Basic Data Structures: Arrays and Linked Lists

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Data Structures http://bit.ly/algospecialization

Outline

long arr[] = new long[5];

long arr[5];

$$arr = [None] * 5$$

Definition

Array:

Contiguous area of memory

Definition

Array:

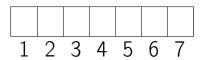
Contiguous area of memory consisting of equal-size elements

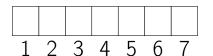


Definition

Array:

Contiguous area of memory consisting of equal-size elements indexed by contiguous integers.

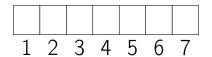




Constant-time access



Constant-time access array addr



```
Constant-time access array\_addr + elem\_size \times (
```

```
1 2 3 4 5 6 7
```

Constant-time access $array_addr + elem_size \times (i - first_index)$



(1, 1)			

	(3,4)	

	(3,4)	

$$(3-1) \times 6$$

	(3,4)	

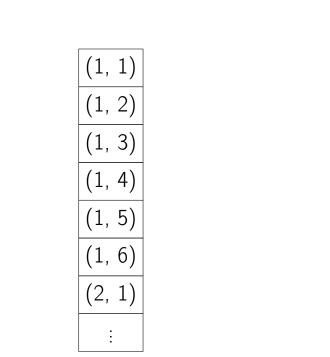
$$(3-1)\times 6+(4-1)$$

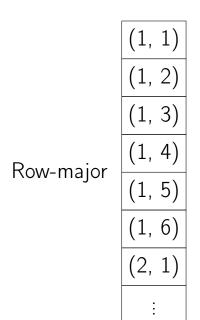
	(3,4)	

elem_size
$$\times$$
 ((3 - 1) \times 6 + (4 - 1))

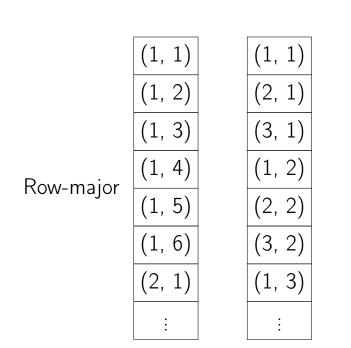
	(3,4)	

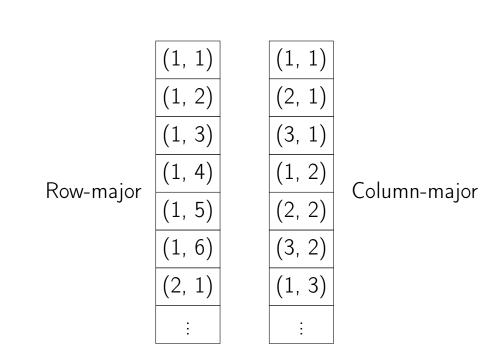
array_addr + elem_size
$$\times$$
 ((3 - 1) \times 6 + (4 - 1))











	Add	Remove
Beginning		
End		
Middle		

	Add	Remove
Beginning		
End		
Middle		

5 8 3 12

	Add	Remove
Beginning		
End	O(1)	
Middle		

5 8 3 12 4

	Add	Remove
Beginning		
End	O(1)	
Middle		

5 8 3 12 4

	Add	Remove
Beginning		
End	O(1)	O(1)
Middle		

5 8 3 12

	Add	Remove
Beginning		O(n)
End	O(1)	O(1)
Middle		

	Add	Remove
Beginning		O(n)
End	O(1)	O(1)
Middle		

	Add	Remove
Beginning		O(n)
End	O(1)	O(1)
Middle		

	Add	Remove
Beginning		O(n)
End	O(1)	O(1)
Middle		

	Add	Remove
Beginning	O(n)	O(n)
End	O(1)	O(1)
Middle		

	Add	Remove
Beginning		O(n)
	O(1)	O(1)
Middle	O(n)	O(n)

Summary

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Array: contiguous area of memory consisting of equal-size elements indexed by contiguous integers.

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- Array: contiguous area of memory consisting of equal-size elements indexed by contiguous integers.
- Constant-time access to any element.

Summary

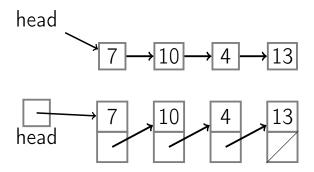
- Array: contiguous area of memory consisting of equal-size elements indexed by contiguous integers.
- Constant-time access to any element.
- Constant time to add/remove at the end.

Summary

- Array: contiguous area of memory consisting of equal-size elements indexed by contiguous integers.
- Constant-time access to any element.
- Constant time to add/remove at the end.
- Linear time to add/remove at an arbitrary location.

