are several ways to perform pooling:

- **Global Average Pooling:** Take the average of all node features to get a single feature vector representing the whole graph.
- **Global Max Pooling:** Take the maximum feature value across nodes.
- **Learned Pooling:** Use an additional GNN layer to learn which nodes contain important information.

5. Benchmark dataset

Benchmark datasets serve as standardized sets of data used to evaluate the performance of machine learning models, particularly in tasks like image classification. Below are descriptions of several commonly used datasets, each with its unique features and challenges. [3]

A. MNIST:

MNIST is one of the most well-known image classification datasets, used for recognizing handwritten digits. It is simple yet powerful for testing new models, often seen as the "hello world" of deep learning. Each image is a grayscale representation of a single handwritten digit, and the task is to classify which digit is shown in the image. Contains 10 (digits 0-9), Size: 70,000 images (60,000 training, 10,000 testing)

Challenge: While MNIST is easy for modern models, it serves as a great starting point to assess the baseline performance of machine learning architectures.

B. Fashion MNIST:

Fashion MNIST was created as a more challenging replacement for MNIST, containing grayscale images of various fashion items like shirts, shoes, and handbags. Although it shares the same structure as MNIST (image size, number of images), the complexity of recognizing detailed features in clothing makes it a more difficult dataset. Contains: 10 (e.g., T-shirt, trouser, sneaker, bag), Size: 70,000 images (60,000 training, 10,000 testing) same as MNIST.

Challenge: The images have subtle differences between classes, making it harder for models to distinguish between items like T-shirts and pullovers.

C. CIFAR 10

CIFAR-10 is a dataset containing low-resolution color images of 10 different objects, ranging from animals to vehicles. The images are much more complex than MNIST, with varying backgrounds, colors, and shapes. CIFAR-10 is often used to evaluate models' ability to generalize across different object categories. Contains: 10 Classes (airplane, automobile,

bird, cat, deer, dog, frog, horse, ship, truck), Size: 60,000 images (50,000 training, 10,000 testing)

Challenge: The small size and complexity of the images, combined with the need to distinguish between visually similar categories (e.g., trucks vs. automobiles), make CIFAR-10 more difficult than MNIST or Fashion MNIST.

D. CIFAR 100

CIFAR-100 is a more complex version of CIFAR-10, with the same number of images but 100 distinct classes. Each class has far fewer examples (600 per class compared to 6,000 per class in CIFAR-10), making it harder for models to learn and generalize. The images are still 32x32 pixels, which means that distinguishing between the finer details of different objects is particularly challenging. Contains: **Classes:** 100 (e.g., aquarium fish, maple tree, castle, butterfly, motorcycle), **Size:** 60,000 images (50,000 training, 10,000 testing)

Challenge: With 100 classes, the task is significantly more complex. The dataset tests a model's ability to perform well with fewer examples per class and more nuanced distinctions between objects.

