# **Neural Networks**



Alejandra Carriero

## Recap

Yesterday we introduced different models.

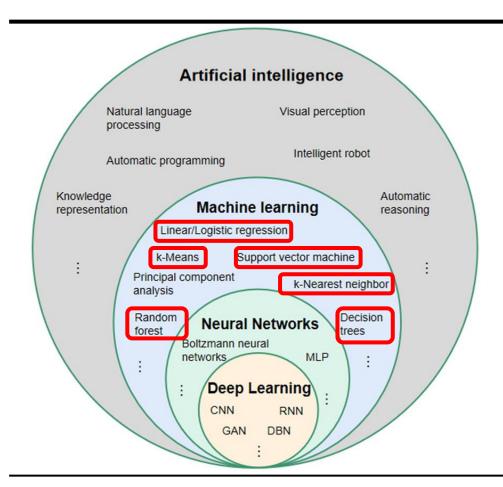
#### For classification:

- SVM
- Random Forest

#### For **clustering**:

- K-means





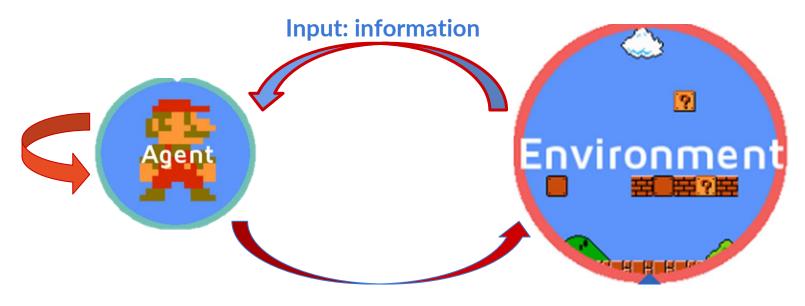


#### **Contents**

- What are Neural Networks
- Artificial Neurons
- Training Neural Networks
- Some types of Neural Networks (CNNs, RNNs, LSTMs)



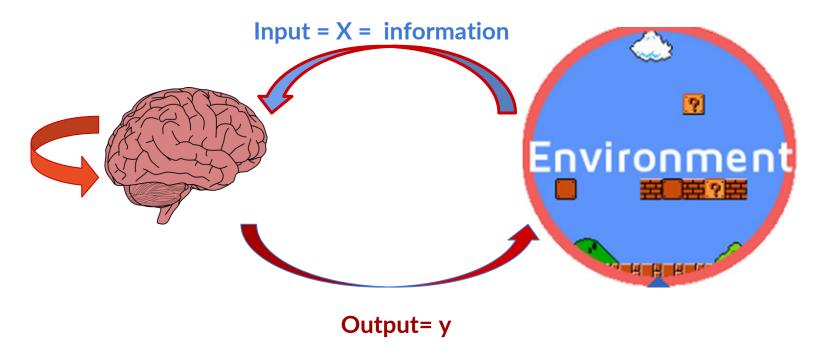
### **Neurons and Artificial Neural Networks**



**Output: Action** 

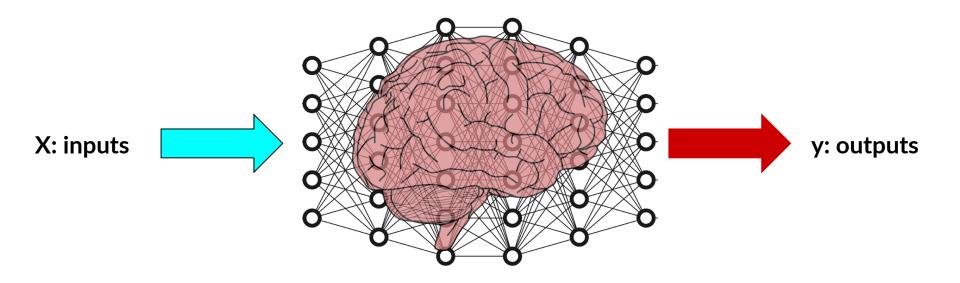


### **Neurons and Artificial Neural Networks**





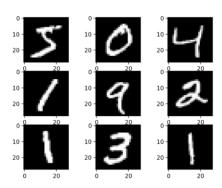
### **Neurons and Artificial Neural Networks**





### **Artificial Neural Networks can be classifiers**

#### Dataset

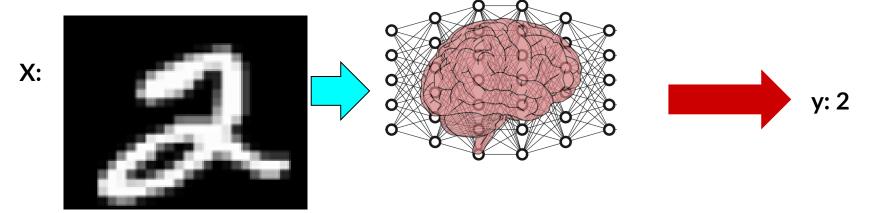


60,000 small square 28×28 pixel grayscale images of handwritten single digits between 0 and 9



### **Artificial Neural Networks can be classifiers**

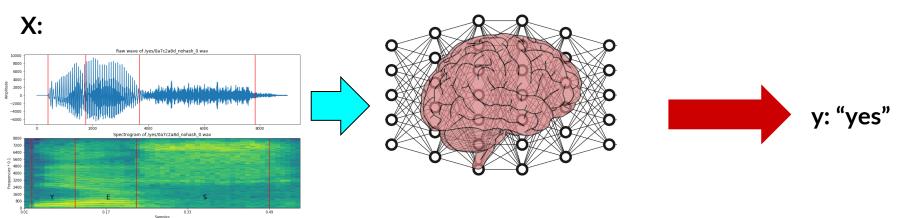
**Image recognition** 





#### Artificial Neural Networks can be classifiers

#### **Speech recognition**



Spectrogram of the spoken word "yes"



#### **Artificial Neural Networks**

#### Can do countless things, including:

#### Natural Language Processing (NLP):

**Input:** Text data (e.g., a sentence or document).

**Output:** Processed text (e.g., sentiment score, translated text, or named entities).

#### Medical Diagnosis:

**Input:** Medical images (e.g., X-rays, MRIs) or patient data (e.g., age, symptoms).

**Output:** Diagnosis or probability of a condition (e.g., presence of a tumor).

#### Financial Services:

**Input:** Historical financial data (e.g., stock prices, transaction records). **Output:** Predictions (e.g., future stock prices, fraud detection alerts).

