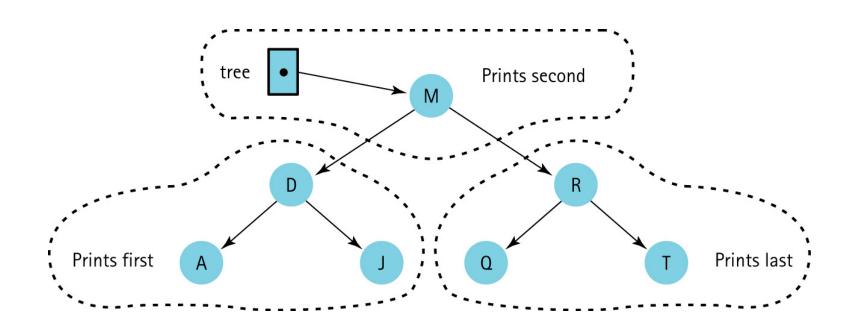


Chapter
8-2
Binary
Search Trees



Printing all the Nodes in Order



Function Print

Function Print

Definition: Prints the items in the binary search

tree in order from smallest to largest.

Size: The number of nodes in the tree whose

root is tree

Base Case: If tree = NULL, do nothing.

General Case: Traverse the left subtree in order.

Then print Info(tree).

Then traverse the right subtree in order.



Code for Recursive InOrder Print

```
void PrintTree(TreeNode* tree,
 std::ofstream& outFile)
 if (tree != NULL)
  PrintTree(tree->left, outFile);
  outFile << tree->info;
  PrintTree(tree->right, outFile);
Is that all there is?
```

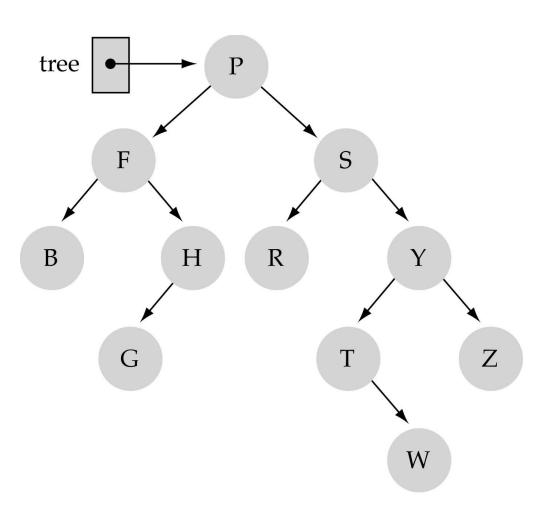


Class Constructor

```
template<class ItemType>
TreeType<ItemType>::TreeType()
{
  root = NULL;
}
```



Class Destructor



How should we delete the nodes of a tree?

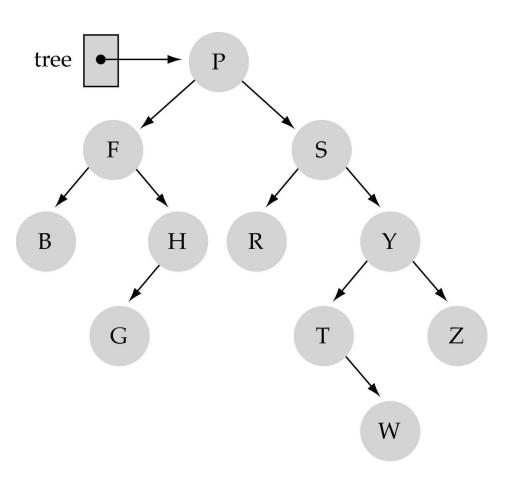


Destructor

```
void Destroy(TreeNode*& tree);
TreeType::~TreeType()
  Destroy(root);
void Destroy(TreeNode*& tree)
  if (tree != NULL)
    Destroy(tree->left);
    Destroy(tree->right);
    delete tree;
```



Copy Constructor



How should we create a copy of a tree?