Outline

Singly-Linked List



Node contains:

- key
- next pointer

PushFront(Key) add to front

PushFront(Key) add to front
Key TopFront() return front item

PushFront(Key) add to front
Key TopFront() return front item
PopFront() remove front item

PushFront(Key)
Key TopFront()
PopFront()
PushBack(Key)

add to front return front item remove front item add to back also known as Append

<pre>PushFront(Key)</pre>	add to front
<pre>Key TopFront()</pre>	return front item
PopFront()	remove front item
PushBack(Key)	add to back
<pre>Key TopBack()</pre>	return back item

PushFront(Key)	add to front
<pre>Key TopFront()</pre>	return front item
PopFront()	remove front item
PushBack(Key)	add to back
<pre>Key TopBack()</pre>	return back item
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PushFront(Key)	add to front
<pre>Key TopFront()</pre>	return front item
<pre>PopFront()</pre>	remove front item
PushBack(Key)	add to back
<pre>Key TopBack()</pre>	return back item
PopBack()	remove back item
Boolean Find(Key)	is key in list?

<pre>PushFront(Key)</pre>	add to front
<pre>Key TopFront()</pre>	return front item
PopFront()	remove front item
PushBack(Key)	add to back
<pre>Key TopBack()</pre>	return back item
PopBack()	remove back item
Boolean Find(Key)	is key in list?
Erase(Key)	remove key from list

PushFront(Key)	add to front
<pre>Key TopFront()</pre>	return front item
<pre>PopFront()</pre>	remove front item
PushBack(Key)	add to back
<pre>Key TopBack()</pre>	return back item
PopBack()	remove back item
Boolean Find(Key)	is key in list?
Erase(Key)	remove key from list
Boolean Empty()	empty list?

PushFront(Key)

Key TopFront()

PopFront()

add to front

return front item

remove front item

PushBack(Key)	add to back
Key TopBack()	return back item
PopBack()	remove back item
Boolean Find(Key)	is key in list?
Erase(Key)	remove key from list
Boolean Empty()	empty list?
AddBefore(Node, Key)	adds key before node

add to front PushFront(Key) Key TopFront() return front item PopFront()

PushBack(Key) Key TopBack() PopBack()

Boolean Find(Key) Erase(Key) Boolean Empty()

remove front item add to back

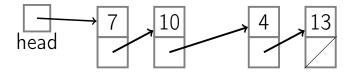
return back item remove back item

is key in list?

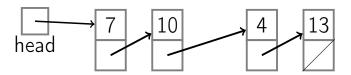
remove key from list

empty list? adds key before node

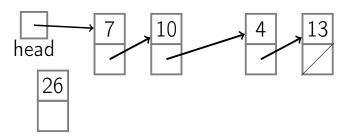
AddBefore(Node, Key) AddAfter(Node, Key) adds key after node



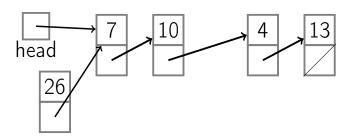
PushFront



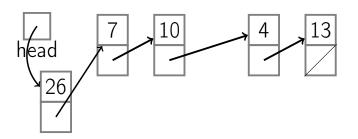
PushFront



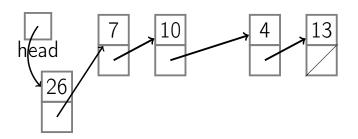
PushFront



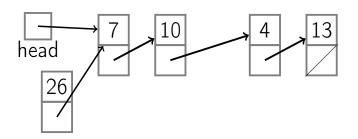
PushFront O(1)



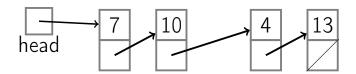
PopFront



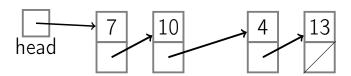
PopFront

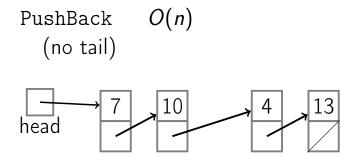


PopFront O(1)

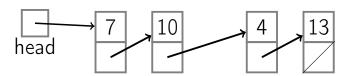


PushBack (no tail)

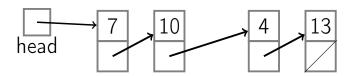


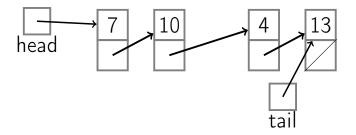


PopBack (no tail)

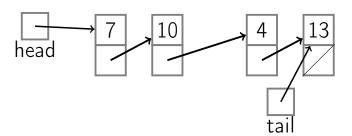


PopBack O(n) (no tail)