#### Autonomous Vehicles:

**Input**: Sensor data (e.g., camera images, LIDAR scans).

Output: Driving actions (e.g., steering angle, acceleration, braking).

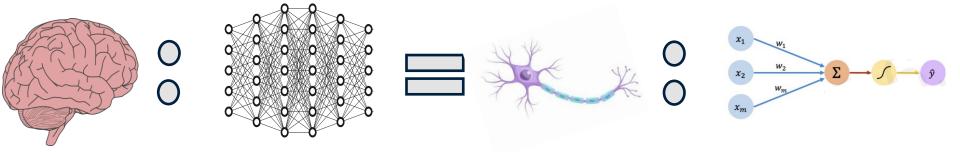
#### Recommendation Systems:

**Input**: User behaviour data (e.g., past purchases, viewing history).

Output: Recommendations (e.g., movies, products



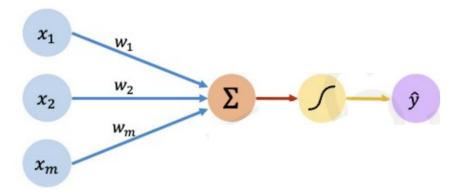
## Perceptron: the singular neuron

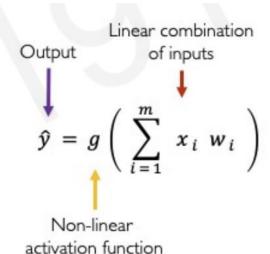




## Perceptron: the singular neuron

The building block of Artificial Neural Networks





## Does this remind you of anything?

Inputs Weights Sum Non-Linearity Output



## Logistic regression

There are many important research topics for which the dependent variable is "limited."

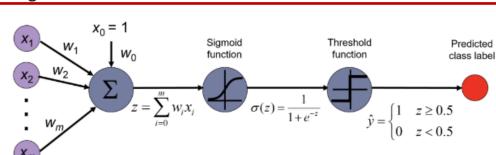
For example: voting, mortality, or number of accidents is not continuous or distributed normally.

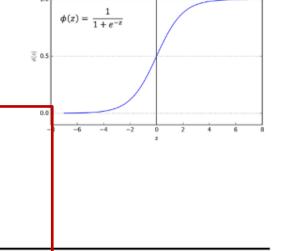
$$Z = X \cdot W = w0 + w1 \cdot x1 + w2 \cdot x2 + ... + wn \cdot xn$$

Uses the sigmoid function to enforce the classification

You can also have a bias term

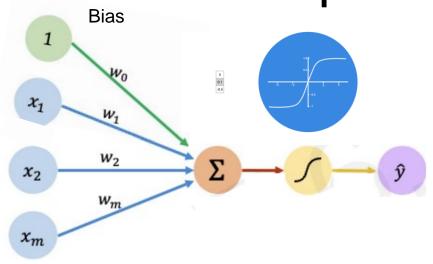
Number of weights = number of features + one bias

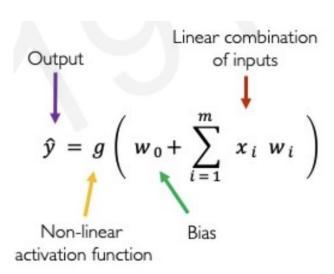






### Perceptron: the singular neuron



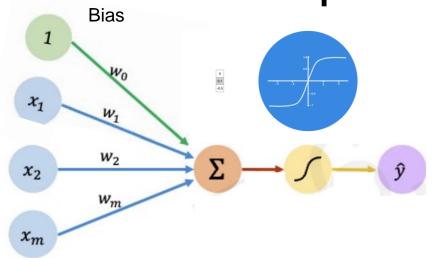


Inputs Weights Sum Non-Linearity Output

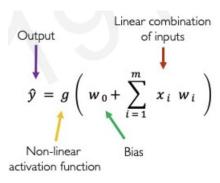


The bias term is a scalar that allows us to shift left or right along our activation function

## Perceptron: the singular neuron



Inputs Weights Sum Non-Linearity Output

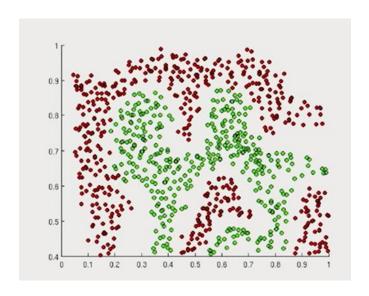


$$\hat{y} = g (w_0 + X^T W)$$
where:  $X = \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix}$  and  $W = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}$ 



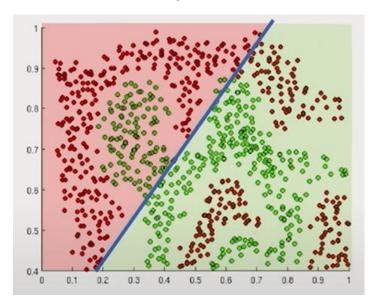
## Why do we need Activation Functions?

The purpose of activation functions is to introduce **non-linearities** into the network

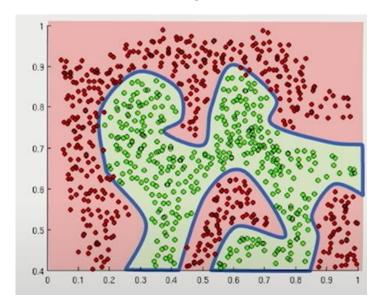




## Why do we need non-linearity?

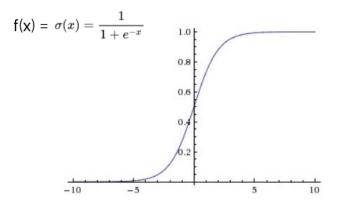


**Linear activation functions** produce **linear decisions** no matter the network size



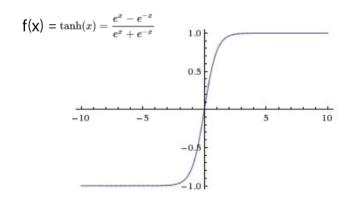
**Non-linearities** allow us to **approximate** arbitrarily complex functions