Algorithm for Copying a Tree

```
if (originalTree is NULL)
   Set copy to NULL
else
   Set Info(copy) to Info(originalTree)
   Set Left(copy) to Left(originalTree)
   Set Right(copy) to Right(originalTree)
```

What traversal order de we use?



Code for CopyTree

```
TreeType::TreeType(const TreeType& originalTree)
 CopyTree(root, originalTree.root);
void CopyTree(TreeNode*& copy,
     const TreeNode* originalTree)
 if (originalTree == NULL)
    copy = NULL;
 else
    copy = new TreeNode;
    copy->info = originalTree->info;
    CopyTree(copy->left, originalTree->left);
    CopyTree(copy->right, originalTree->right);
```



 A tree traversal means visiting all the nodes in the tree

"visit" means that the algorithm does something with the values in the node, e.g., print the value



Tree Traversal Methods

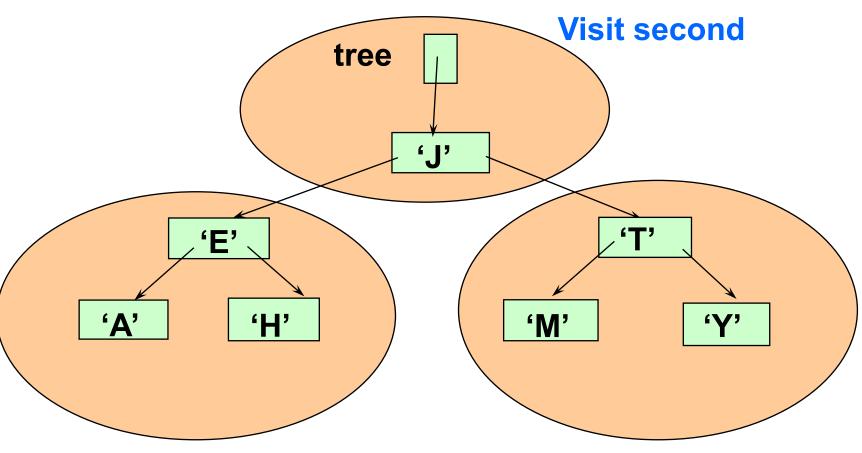
There are mainly three ways to traverse a tree:

- 1) Inorder Traversal
- 2) Postorder Traversal
- 3) Preorder Traversal



Inorder Traversal

Inorder Traversal: A E H J M T Y



Visit left subtree first

Visit right subtree last



Inorder(tree)

if tree is not NULL
 Inorder(Left(tree))
 Visit Info(tree)
 Inorder(Right(tree))

To print in alphabetical order



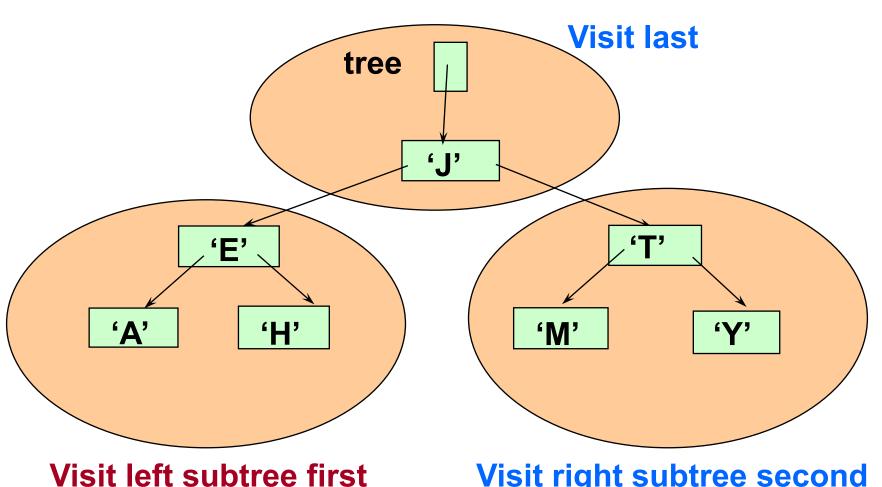
InOrder Implementation

```
void InOrder(TreeNode* tree,
   QueType& inQue)
{
  if(tree != NULL) {
    InOrder(tree->left, inQue);
    inQue.Enqueue(tree->info);
    InOrder(tree->right, inQue);
  }
}
```



