(916) The following information has been gathered from a random Sample of apartment renters in a city. We have information of rent in (000 Rs per month) based on the size of apartment, (number of rooms) and the distance from downtown (in KM).

Rent (ODO RS) 16 20 25 22 4 6 3 4 Number of rooms Distance from downtown 8 4 10

a. Obtain the multiple regression models that best relate these Variables

b. Interpret the obtained regression coefficients.

C. If someone is looking for a two bed apartment 8 km from down town, What rent should he expect to pay?

d. Obtain residuals

C. Calculate standard error of dist estimate

f. Test the significance of regression Coefficient at sy, level of Significance

g. Test overall significance of regression equation at 5% level

of Significance.

1) Find out dependent and independent Variable. Here, Rent 95 dependent (say y), Number of rooms and Distance from downtown (say X, and X2) respectively independent

2) Regression Equation of you of, and X2 Where, bo, b, & bz are parameters To fit, y = bo+b12/2+b22/2 of the three Variable

· = 1 = 1 bo + b, & X, +b2 & X2

· EyX, = bo Ex, +b, Ex, + b2 Ex, X2

•  $\xi y \chi_2 = b_0 \xi \chi_2 + b_1 \xi \chi_1 \chi_2 + b_2 \xi \chi_2^2$ 

3) use cramer's rule for calculating the value of parameters 90,91 &92

- 4) Residual Calculation

  R: = Observed rent predicted rent
- 5) Standard Error Calculation,  $Se = \sqrt{\frac{SSE}{N-K-1}} \quad \text{Where, } SSE = \mathcal{Z}(\chi_1 \overline{\chi}_1)^2$   $= \mathcal{Z}\chi_1^2 a \mathcal{Z}\chi_1 b_2 \mathcal{Z}\chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_1 \chi_1 \chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1 \chi_1 \chi_1 \chi_2^2 b_3 \mathcal{Z}\chi_1$
- 6) Test statistic calculation,

  t = bi
  Sb; Lihere, b; = Sample regression coefficient
  Sb; = Standard error of regression Coefficient
- 3) Test of Overall significance of the Regression Coefficients
- 8) Calculate, test statistic

  F = MSR Where, MSR = mean sum of square due to regression

  MSE = Mean Sum of square due to error
  - of Significance then regression model is Significant.

Residuals:			1	<i>-</i>	6
1	<b>9</b>	3	4	5	- 4 4-
<u>.</u>		2 07/2	0.0519	-1.8603	0.8428

#### Coefficients:

Intercepts	Estimate Std. 27.3954	Error 1 5.6128	t.Value 4.881	pr(>1t1)
hoofrooms distance	-0.9414 -0.4141	1.5725	-0.599 -0.786	0.5916

Residual Standard error: 3.348 on 3 degree of free dom Multiple R-squared: 0.4334, Adjusted R-squared: 0.05569 F-Statistic: 1.147 on 2 and 3 Df, p-value: 0.4265 11 predicted rent 22.1998

#### Conclusion:

- a. The multiple regression model obtained from the data is: Rent = 27.8954 - 0.9414 No. of rooms - 0.4141 Distance  $Y = 27.3954 - 0.9414 \chi_1 - 0.4141 \chi_2$
- b. Interpretation of Coefficients:
  - · The intercept of 27.3954 represents the expected rent When the number of rooms and distance from down town are both zero.
  - · For each additional room, the rent decreases by approximately 0.9414 RS with constant distance from downtown.
  - · For each additional Kilometer away from downtown, the vent decreases by approximately 0.4141 Rs with Constant number of rooms.
- C. If Someone is looking for a two-bedroom agartment 8km from downtown, the predicted rent would be approximately 22.1998 RS.

- d. Residuals

  1 2 3 4 5 6

  -4.3168 2.3942 2.0852 0.8549 -1.8603 0.8428
- e. The Standard error of estimate is approximately 3.348 Rs.
- f. Testing the significance of regression coefficients:
  - The Coefficients are significant at the 5% level, as indicated by their p-values being greater than 0.05.
- g. Testing the overall significance of the regression equation:
  - The p-value for the F-Statistic is 0.4265, indicating that the regression equation as a whole is that statistically significant at the 5.10 level. (p-value =0.4265 > x=0.05).

Adeveloper of food for pig would like to determine what relationship exists among the age of a pig when it starts receiving a newly developed food supplement, the initial weight of the pig and the amount of weight it gains in a week period with the food supplement. The following information is the result of study of eight

Initial Weight (pounds)	39	52	49	4-6	61	36	28	578
Initial age (weeks)	8	7	6	11	8	7	9	5
Weight gain		7	6	9	10	6	4	5

. 9. Determine multiple correlation zoefficient and partial Correlation coefficients of Lependent Vargable with independent variables.

b. Determine multiple coefficient of determination and interpret

C. Determine adjusted multiple coefficient of determination

## > Working Steps

1. Multiple Correlation Coefficient

It is lies between 0 and 1 i.e.  $0 < R_{1.23} \le 1$ ,  $0 \le R_{2.13} \le 1$ ,  $0 \le R_{3.12} \le 1$ 

· It is not less than Simple Correlation Rs. 23 = \$12, 813, 823

Where,
$$R_{1.23} = \sqrt{\frac{\gamma_{12} + \gamma_{13} - 2\gamma_{12}\gamma_{13}\gamma_{13}}{1 - \gamma_{23}^2}}$$