**Sigmoid** non-linearity squashes the numbers to range between [0,1].

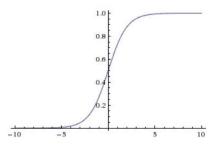
Used for models where we have to predict the probability as an output



**tanh** non-linearity squashes the numbers to range between [-1,1]

Tanh tends to be preferred to sigmoid



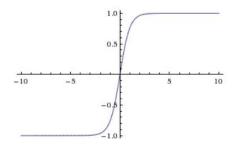


```
from sklearn.neural_network import MLPClassifier

# Define the neural network with the sigmoid activation function

clf = MLPClassifier(activation='logistic', hidden_layer_sizes= (100,), max_iter=300)

# Train the neural network on the training data clf.fit(X_train, y_train)
```

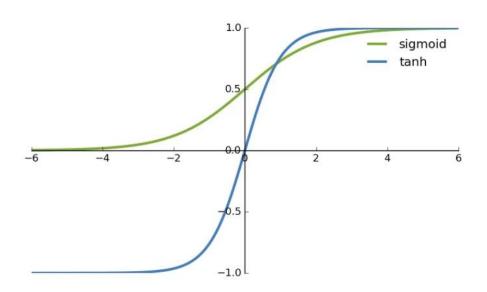


```
from sklearn.neural_network import MLPClassifier

# Define the neural network with the tanh activation function clf = MLPClassifier(activation='tanh', hidden_layer_sizes= (100,), max_iter=300)

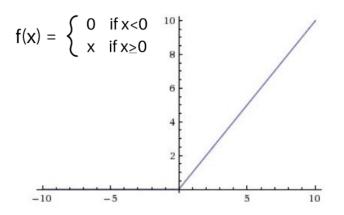
# Train the neural network on the training data clf.fit(X_train, y_train)
```







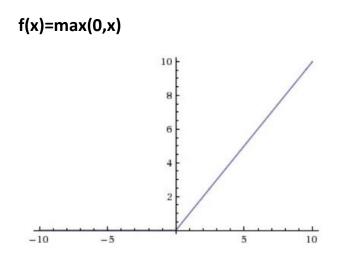
#### f(x)=max(0,x)



**ReLu** (Rectified Linear Unit) activation function is zero when x < 0 and then linear with slope 1 when x > 0

- ReLu speeds up the calculations up to 6x compared to tanh
- ReLU units can be fragile during training and can "die". (i.e. neurons that never activate across the entire training dataset) if the learning rate is set too high. With a proper setting of the learning rate this is less frequently an issue.





**ReLu** (Rectified Linear Unit) activation function is zero when x < 0 and then linear with slope 1 when x > 0

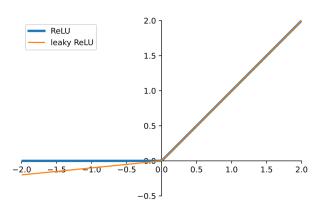
```
from sklearn.neural_network import MLPClassifier

# Define the neural network with the ReLU activation function
clf = MLPClassifier(activation='relu', hidden_layer_sizes=(100,), max_iter=300)

# Train the neural network on the training data
clf.fit(X_train, y_train)
```



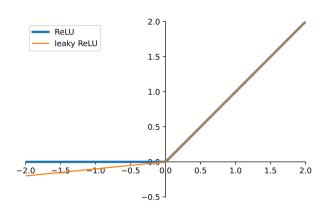
$$f(x) = \begin{cases} 0.01x & \text{if } x < 0 \\ x & \text{if } x \ge 0 \end{cases}$$



- Leaky ReLUs are one attempt to fix the "dying ReLU" problem.
- Instead of the function being zero when x < 0, a leaky ReLU will instead have a small positive slope (of 0.01, or so). That is, the function computes f(x)=1(x<0)(αx)+1(x>=0)(x) where α is a small constant.

Other solutions to the "dying ReLU" problem include ELUs (Exponential Linear Units) and PReLUs (Parametric ReLU).





 Leaky ReLUs are one attempt to fix the "dying ReLU" problem.

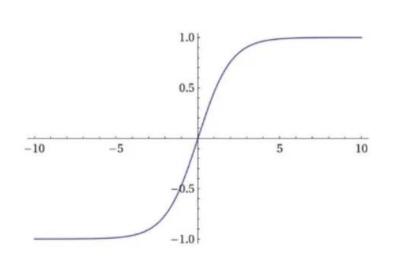
```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, LeakyReLU

# Define the neural network model
model = Sequential([
    # Add a dense layer with 100 neurons
Dense(100, input_dim=input_dim),
    # Apply Leaky ReLU activation function with alpha=0.01
LeakyReLU(alpha=0.01),
    # Add the output layer with softmax activation for multi-class classification
Dense(output_dim, activation='softmax')
])

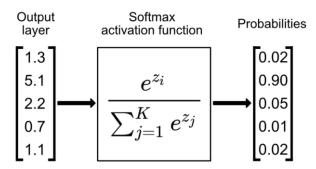
# Compile the model with Adam optimizer and categorical crossentropy loss
model.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'])

# Train the neural network on the training data
model.fit(X_train, y_train, epochs=300)
```





- Softmax is used when you need to classify data into more than two categories. For example, if you have a dataset with images of cats, dogs, and birds, Softmax can help determine the probability that a given image belongs to each of these classes.
- It is applied after the output.