Postorder Traversal

Postorder Traversal: AHEMYTJ



Visit right subtree second



Postorder(tree)

if tree is not NULL
 Postorder(Left(tree))
 Postorder(Right(tree))
 Visit Info(tree)

Visits leaves first (good for deletion)

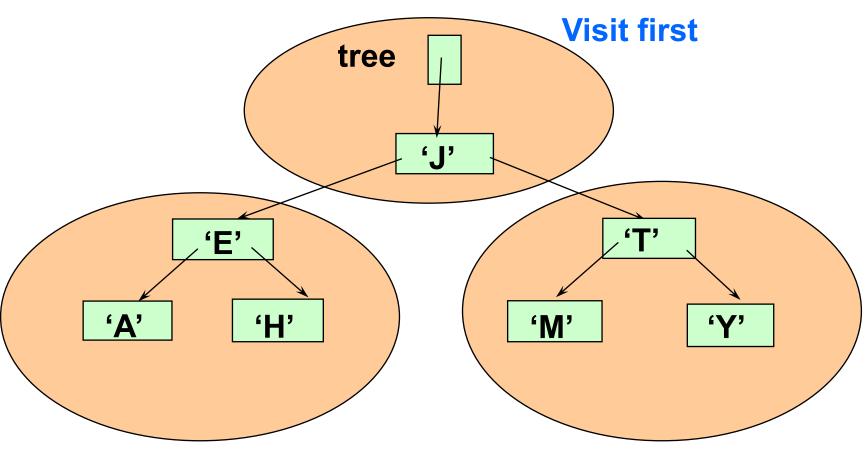


PostOrder Implementation

```
void PostOrder(TreeNode *tree,
 QueType& postQue)
 if(tree != NULL)
   PostOrder(tree->left, postQue);
   PostOrder(tree->right, postQue);
   postQue.Enqueue(tree->info);
```

Preorder Traversal

Preorder Traversal: JEAHTMY



Visit left subtree second

Visit right subtree last



Preorder(tree)

if tree is not NULL
 Visit Info(tree)
 Preorder(Left(tree))
 Preorder(Right(tree))

Useful with binary trees (not binary search trees)

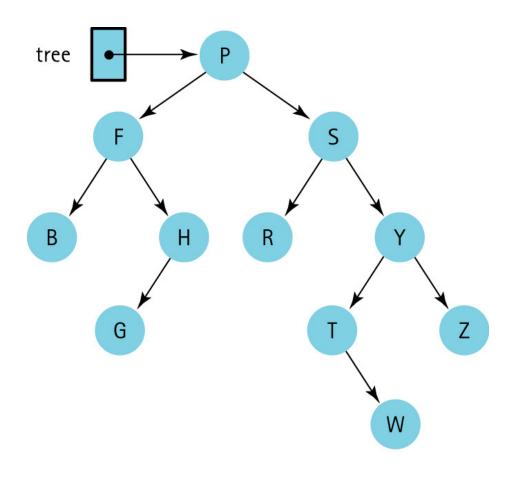


PreOrder Implementation

```
void PreOrder(TreeNode* tree,
   QueType& preQue)
{
   if(tree != NULL) {
      preQue.Enqueue(tree->info);
      PreOrder(tree->left, preQue);
      PreOrder(tree->right, preQue);
   }
}
```



Three Tree Traversals



Inorder: B F G H P R S T W Y Z Preorder: P F B H G S R Y T W Z Postorder: B G H F R W T Z Y S P



- The client program passes the ResetTree and GetNextItem functions a parameter indicating which of the three traversals to use
- For efficiency, ResetTree generates a queue of node contents in the indicated order
- GetNextItem processes the node contents from the appropriate queue: inQue, preQue, postQue.