6. Implementation

A. MNIST:

```
import torch

import torch.nn.functional as F

from torch.utils.data import DataLoader

from torchvision import datasets, transforms

from skimage.segmentation import slic

from skimage import graph # Corrected import

import matplotlib.pyplot as plt

import networkx as nx

from torch_geometric.data import Data, Batch # Import Batch

from torch_geometric.nn import GCNConv, global_mean_pool

from torch_geometric.utils import to_networkx

import numpy as np


# Load MNIST Dataset

transform = transforms.Compose([transforms.ToTensor()])

mnist_train = datasets.MNIST(root='data', train=True, download=True,
transform=transform)

mnist_test = datasets.MNIST(root='data', train=False, download=True,
transform=transform)


# Function to Convert Image to Superpixel Graph

def image_to_graph(image, segments=75, plot_graph=False):

    # Convert the image to superpixels

    image_np = image.squeeze().numpy()

    # Use slic for superpixel segmentation, specify channel_axis=None for grayscale
```

```
superpixels = slic(image_np, n_segments=segments, compactness=0.1, start_label=0,
channel_axis=None)
```

```
# Create Region Adjacency Graph (RAG)
```

```
rag = graph.rag_mean_color(image_np, superpixels, mode='distance')
```

```
# Get node features (average intensity of each superpixel)
```

```
node_features = []
```

```
for region in rag.nodes:
```

```
    mask = (superpixels == region)
```

```
    avg_intensity = np.mean(image_np[mask])
```

```
    node_features.append([avg_intensity])
```

```
# Get edges from the RAG
```

```
edge_index = []
```

```
for edge in rag.edges:
```

```
    edge_index.append(edge)
```

```
# Convert to PyTorch tensors
```

```
node_features = torch.tensor(node_features, dtype=torch.float)
```

```
edge_index = torch.tensor(edge_index, dtype=torch.long).t().contiguous()
```

```
# Create the graph data object
```

```
graph_data = Data(x=node_features, edge_index=edge_index)
```

```
# Visualize the graph if plot_graph is True
```

```
if plot_graph:
```

```
    # Convert PyTorch Geometric graph to NetworkX for visualization
```

```
    G = to_networkx(graph_data, to_undirected=True)
```

```

pos = nx.spring_layout(G) # Layout for graph visualization

# Create a new figure for visualization
fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(12, 6))

# Plot the superpixels
ax1.imshow(superpixels, cmap='gray')
ax1.set_title('Superpixels')

# Plot the graph on a new axis
nx.draw(G, pos, node_size=20, node_color='r', with_labels=False, ax=ax2) # Use
ax2 for axis control
ax2.set_title('Graph Visualization')

plt.show()

return graph_data

# Define the GNN Model
class GNNModel(torch.nn.Module):
    def __init__(self, hidden_channels):
        super(GNNModel, self).__init__()
        torch.manual_seed(12345)
        self.conv1 = GCNConv(1, hidden_channels)
        self.conv2 = GCNConv(hidden_channels, hidden_channels)
        self.lin = torch.nn.Linear(hidden_channels, 10)

    def forward(self, x, edge_index, batch):
        x = self.conv1(x, edge_index)

```

```

x = x.relu()

x = self.conv2(x, edge_index)


# Global mean pooling (graph-level readout)
x = global_mean_pool(x, batch)


# Apply a final classifier
x = self.lin(x)


return F.log_softmax(x, dim=1)


# DataLoader and Training Setup
def train(model, loader, optimizer):
    model.train()
    total_loss = 0
    correct = 0

    for images, labels in loader:
        optimizer.zero_grad()

        graphs = []
        for image in images:
            graph = image_to_graph(image)
            graphs.append(graph)

        data_list = [g.to(device) for g in graphs]
        batch = Batch.from_data_list(data_list)

        out = model(batch.x, batch.edge_index, batch.batch)

```

```

    loss = F.nll_loss(out, labels)
    loss.backward()
    optimizer.step()

    total_loss += loss.item()
    correct += out.argmax(dim=1).eq(labels).sum().item()

return total_loss / len(loader.dataset), correct / len(loader.dataset)

def test(model, loader):
    model.eval()
    total_loss = 0
    correct = 0

    with torch.no_grad():
        for images, labels in loader:
            graphs = []
            for image in images:
                graph = image_to_graph(image)
                graphs.append(graph)

            data_list = [g.to(device) for g in graphs]
            batch = Batch.from_data_list(data_list)

            out = model(batch.x, batch.edge_index, batch.batch)
            loss = F.nll_loss(out, labels)

            total_loss += loss.item()
            correct += out.argmax(dim=1).eq(labels).sum().item()

```

```

    return total_loss / len(loader.dataset), correct / len(loader.dataset)

# Set device and hyperparameters
device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
model = GNNModel(hidden_channels=16).to(device)
optimizer = torch.optim.Adam(model.parameters(), lr=0.01)

# Prepare DataLoader
train_loader = DataLoader(mnist_train, batch_size=64, shuffle=True)
test_loader = DataLoader(mnist_test, batch_size=64, shuffle=False)

# Training loop
num_epochs = 5
for epoch in range(num_epochs):
    train_loss, train_acc = train(model, train_loader, optimizer)
    test_loss, test_acc = test(model, test_loader)

    print(f'Epoch {epoch+1}, Train Loss: {train_loss:.4f}, Train Acc: {train_acc:.4f}, Test
    Loss: {test_loss:.4f}, Test Acc: {test_acc:.4f}')

# Step 6: Visualize graph for an example image
image, label = mnist_train[0] # Get the first image from the training set
graph_data = image_to_graph(image, plot_graph=True)

```

OUTPUT:

Epoch 1, Train Loss: 0.0327, Train Acc: 0.2221, Test Loss: 0.0324, Test Acc: 0.2287
Epoch 2, Train Loss: 0.0323, Train Acc: 0.2347, Test Loss: 0.0323, Test Acc: 0.2390
Epoch 3, Train Loss: 0.0323, Train Acc: 0.2361, Test Loss: 0.0323, Test Acc: 0.2316
Epoch 4, Train Loss: 0.0323, Train Acc: 0.2345, Test Loss: 0.0325, Test Acc: 0.2255
Epoch 5, Train Loss: 0.0323, Train Acc: 0.2360, Test Loss: 0.0323, Test Acc: 0.2327

Figure 3: Loss and accuracy of training and test datasets of MNIST

Graph Visualization

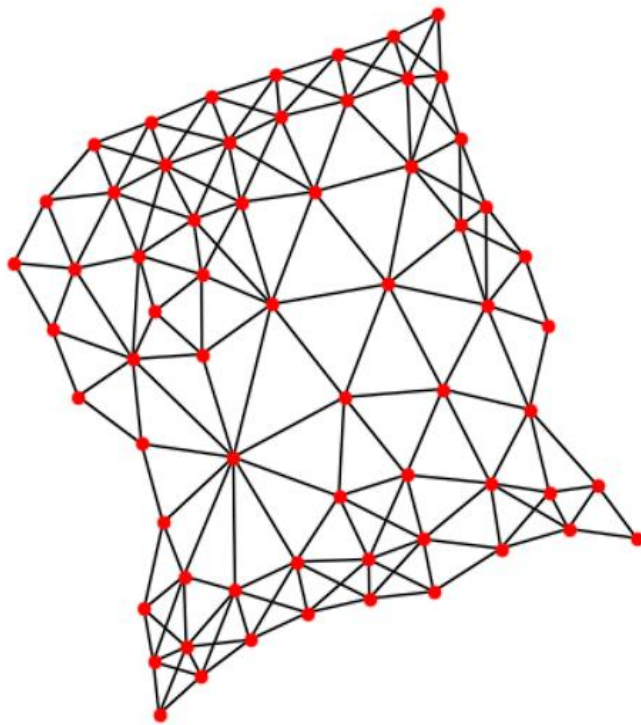


Figure 5: Graphical Visualization of MNIST Dataset

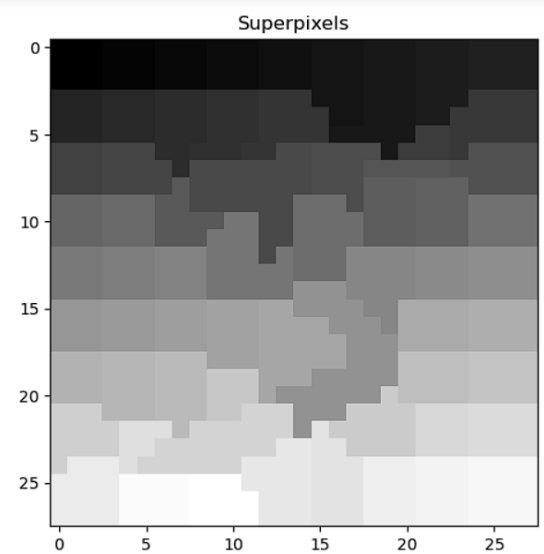


Figure 4: Superpixel Image of MNIST dataset

7. Conclusion:

In this study, we set out to see if Graph Neural Networks (GNNs) could bring something new to the table for image classification, a field dominated by Convolutional Neural Networks (CNNs). Using well-known image datasets like MNIST, Fashion MNIST, CIFAR-10, and CIFAR-100, we experimented with representing images as graphs—where pixels or regions become nodes, and their connections form edges. This approach allowed us to see if GNNs could capture more complex relationships in images that CNNs might miss.

Our findings show that GNNs have the potential to pick up on deeper, long-range patterns and contextual clues in images. This ability comes from the graph-based approach, which lets GNNs explore relationships beyond just local features. While they might require more computing power compared to CNNs, GNNs performed well across the datasets, especially in situations where the structure of the image mattered more than just the local details.

Overall, GNNs offer a fresh perspective in image classification. They may not always outperform CNNs, but they do provide a valuable alternative when understanding complex relationships is key. This study suggests that GNNs could be a strong choice for certain tasks, and there's a lot of potential in combining them with CNNs to get the best of both worlds. Future work could focus on refining how we turn images into graphs and finding the sweet spot between the power of CNNs and the unique strengths of GNNs.

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