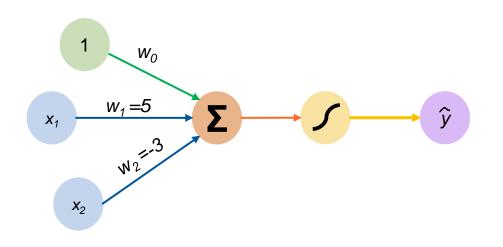




ACTIVATION FUNCTION	PLOT	EQUATION	DERIVATIVE	RANGE
Linear	-/	f(x) = x	f'(x) = 1	(-∞, ∞)
Binary Step		$f(x) = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{if } x \ge 0 \end{cases}$	$\mathbf{f}'(x) = \begin{cases} 0 & \text{if } x \neq 0 \\ \text{undefined} & \text{if } x = 0 \end{cases}$	{0, 1}
Sigmoid		$f(x) = \sigma(x) = \frac{1}{1 + e^{-x}}$	f'(x) = f(x)(1 - f(x))	(0, 1)
Hyperbolic Tangent(tanh)		$f(x) = \tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$	$f(x) = 1 - f(x)^2$	(-1, 1)
Rectified Linear Unit(ReLU)		$f(x) = \begin{cases} 0 & \text{if } x < 0 \\ x & \text{if } x \ge 0 \end{cases}$	$f'(x) = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{if } x > 0 \\ \text{undefined} & \text{if } x = 0 \end{cases}$	[0, ∞) .
Softplus		$f(x) = \ln(1 + e^x)$	$f(x) = \frac{1}{1 + e^{-x}}$	(0, 1)
Leaky ReLU		$f(x) = \begin{cases} 0.01x & \text{if } x < 0 \\ x & \text{if } x \ge 0 \end{cases}$	$f'(x) = \left\{ \begin{array}{ll} 0.01 & \text{if } x < 0 \\ 1 & \text{if } x \geq 0 \end{array} \right.$	(-1, 1)
Exponential Linear Unit(ELU)		$f(x) = \begin{cases} \alpha (e^x - 1) & \text{if } x \le 0 \\ x & \text{if } x > 0 \end{cases}$	$f'(X) = \begin{cases} \alpha e^x & \text{if } x < 0 \\ 1 & \text{if } x > 0 \\ 1 & \text{if } x = 0 \text{ and } \alpha = 1 \end{cases}$	[0, ∞)



## Perceptron: an example



We have  $w_0 = 1$  and  $W = \begin{bmatrix} 5 \\ -3 \end{bmatrix}$ 

$$\hat{y} = g(w_0 + X^T W)$$

$$= g\left(1 + \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}^T \begin{bmatrix} 5 \\ -3 \end{bmatrix}\right)$$

$$\hat{y} = g(1 + 5x_1 - 3x_2)$$

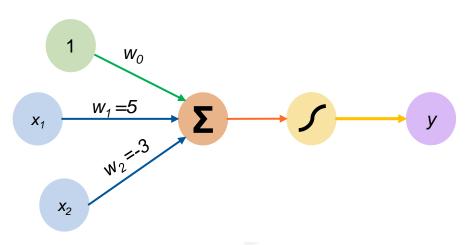
This is just a line in 2D!

Inputs Weights

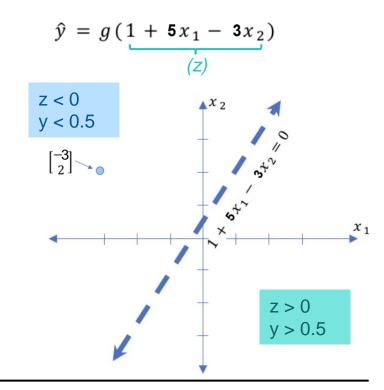
Sum Non-Linearity Output



## Perceptron: an example

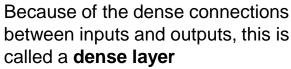


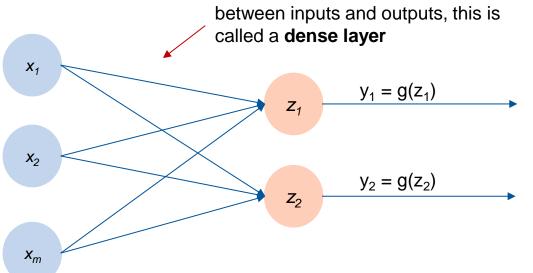
If we have an input 
$$X = \begin{bmatrix} -3 \\ 2 \end{bmatrix}$$
  
 $\hat{y} = g(1 + (5*-3) - (3*2))$   
 $= g(-20) = 2.06 \text{ E-9}$ 





## Multi-output perceptron



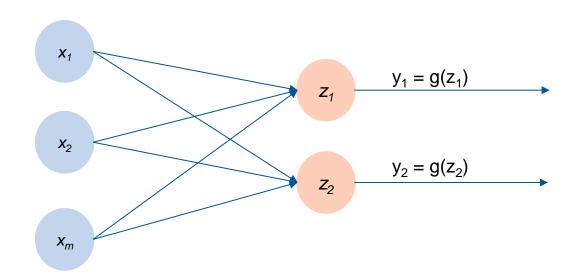


This is just an example to understand the intuition, but multioutput perceptrons are useful when you need to predict multiple target variables simultaneously. For example, predicting both temperature and humidity based on weather data.

$$z_{i} = w_{0,i} + \sum_{j=1}^{m} x_{j} w_{j,i}$$



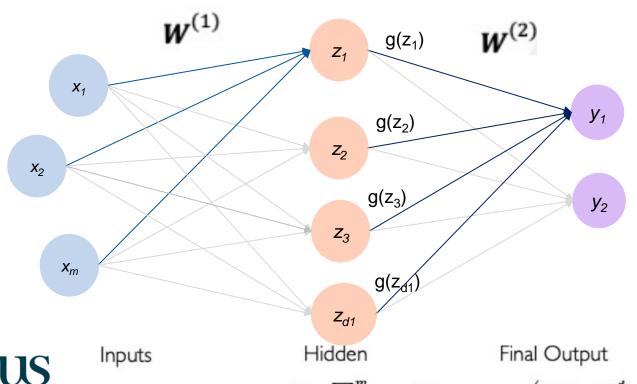
### Multi-output perceptron



$$z_{i} = w_{0,i} + \sum_{j=1}^{m} x_{j} w_{j,i}$$



## Single Layer Neural Network



In layered neural networks, the outputs from one layer become the inputs of the next layer



$$z_i = w_{0,i}^{(1)} + \sum_{j=1}^m x_j w_{j,i}^{(1)}$$

$$\hat{y}_i = g\left(w_{0,i}^{(2)} + \sum_{j=1}^{d_1} g(z_j) w_{j,i}^{(2)}\right)$$

## Single Layer Neural Network

#### For classification:

```
from sklearn.neural network import MLPClassifier
from sklearn.datasets import make classification
from sklearn.model_selection import train_test_split
# Generate synthetic classification data
X, y = make_classification(n_samples=1000, n_features=20, n_classes=2,
random state=42)
X_train, X_test, y_train, y_test = train_test_split(X, y,
test_size=0.2, random_state=42)
clf = MLPClassifier(hidden layer sizes=(100,), activation='relu',
max iter=300)
clf.fit(X_train, y_train)
predictions = clf.predict(X test)
```