Modification of Class TreeType

```
enum OrderType {PRE ORDER, IN ORDER,
  POST ORDER };
class TreeType {
  public:
   // same as before
  private:
    TreeNode* root;
    QueType preQue;
                        new private data
    QueType inQue;
    QueType postQue;
};
```



Code for ResetTree

```
void TreeType::ResetTree(OrderType order)
// Calls function to create a queue of the tree
// elements in the desired order.
  switch (order)
    case PRE ORDER : PreOrder(root, preQue);
                     break;
    case IN ORDER : InOrder(root, inQue);
                     break;
    case POST ORDER: PostOrder(root, postQue);
                     break;
```



Code for GetNextItem

```
void TreeType::GetNextItem(ItemType& item,
     OrderType order, bool& finished)
  finished = false;
  switch (order)
    case PRE ORDER : preQue.Dequeue(item);
                      if (preQue.IsEmpty())
                        finished = true;
                      break;
                    : inQue.Dequeue(item);
    case IN ORDER
                      if (inQue.IsEmpty())
                        finished = true;
                      break:
         POST ORDER: postQue.Dequeue(item);
    case
                      if (postQue.IsEmpty())
                        finished = true;
                      break;
```

Prototypes of Traversal Functions

```
void PreOrder(TreeNode*,
 QueType&);
void InOrder(TreeNode*,
 QueType&);
void PostOrder(TreeNode*,
 QueType&);
```



Iterative Versions

```
FindNode
Set nodePtr to tree
Set parentPtr to NULL
Set found to false
while more elements to search AND NOT found
  if item < Info(nodePtr)</pre>
      Set parentPtr to nodePtr
      Set nodePtr to Left(nodePtr)
  else if item > Info(nodePtr)
      Set parentPtr to nodePtr
      Set nodePtr to Right(nodePtr)
  else
      Set found to true
```

```
void FindNode(TreeNode* tree, ItemType item,
     TreeNode*& nodePtr, TreeNode*& parentPtr)
 nodePtr = tree;
 parentPtr = NULL;
 bool found = false;
 while (nodePtr != NULL && !found)
  { if (item < nodePtr->info)
     parentPtr = nodePtr;
     nodePtr = nodePtr->left;
   else if (item > nodePtr->info)
                                     Code for
     parentPtr = nodePtr;
                                     FindNode
     nodePtr = nodePtr->right;
   else found = true;
                                                 29
```

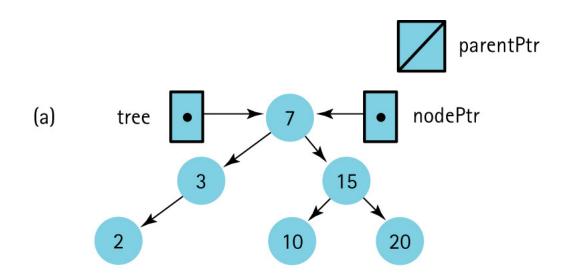


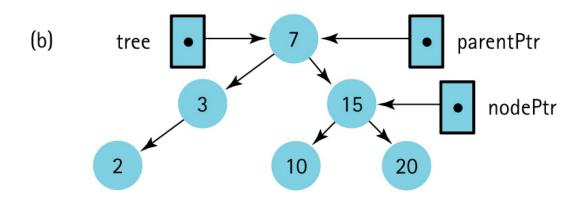
InsertItem

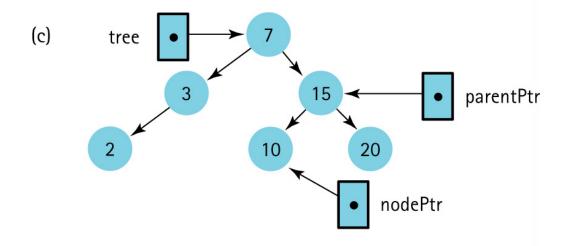
Create a node to contain the new item. Find the insertion place.