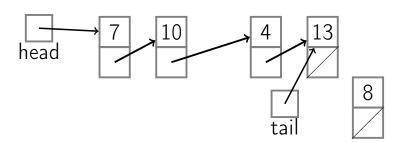




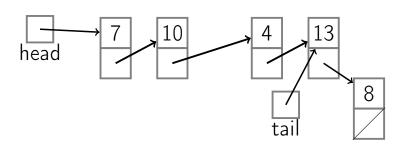
PushBack (with tail)



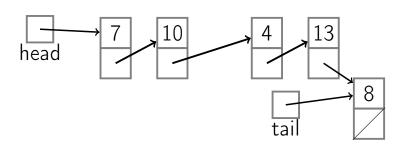
PushBack (with tail)



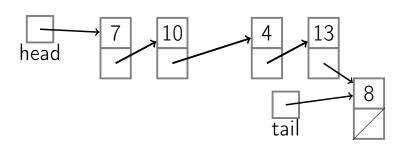
PushBack (with tail)



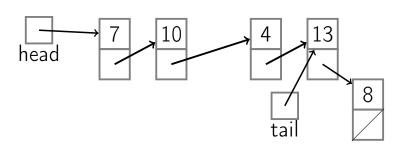
PushBack O(1) (with tail)



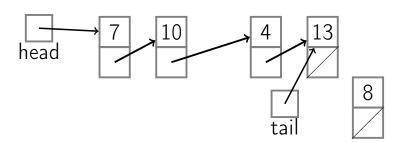
PopBack (with tail)



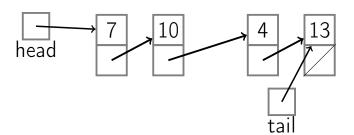
PopBack (with tail)



PopBack (with tail)



PopBack O(n) (with tail)



PushFront(key)

```
node ←new node
node.key ← key
node.next ← head
head ← node
if tail = nil:
tail ← head
```

```
PopFront()
if head = nil:
  ERROR: empty list
head \leftarrow head.next
if head = nil:
  tail \leftarrow nil
```

```
node \leftarrow new node

node.key \leftarrow key

node.next = nil
```

```
node ←new node
node.key ← key
node.next =nil
if tail = nil:
head ← tail ← node
```

```
node \leftarrow new node
node.key \leftarrow key
node.next = nil
if tail = nil:
   head \leftarrow tail \leftarrow node
else:
   tail.next \leftarrow node
   tail ← node
```

```
if head = nil: ERROR: empty list
```

```
if head = nil: ERROR: empty list
if head = tail:
  head ← tail ← nil
```

```
if head = nil: ERROR: empty list
if head = tail:
  head \leftarrow tail \leftarrow nil
else:
  p \leftarrow head
  while p.next.next \neq nil:
     p \leftarrow p.next
```

```
if head = nil: ERROR: empty list
if head = tail:
  head \leftarrow tail \leftarrow nil
else:
  p \leftarrow head
  while p.next.next \neq nil:
     p \leftarrow p.next
  p.next \leftarrow nil; tail \leftarrow p
```

AddAfter(node, key)

```
node2 ←new node
node2.key ← key
node2.next = node.next
node.next = node2
if tail = node:
tail ← node2
```

Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	

Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	

Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	
PopFront()	O(1)	
'		

PushFront(Key)	O(1)		
<pre>TopFront()</pre>	O(1)		
<pre>PopFront()</pre>	O(1)		
PushBack(Key)	O(n)	O(1)	

Singly-Linked List | no tail with tail

PushFront(Key)	O(1)		
<pre>TopFront()</pre>	O(1)		
<pre>PopFront()</pre>	O(1)		
PushBack(Key)	O(n)	O(1)	
TopBack()	O(n)	O(1)	

Singly-Linked List | no tail with tail

PushFront(Key)	O(1)		_
TopFront()	O(1)		
PopFront()	O(1)		
PushBack(Key)	O(n)	O(1)	
TopBack()	O(n)	O(1)	
PopBack()	O(n)		
·			

Singly-Linked List | no tail with tail

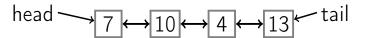
Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	
PopFront()	O(1)	
PushBack(Key)	O(n)	O(1)
TopBack()	O(n)	O(1)
PopBack()	O(n)	
Find(Key)	O(n)	

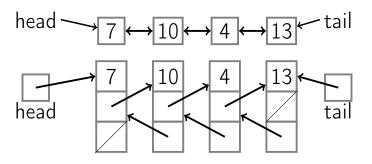
Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	
PopFront()	O(1)	
PushBack(Key)	O(n)	O(1)
TopBack()	O(n)	O(1)
PopBack()	O(n)	
Find(Key)	O(n)	
Erase(Key)	O(n)	

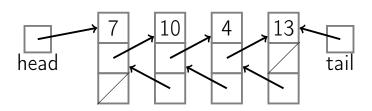
Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	
PopFront()	O(1)	
PushBack(Key)	O(n)	O(1)
TopBack()	O(n)	O(1)
PopBack()	O(n)	
Find(Key)	O(n)	
Erase(Key)	O(n)	
Empty()	O(1)	
·		

Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
<pre>TopFront()</pre>	O(1)	
<pre>PopFront()</pre>	O(1)	
PushBack(Key)	O(n)	O(1)
TopBack()	O(n)	O(1)
PopBack()	O(n)	
Find(Key)	O(n)	
Erase(Key)	O(n)	
<pre>Empty()</pre>	O(1)	
AddBefore(Node, Key)	O(n)	

Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	
PopFront()	O(1)	
PushBack(Key)	O(n)	O(1)
TopBack()	O(n)	O(1)
PopBack()	O(n)	
Find(Key)	O(n)	
Erase(Key)	O(n)	
Empty()	O(1)	
AddBefore(Node, Key)	O(n)	
AddAfter(Node, Key)	O(1)	

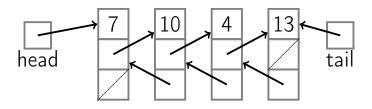


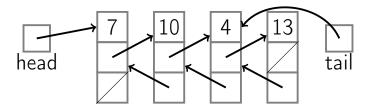


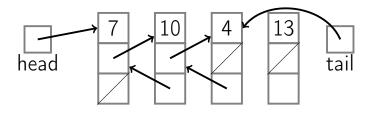


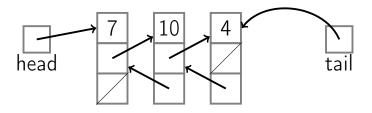
Node contains:

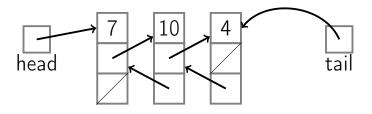
- key
- next pointer
- prev pointer











PopBack O(1)

```
node \leftarrow new node
node.key \leftarrow key; node.next = nil
```

```
node ←new node
node.key ← key; node.next =nil
if tail = nil:
  head ← tail ← node
  node.prev ←nil
```

```
node \leftarrow new node
node.key \leftarrow key; node.next = nil
if tail = nil:
   head \leftarrow tail \leftarrow node
   node.prev \leftarrow nil
else:
   tail.next \leftarrow node
   node.prev \leftarrow tail
   tail ← node
```

```
PopBack()
```

```
if head = nil: ERROR: empty list
```

```
if head = nil: ERROR: empty list
if head = tail:
  head ← tail ← nil
```

```
if head = nil: ERROR: empty list
if head = tail:
  head ← tail ← nil
else:
  tail ← tail.prev
  tail.next ← nil
```

AddAfter(node, key)

```
node2 \leftarrow new node
node2.key \leftarrow key
node2.next \leftarrow node.next
node2.prev \leftarrow node
node.next \leftarrow node2
if node2.next \neq nil:
```

 $node2.next.prev \leftarrow node2$ if tail = node:

 $tail \leftarrow node2$

AddBefore(node, key)

```
node2 \leftarrow new node
node2.key \leftarrow key
node2.next \leftarrow node
node2.prev \leftarrow node.prev
node.prev \leftarrow node2
if node2.prev \neq nil:
```

 $node2.prev.next \leftarrow node2$ if head = node:

nead = node: $head \leftarrow node$?

Singly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	
PopFront()	O(1)	
PushBack(Key)	O(n)	O(1)
TopBack()	O(n)	O(1)
PopBack()	O(n)	
Find(Key)	O(n)	
Erase(Key)	O(n)	
Empty()	O(1)	
AddBefore(Node, Key)	O(n)	
AddAfter(Node, Key)	O(1)	

Doubly-Linked List	no tail	with tail
PushFront(Key)	O(1)	
TopFront()	O(1)	
PopFront()	O(1)	
PushBack(Key)	O(n)	O(1)
TopBack()	O(n)	O(1)
PopBack()	O(n) O(1)	
Find(Key)	O(n)	
Erase(Key)	O(n)	
Empty()	O(1)	
AddBefore(Node, Key)	O(n) O(1)	
AddAfter(Node, Key)	O(1)	

Constant time to insert at or remove from the front.

- Constant time to insert at or remove from the front.
- With tail and doubly-linked, constant time to insert at or remove from the back.

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- With tail and doubly-linked, constant time to insert at or remove from the back.
- O(n) time to find arbitrary element.

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- With tail and doubly-linked, constant time to insert at or remove from the back.
- O(n) time to find arbitrary element.
- List elements need not be contiguous.

- Constant time to insert at or remove from the front.
- With tail and doubly-linked, constant time to insert at or remove from the back.
- O(n) time to find arbitrary element.
- List elements need not be contiguous.
- With doubly-linked list, constant time to insert between nodes or remove a node.