

Queue

Queue is a specialized data storage structure (Abstract data type). Unlike, arrays access of elements in a Queue is restricted. It has two main operations **enqueue** and **dequeue**. Insertion in a queue is done using **enqueue** function and removal from a queue is done using **dequeue** function. An item can be inserted at the end ('rear') of the queue and removed from the front ('front') of the queue. It is therefore, also called First-In-First-Out (FIFO) list. Queue has five properties - **capacity** stands for the maximum number of elements Queue can hold, **size** stands for the current size of the Queue, **elements** is the array of elements, **front** is the index of first element (the index at which we remove the element) and **rear** is the index of last element (the index at which we insert the element).

Algorithm:

Queue structure is defined with fields **capacity**, **size**, ***elements** (pointer to the array of elements), **front** and **rear**.

Functions –

1. **createQueue** function– This function takes the maximum number of elements (**maxElements**) the Queue can hold as an argument, creates a Queue according to it and returns a pointer to the Queue. It initializes Queue **Q** using malloc function and its properties.
elements = (int *)malloc(sizeof(int)***maxElements**).
Q->size = 0, current size of the Queue **Q**.
Q->capacity = **maxElements**, maximum number of elements Queue **Q** can hold.
Q->front = 0
Q->rear = -1
2. **enqueue** function - This function takes the pointer to the top of the queue **Q** and the item (**element**) to be inserted as arguments. Check for the emptiness of queue
If **Q->size** is equal to **Q->capacity**, we cannot push an element into **Q** as there is no space for it.
Else, enqueue an element at the end of **Q**, increase its **size** by one. Increase the value of **Q->rear** to **Q->rear** + 1. As we fill the queue in circular fashion, if **Q->rear** is equal to **Q->capacity** make **Q->rear** = 0. Now, Insert the element in its rear side

Q->elements[Q->rear] = element
3. **dequeue** function - This function takes the pointer to the top of the stack **S** as an argument.
If **Q->size** is equal to zero, then it is empty. So, we cannot dequeue.
Else, remove an element which is equivalent to incrementing index of **front** by

one. Decrease the **size** by 1. As we fill elements in circular fashion, if **Q->front** is equal to **Q->capacity** make **Q->front=0**.

4. **front** function – This function takes the pointer to the top of the queue **Q** as an argument and returns the front element of the queue **Q**. It first checks if the queue is empty (**Q->size** is equal to zero). If it's not it returns the element which is at the front of the queue.

Q->elements[Q->front]

Property:

1. Each function runs in $O(1)$ time.
2. It has two basic implementations
 - Array-based implementation – It's simple and efficient but the maximum size of the queue is fixed.
 - Singly Linked List-based implementation – It's complicated but there is no limit on the queue size, it is subjected to the available memory.

Example:

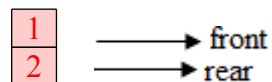
Create the queue **Q** using **createQueue** function, where **Q** is the pointer to the structure Queue. The maximum number of elements (**maxElements**) = 5.

Initially **Q->size** = 0, **Q->capacity** = 5, **Q->front** = 0, **Q->rear** = -1.

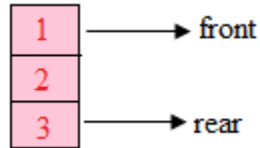
1. **enqueue(Q,1)**: Since, **Q->size** \neq **Q->capacity**. Increase its size by one and also **Q->rear** by 1. Now, **size** = 1 and **Q->rear** = 0. Since, **Q->rear** = **Q->capacity**, **Q->rear** remains unchanged. Enqueue 1 at the end of **Q**.



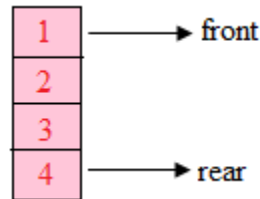
2. **enqueue(Q,2)**: Since, **Q->size** \neq **Q->capacity**. Increase its size by one and also **Q->rear** by 1. Now, **size** = 2 and **Q->rear** = 1. Since, **Q->rear** = **Q->capacity**, **Q->rear** remains unchanged. Enqueue 2 at the end of **Q**.



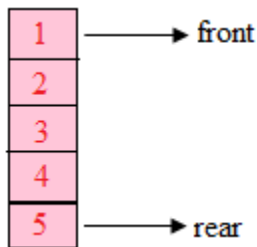
3. **enqueue(Q,3)**: Since, **Q->size** \neq **Q->capacity**. Increase its size by one and also **Q->rear** by 1. Now, **size** = 3 and **Q->rear** = 2. Since, **Q->rear** = **Q->capacity**, **Q->rear** remains unchanged. Enqueue 3 at the end of **Q**.



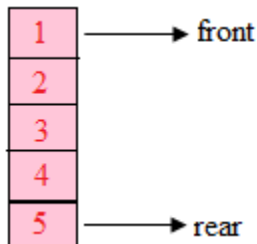
4. **enqueue(Q,4)**: Since, $Q \rightarrow \text{size} \neq Q \rightarrow \text{capacity}$. Increase its size by one and also $Q \rightarrow \text{rear}$ by 1. Now, $\text{size} = 4$ and $Q \rightarrow \text{rear} = 3$. Since, $Q \rightarrow \text{rear} = Q \rightarrow \text{capacity}$, $Q \rightarrow \text{rear}$ remains unchanged. Enqueue 4 at the end of Q.



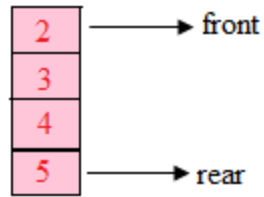
5. **front(Q)**: Since, $Q \rightarrow \text{size}(=4)$ is not equal to zero. It returns the element at the front end of the queue i.e. 1. Output = '1'.
6. **enqueue(Q,5)**: Since, $Q \rightarrow \text{size} \neq Q \rightarrow \text{capacity}$. Increase its size by one and also $Q \rightarrow \text{rear}$ by 1. Now, $\text{size} = 5$ and $Q \rightarrow \text{rear} = 4$. Since, $Q \rightarrow \text{rear} = Q \rightarrow \text{capacity}$, $Q \rightarrow \text{rear}$ remains unchanged. Enqueue 5 at the end of Q.



7. **enqueue(Q,6)**: Since, $Q \rightarrow \text{size} = Q \rightarrow \text{capacity}$, we cannot push an element as there is no space for it. $\text{size} = 5$ and $Q \rightarrow \text{rear} = 4$.



8. **dequeue(Q)**: Since, $Q \rightarrow \text{size}(=5)$ is not equal to zero. It removes the front most element i.e. 1 by simply incrementing index of **front** by one. Decrease the **size** by 1. Now, $\text{size} = 4$ and $Q \rightarrow \text{front} = 1$. Since, $Q \rightarrow \text{front}$ is not equal $Q \rightarrow \text{capacity}$, $Q \rightarrow \text{front}$ remains unchanged.



9. **front(Q)**: Since, $Q \rightarrow \text{size}(=4)$ is not equal to zero. It returns the element at the front end of the queue i.e. 2. Output = '2'.
10. **dequeue(Q)**: Since, $Q \rightarrow \text{size}(=4)$ is not equal to zero. It removes the front most element i.e. 1 by simply incrementing index of **front** by one. Decrease the **size** by 1. Now, **size** = 3 and $Q \rightarrow \text{front} = 2$. Since, $Q \rightarrow \text{front}$ is not equal $Q \rightarrow \text{capacity}$, $Q \rightarrow \text{front}$ remains unchanged.