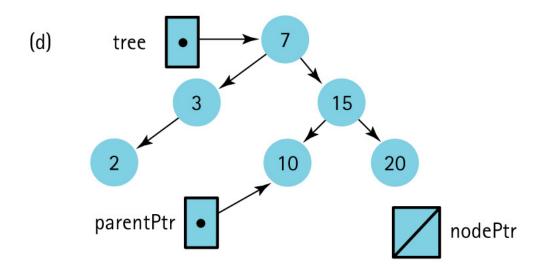
Attach new node.

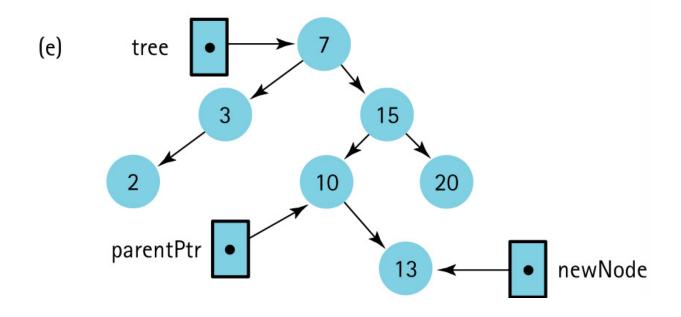
Find the insertion place FindNode(tree, item, nodePtr, parentPtr);













AttachNewNode

if item < Info(parentPtr)
 Set Left(parentPtr) to newNode
else
 Set Right(parentPtr) to newNode</pre>

What's wrong?



AttachNewNode(revised)

```
if parentPtr equals NULL
   Set tree to newNode
else if item < Info(parentPtr)
   Set Left(parentPtr) to newNode
else
   Set Right(parentPtr) to newNode</pre>
```



Code for InsertItem

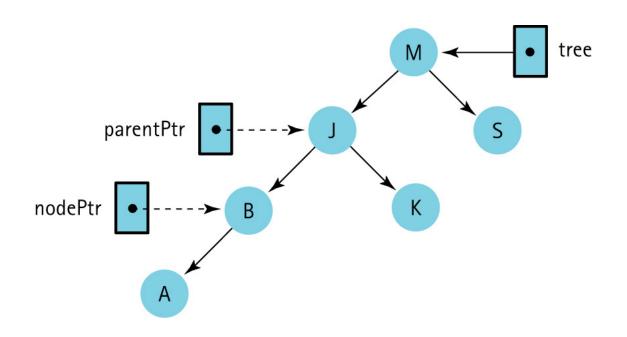
```
void TreeType::InsertItem(ItemType item)
  TreeNode* newNode;
  TreeNode* nodePtr;
  TreeNode* parentPtr;
  newNode = new TreeNode;
  newNode->info = item;
  newNode->left = NULL;
  newNode->right = NULL;
  FindNode(root, item, nodePtr, parentPtr);
  if (parentPtr == NULL)
    root = newNode;
  else if (item < parentPtr->info)
    parentPtr->left = newNode;
  else parentPtr->right = newNode;
```



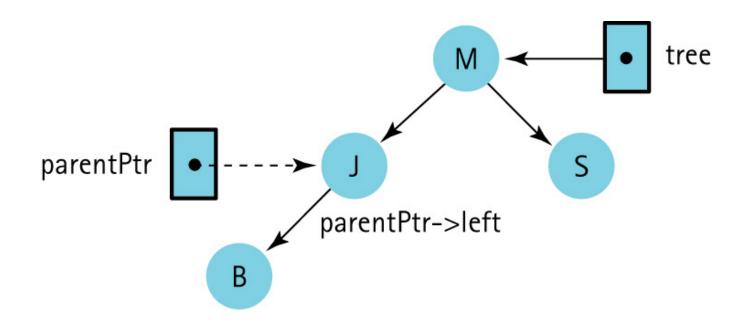
Code for DeleteItem

```
void TreeType::DeleteItem(ItemType item)
  TreeNode* nodePtr;
  TreeNode* parentPtr;
  FindNode (root, item, nodePtr, parentPtr);
  if (nodePtr == root)
    DeleteNode(root);
  else
    if (parentPtr->left == nodePtr)
      DeleteNode(parentPtr->left);
    else DeleteNode(parentPtr->right);
```