#### For regression:

```
from sklearn.neural network import MLPRegressor
from sklearn.datasets import make regression
from sklearn.model_selection import train_test_split
X, y = make_regression(n_samples=1000, n_features=20, noise=0.1
random state=42)
X train, X test, y train, y test = train test split(X, y,
test size=0.2, random state=42)
reg = MLPRegressor(hidden layer sizes=(100,), activation='relu',
max iter=300)
reg.fit(X_train, y_train)
predictions = reg.predict(X_test)
```



## Single Layer Neural Network

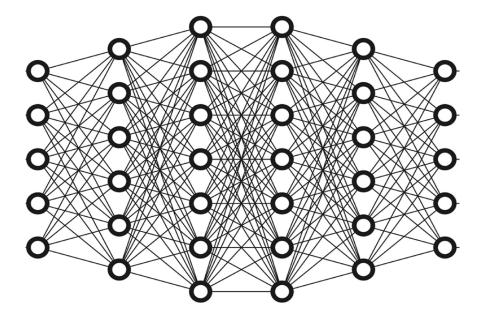
#### For classification:

OF SUSSEX

```
from sklearn.neural network import MLPClassifier
from sklearn.datasets import make classification
from sklearn.model_selection import train_test_split
X, y = make_classification(n_samples=1000, n_features=20, n_classes=2,
random state=42)
X_train, X_test, y_train, y_test = train_test_split(X, y,
test_size=0.2, random_state=42)
clf = MLPClassifier(hidden layer sizes=(100,), activation='relu',
max iter=300)
clf.fit(X_train, y_train)
predictions = clf.predict(X test)
```

- n\_samples= The number of samples (data points) in your dataset. 1000 creates 1000 data points.
- n\_features=The number of features (input variables) in your dataset. 20 means each data point has 20 input variables.
- n\_classes= It determines how many different categories the target variable (y) can take.2 means the target variable (y) will have three distinct class labels (e.g., 0, 1).
- random\_state=A seed value for random number generation to ensure reproducibility. 42 ensures the data generation process is reproducible.

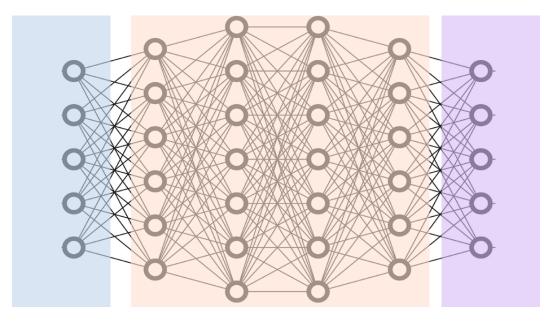
## Multi Layer Neural Network



In layered neural networks, the outputs from one layer become the inputs of the next layer



## Multi Layer Neural Network



In layered neural networks, the outputs from one layer become the inputs of the next layer



**OF SUSSEX** 

Inputs Hidden Layers

Outputs

# Multi Layer Neural Network

#### For classification:

```
from sklearn.neural network import MLPClassifier
from sklearn.datasets import make classification
from sklearn.model selection import train test split
X, y = make classification(n samples=1000, n features=20, n classes=2, random state=42)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
clf = MLPClassifier(hidden layer sizes=(100, 50), activation='relu', max iter=300)
clf.fit(X train, y train)
predictions = clf.predict(X test)
```

 hidden\_layer\_sizes= in this case it specifies two hidden layers, the first with 100 neurons and the second with 50 neurons.



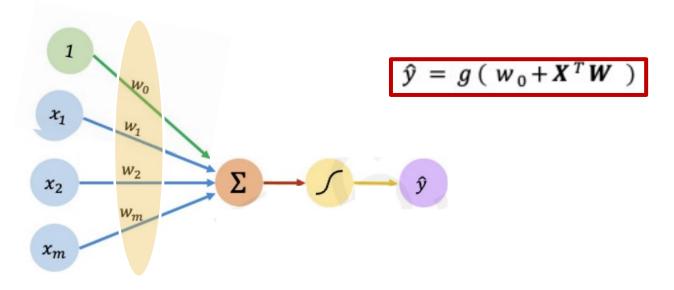
# Training a neural network



The code does it for us. But what does it do exactly?



# Think about your data and think about this model





Is there any information we don't have?

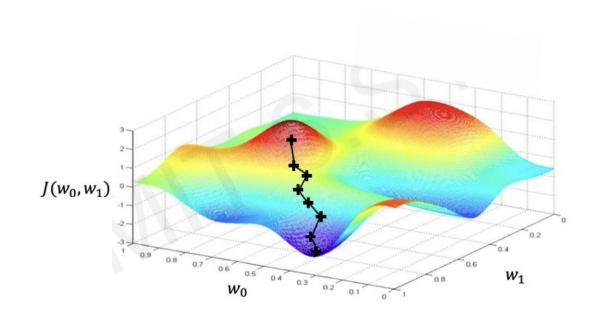
# Loss optimisation

- Quantify the Loss (how wrong the outputs y are compared to our test data)
- Update the weights (through gradient descent and backpropagation) to minimise this loss



# Loss optimisation

- Quantify the Loss (how wrong the outputs y are compared to our test data)
- Update the weights
   (through gradient descent and backpropagation) to minimise this loss





scikit-learn handles all the underlying details of backpropagation and gradient descent, allowing you to focus on defining and training your model

### The code handles this for us



# **Types of ANNs**

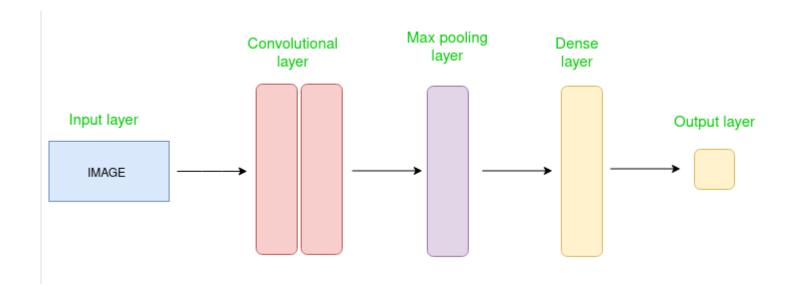


### **Convolutional Neural Networks (CNNs)**

CNNs are designed for visual data processing.









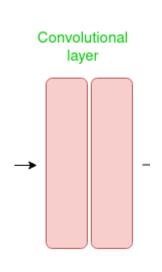
Input layer

IMAGE

Let's take an example by running an image of dimension 32 x 32 x 3.

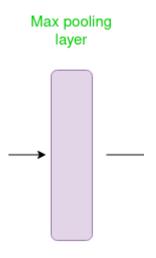
•Input Layers: It's the layer in which we give input to our model. In CNN, Generally, the input will be an image or a sequence of images. This layer holds the raw input of the image with width 32, height 32, and depth 3 (= the colour array).





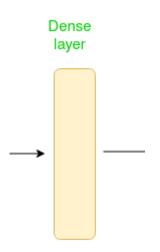
- **Filters/Kernels**: Small matrices that slide over the input image. Each filter is designed to detect specific features like edges, textures, or patterns. Imagine looking at an image through a small window that slides over the picture. Each window (filter) looks for specific things like edges or patterns.
- Convolution Operation: The filter is applied to the input image, producing a feature map. This operation involves multiplying the filter values with the corresponding pixel values and summing them up. The result is a new matrix that highlights the presence of the feature detected by the filter. As the window slides over the image, it creates a new picture (feature map) that highlights where it found those edges or patterns.
- **ReLU:** After the window slides over the image, ReLU changes all negative values to zero. This helps the network focus on important features and ignore less useful information.





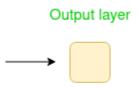
- Max Pooling: This layer reduces the dimensionality
  of the feature map while retaining important
  features. It does this by selecting the maximum
  value from a small region (e.g., 2x2) of the feature
  map. This helps in reducing computational load and
  preventing overfitting.
- Think of zooming out on a picture to make it smaller while keeping the important parts. Max pooling picks the biggest value from a small area, reducing the size of the feature map but keeping the key features.





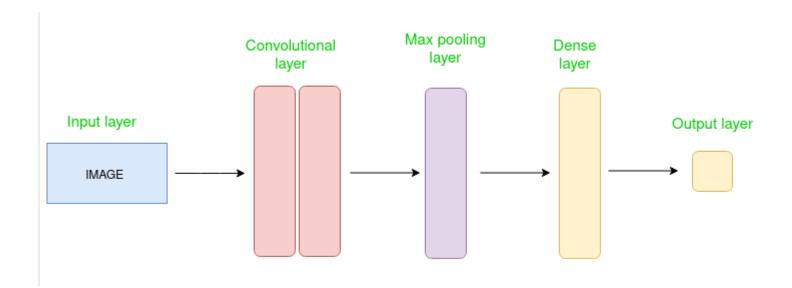
- Flattening: Converts the 2D feature maps into a 1D vector. This step prepares the data for the fully connected layers. Imagine taking all the important features from the picture and laying them out in a single line.
- Dense Layers: These layers connect every neuron from one layer to every neuron in the next layer. They combine the features learned by the convolutional and pooling layers to make final predictions. This is where the network decides which class the input image belongs to.



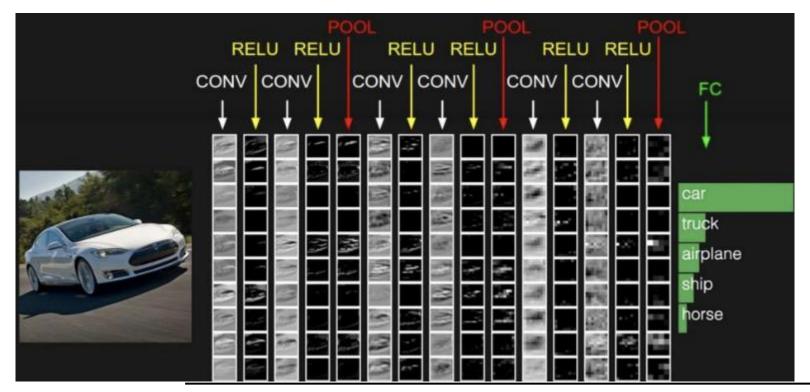


• Output Layer: The output from the fully connected layers is then fed into a logistic function for classification tasks like sigmoid or softmax which converts the output of each class into the probability score of each class.











```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Conv2D, MaxPooling2D, Flatten, Dense
model = Sequential()
model.add(Conv2D(32, (3, 3), activation='relu', input shape=(64, 64, 3)))
model.add(MaxPooling2D(pool size=(2, 2)))
model.add(Conv2D(64, (3, 3), activation='relu'))
model.add(MaxPooling2D(pool size=(2, 2)))
model.add(Flatten())
model.add(Dense(128, activation='relu'))
model.add(Dense(10, activation='softmax'))
model.compile(optimizer='adam', loss='categorical crossentropy', metrics=['accuracy'])
model.summary()"
```

#### 1.Convolutional Layers:

- Number of Filters: The choice of 32 and 64 filters is typical for initial layers in a CNN.
  These numbers can be adjusted based on the complexity of the task and the size of
  the dataset.
- Kernel Size: A 3x3 kernel is a standard choice that balances computational efficiency and the ability to capture spatial features.

#### 2.Pooling Layers:

 Pool Size: A 2x2 pool size is commonly used to reduce the spatial dimensions while retaining important features.

#### 3.Fully Connected Layers:

 Number of Neurons: The choice of 128 neurons in the dense layer is a common practice, but it can be tuned based on the complexity of the task.

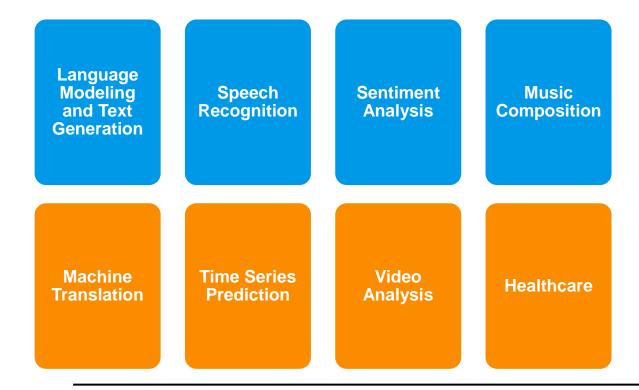
#### 4.Activation Functions:

- ReLU: The ReLU activation function is widely used due to its ability to mitigate the vanishing gradient problem and speed up training.
- . **Softmax**: Softmax is used in the output layer for multi-class classification tasks.