Pointers nodePtr and parentPtr Are External to the Tree



Pointer parentPtr is External to the Tree, but parentPtr-> left is an Actual Pointer in the Tree



Comparing Binary Search Trees to Linear Lists

Big-O Comparison			
Operation	Binary Search Tree	Array-based List	Linked List
Constructor	O(1)	O(1)	O(1)
Destructor	O(N)	O(1)	O(N)
IsFull	O(1)	O(1)	O(1)
IsEmpty	O(1)	O(1)	O(1)
RetrieveItem	O(logN)	O(logN)	O(N)
InsertItem	O(logN)	O(N)	O(N)
DeleteItem	O(logN)	O(N)	O(N)

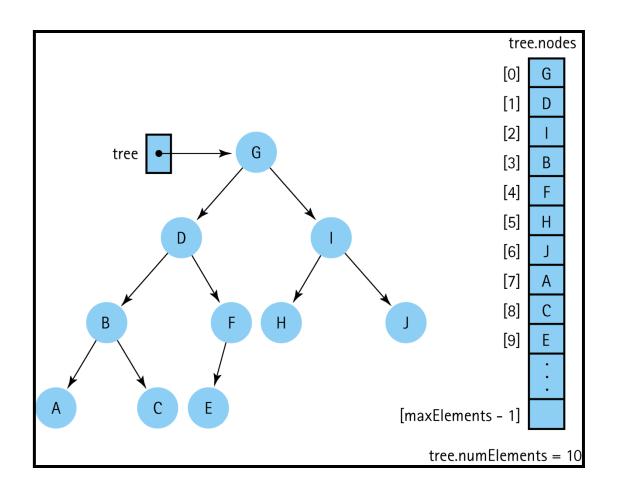


With Array Representation

- For any node tree.nodes[index]
 - □ its left child is in tree.nodes[index*2 + 1]
 - □ right child is in tree.nodes[index*2 + 2]
 - □ its parent is in tree.nodes[(index 1)/2].



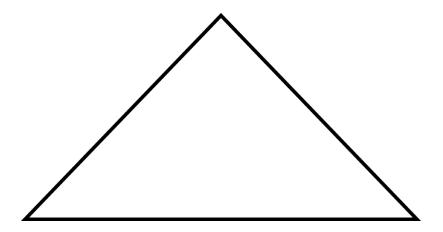
A Binary Tree and Its Array Representation





Definitions

Full Binary Tree: A binary tree in which all of the leaves are on the same level and every nonleaf node has two children

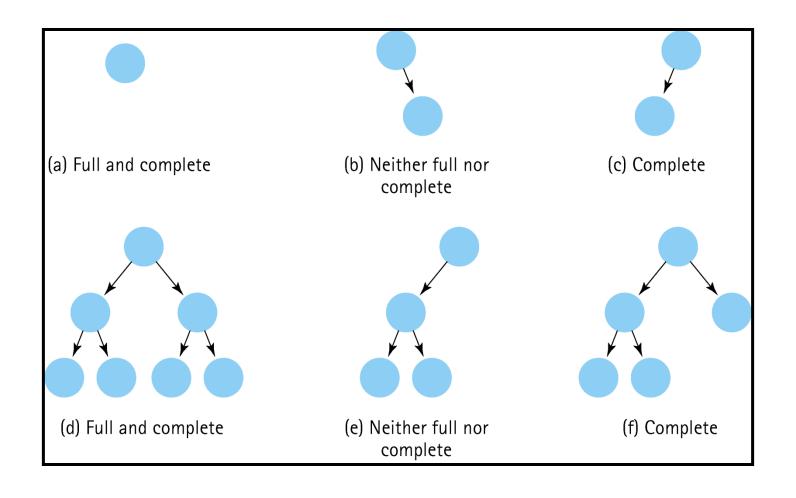




Definitions (cont.)

Complete Binary Tree: A binary tree that is either full or full through the nextto-last level, with the leaves on the last level as far to the left as possible

Examples of Different Types of Binary Trees





A Binary Search Tree Stored in an Array with Dummy Values