#### 5.Optimizer and Loss Function:

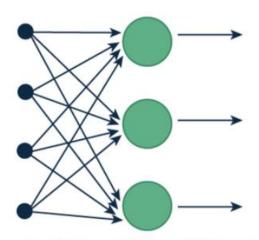
- Adam Optimizer: Adam is a popular choice for its adaptive learning rate and efficiency.
- Categorical Crossentropy: This loss function is suitable for multi-class classification problems.



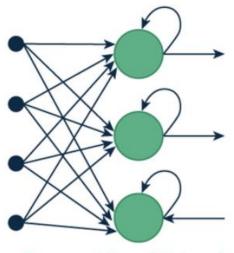




RNNs are unique because they have **loops in their architecture**, allowing information to persist. This makes them well-suited for **tasks where context or previous information is important**, such as language modeling or predicting stock prices.



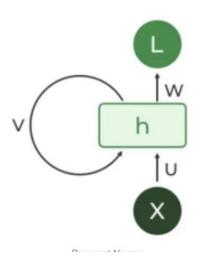




Recurrent Neural Network

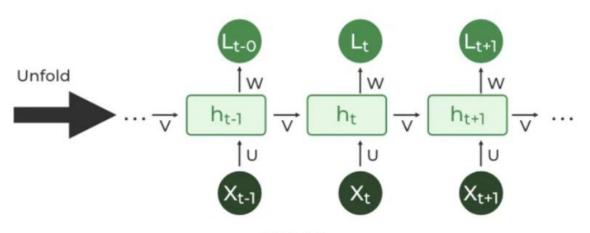


The fundamental processing unit in RNN is a **Recurrent Unit.**.



 Recurrent units hold a hidden state that maintains information about previous inputs in a sequence.
 Recurrent units can "remember" information from prior steps by feeding back their hidden state

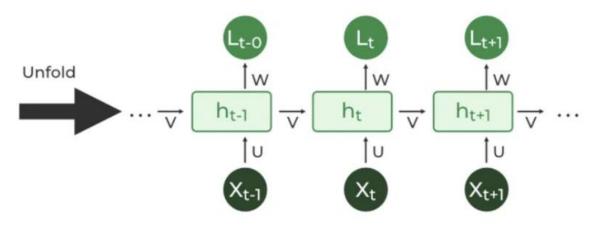




• Sequence Processing:
RNNs process input
sequences one element at
a time, updating the
hidden state at each step.







network's parameters.

But this is also handled by code, so

Time (BPTT) is used to update the

Since RNNs process sequential data **Backpropagation Through** 

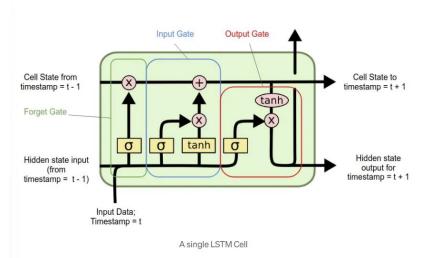
But this is also handled by code, so we don't need to worry about this!





# Long Short-Term Memory (LSTM) networks

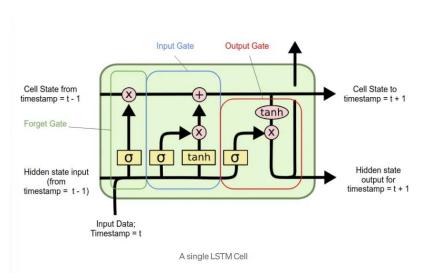
LSTMs are a type of Recurrent Neural Network (RNN) designed to address the limitations of traditional RNNs, particularly the issue of long-term dependencies



- **Cell State**: LSTMs have a cell state that runs through the entire sequence, allowing information to be carried over long distances.
- Gates: LSTMs use gates to control the flow of information. These gates are:
  - Forget Gate: Decides what information to discard from the cell state.
  - Input Gate: Decides what new information to add to the cell state.
  - Output Gate: Decides what information to output from the cell state.



# Long Short-Term Memory (LSTM) networks



#### 1. Forget Gate:

 The forget gate determines which parts of the cell state to forget. It uses a sigmoid function to output values between 0 and 1, where 0 means "forget completely" and 1 means "keep completely."

#### 2. Input Gate:

 The input gate decides which new information to add to the cell state. It uses a sigmoid function to determine which values to update and a tanh function to create new candidate values.

#### 3. Cell State Update:

 The cell state is updated by combining the forget gate's output and the input gate's new candidate values.

#### 4. Output Gate:

The output gate determines the final output of the LSTM cell. It
uses a sigmoid function to decide which parts of the cell state to
output and a tanh function to scale the output.



# **RNNs** implementations

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.models import SimpleRNN, Dense

# Define the RNN model
model = Sequential()

# Add a SimpleRNN layer with 50 units
# 50 units is a common choice for capturing patterns without overfitting
model.add(SimpleRNN(50, input_shape=(None, 1)))

# Add a fully connected layer with 1 neuron and sigmoid activation
# Sigmoid activation is used for binary classification
model.add(Dense(1, activation='sigmoid'))

# Compile the model with Adam optimizer and binary crossentropy loss
# Adam optimizer is efficient and adaptive, binary crossentropy is suitable for binary classification
model.compile(optimizer='adam', loss='binary_crossentropy', metrics=['accuracy'])

# Print the model summary
model.summary()
```

**RNNs**: Suitable for tasks with short-term dependencies, such as simple sequence prediction.

```
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import LSTM, Dense

# Define the LSTM model
model = Sequential()

# Add an LSTM layer with 50 units
# LSTM units are optimal for capturing long-term dependencies
model.add(LSTM(50, input_shape=(None, 1)))

# Add a fully connected layer with 1 neuron and sigmoid activation
# sigmoid activation is used for binary classification
model.add(Dense(1, activation='sigmoid'))

# Compile the model with Adam optimizer and binary crossentropy loss
# Adam optimizer is efficient and adaptive, binary crossentropy is suitable for binary classification
model.compile(optimizer='adam', loss='binary_crossentropy', metrics=['accuracy'])

# Print the model summary
model.summary()
```

**LSTMs**: Suitable for tasks with long-term dependencies, such as language modeling, speech recognition, and time series forecasting.



# Recap

- What are Neural Networks
- Artificial Neurons (perceptron, MLPs, Single and multi layered NNs)
- Training Neural Networks
- Some types of Neural Networks (CNNs, RNNs, LSTMs)



# LAB



## **Neural Nets Lab**

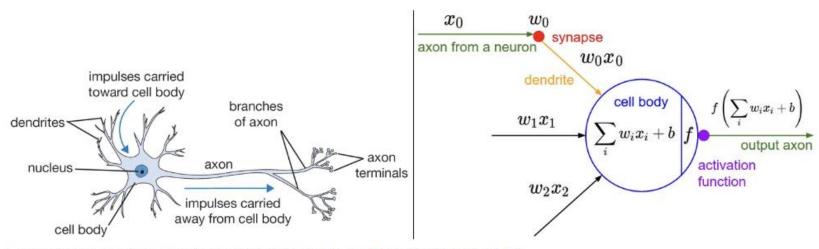
• Go to github for lab8.ipynb



# **Supplementary Material**



# Biological vs Artificial neuron



A cartoon drawing of a biological neuron (left) and its mathematical model (right).



# **Quantifying loss**

$$\mathcal{L}\left(\underline{f\left(x^{(i)}; \boldsymbol{W}\right)}, \underline{y^{(i)}}\right)$$
Predicted Actual

- Empirical loss: measures the total loss over the entire dataset
- Binary Cross Entropy Loss: can be used with models that output a probability between 0 and 1
- Mean Squared Error Loss: can be used with regression models that output continuous numbers

$$\begin{cases}
f(x) & y \\
0.1 & \times \\
0.8 & \times \\
0.6 & \checkmark
\end{cases}$$

$$\begin{bmatrix}
1 & 0 \\
0 & 1 \\
\vdots & \vdots
\end{bmatrix}$$

f(x)

$$J(W) = \frac{1}{n} \sum_{i=1}^{n} \mathcal{L}\left(f(x^{(i)}; W), y^{(i)}\right)$$
Predicted Actual

$$J(\mathbf{W}) = -\frac{1}{n} \sum_{i=1}^{n} \underbrace{y^{(i)} \log \left( f(\mathbf{x}^{(i)}; \mathbf{W}) \right) + (1 - y^{(i)}) \log \left( 1 - f(\mathbf{x}^{(i)}; \mathbf{W}) \right)}_{\text{Actual}} + \underbrace{Actual}_{\text{Predicted}}$$

$$J(\mathbf{W}) = \frac{1}{n} \sum_{i=1}^{n} \underbrace{\left(y^{(i)} - f(x^{(i)}; \mathbf{W})\right)^{2}}_{\text{Actual}}$$

# Loss optimisation

We want to find the network weights that achieve the lowest loss

$$W^* = \underset{W}{\operatorname{argmin}} \frac{1}{n} \sum_{i=1}^{n} \mathcal{L}(f(x^{(i)}; W), y^{(i)})$$

$$W^* = \underset{W}{\operatorname{argmin}} J(W)$$

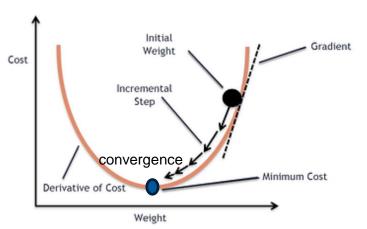
$$W = \underset{W}{\operatorname{Remember:}}$$

$$W = \{w^{(0)}, w^{(1)}, \dots\}$$



### **Gradient descent**

"A gradient measures how much the output of a function changes if you change the inputs a little bit." — Lex Fridman (MIT)

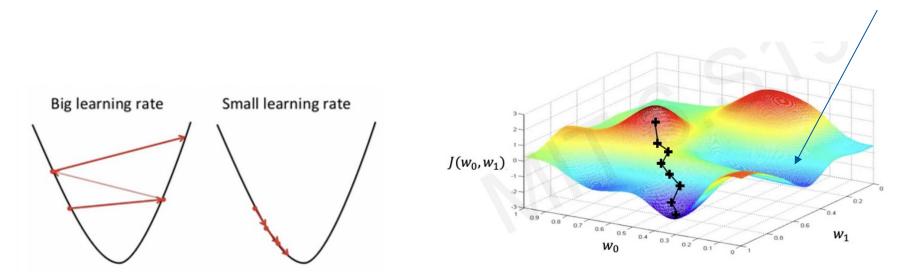


#### Algorithm

- 1. Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Compute gradient,  $\frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
- 4. Update weights,  $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
- 5. Return weights



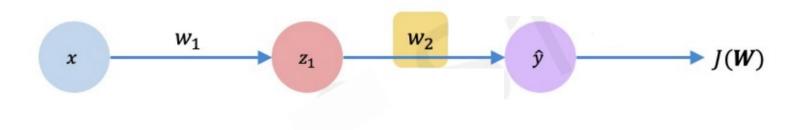
# **Gradient Descent and learning rate**



A big learning rate may not find a minimum, but a small learning rate might get stuck in a local minimum



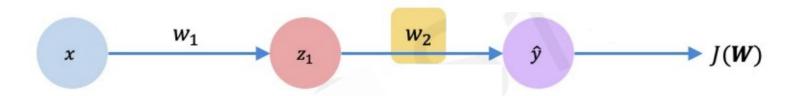
# **Backpropagation**



How does a small change in one weight (ex.  $w_2$ ) affect the final loss J(W)?



# **Backpropagation**

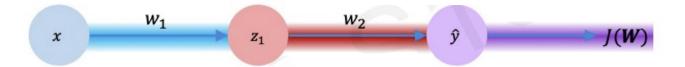


How does a small change in one weight (ex.  $w_2$ ) affect the final loss J(W)?

$$\frac{\partial J(\mathbf{W})}{\partial w_2} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial w_2}$$



# **Backpropagation**



$$\frac{\partial J(\mathbf{W})}{\partial w_1} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial z_1} * \frac{\partial z_1}{\partial w_1}$$

Applying the chain rule!



#### Recommended resources

- Stanford's Convolutional neural networks for visual recognition notes on neural networks <a href="https://cs231n.github.io/neural-networks-1/">https://cs231n.github.io/neural-networks-1/</a>
- MIT's intro to deep learning course https://introtodeeplearning.com/
- A Tutorial on Deep Learning Part 2: Autoencoders, Convolutional Neural Networks and Recurrent Neural Networks tutorial2.pdf