• If R1.23 = 0 then Y12=0, Y13 = 0 • R1.23 = R1.32

2. Partial Correlation Coefficients Let, three variables X1, X2 & X3 then, partial Correlation Coefficients bet X1 and X2 keeping X3 constant is dentated by 812.3.

$$\gamma_{12.3} = \frac{\gamma_{12} - \gamma_{13}\gamma_{23}}{\sqrt{1 - \gamma_{13}^2} \cdot \sqrt{1 - \gamma_{23}^2}}$$

Same way,  $\gamma_{13.2} = \frac{\gamma_{13} - \gamma_{12}\gamma_{32}}{\sqrt{1 - \gamma_{13}^2} \cdot \sqrt{1 - \gamma_{32}^2}} , \quad \gamma_{23.1} = \frac{\gamma_{23} - \gamma_{21}\gamma_{31}}{\sqrt{1 - \gamma_{23}^2} \cdot \sqrt{1 - \gamma_{31}^2}}$ 

Calculate,

$$R_{1.23} = \left(\frac{\gamma_{12}^2 + \gamma_{13}^2 - 2\gamma_{12}\gamma_{13}\gamma_{23}}{1 - \gamma_{23}^2}\right)^2$$

$$= \frac{\gamma_{12}^2 + \gamma_{13}^2 - 2\gamma_{12}\gamma_{13}\gamma_{23}}{1 - \gamma_{23}^2}$$
in the same way
$$R_{2.13}^2 \text{ and } R_{3.12}^2$$

4. Calculate adjusted multiple coefficien of determination 
$$R^2$$
 adjusted  $(\overline{R}_2) = 1 - \frac{n-1}{(n-k-1)}[1-R^2]$ 

Where, n=no. of pair of observations k=no. of independent variables

Moutput

Coefficients:

C5 -1,) 101	Estimate std.	Error	t-value	Pr (>1t1)
(Intercept	) -5.50561	3.77392	-1.459	0.2044
initialweight	0.13775	0.04926	2.797	0.0387
initialage	0.79269	0.29630	2.675	0.0441

Multiple R-Squared: 0.6865, Adjusted R-Squared: 0.561 //sqrt(0.6865) 0.828553

\$ estimate	weightgain	initial weight	initialage
Weightgain	1.0000000	0.7810314	0.7672784
initialweight	0-7810314	1.0000000	-0.7470585
initialage	0.7672784	-0.7470585	1.0000000

- a. Multiple Correlation Coefficient and partial Correlation Coefficient:
  - Multiple Correlation Coefficient - Correlation beth dependent variable (weight gain) and all independent variables (initial weight and initial age).
    - The correlation coefficient beth weight gain and initial weight is 0.781, and between weight gain and initial age is 0.767.

· Partial correlation coefficient

- The partial correlation Coefficient between wight gain and initial weight, a controlling for initial age is 0.781.

Similarly, the partial correlation coefficient between weight gain and initial age, controlling for initial weight is 0.767.

b. Multiple Coefficient Determination (R2) and interpretation:

- of the Variance in weight gain can be explained by the linear relationship with initial weight and initial age.
- C. Adjusted multiple Coefficient of Letermination
  - The adjusted Radi = 0.561

    This indicates that approximately 56.1% of the Narrance in weight gain can be explained by the linear relationship with initial weight and initial age, adjusting for the number of predictors and the Sample Size.

Q18) let A, H,D and L represents A (er, HP, Dell and Lenovo laptop and following information represents their operating time in hours before Charge is required.

carryout analysis of the design at 1% level of significance.

1. Find out which design of experiment and calculate

-## is CRD design of experiment

so, calculate treatment (t)=4 and Replication (r)=6

(A,H,D,L)

2. Mathematical Model

Yij = Il + Ti + eij

Where, i=1,2,---,t; j=1,2,--
Yij = Observation or Yield due to ith treatment and jth replication

Il = General mean

Ti = Effect due to ith treatment

eij = Error due to ith treatment and jth replication

eij = Error due to ith treatment and jth replication

3. Calculate, TSS = SST + SSEWhere,  $TSS = \underbrace{5}_{i} \underbrace{(y_{ij} - y_{..})^{2}}_{\text{Where}}$   $TSS = \underbrace{5}_{i} \underbrace{(y_{ij} - y_{..})^{2}}_{\text{SST}}$   $SST = \underbrace{5}_{i} \underbrace{(y_{ij} - y_{..})^{2}}_{\text{SST}}$   $SST = \underbrace{5}_{i} \underbrace{(y_{ij} - y_{i..})^{2}}_{\text{SST}}$   $SST = \underbrace{5}_{i} \underbrace{(y_{ij} - y_{i..})^{2}}_{\text{SST}}$  4. ANONA Table

SV Treatment t	Table  f SS -1 SST  (r-1) SSE  rt-1 TSS	$MS = \frac{SST}{\xi-1}$ $MSE = \frac{SSE}{\xi(r-1)}$	Fcal FT = MST MSE	Ftab Edt-1, t(r-1)).
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5. Check F-value with a Corresponding P-value, if p-value > than < level of significance then Accept Ho. Else Reject.

# 11 Output

Df Sum sq Mean Sq F. Value Pr(>F). Laptop 3 2.308 0.7694 1.197 0.336 Residuals 20 12.857 0.6428

Here, from the above result,

- The design used in the analysis is a Completely Randomized Design (CRD), as laptops of different brands were randomly assigned to the experimental unit without any specific blocking or grouping criteria.
- The value of F is 1.197 with a corresponding p-value is 0.336. Since, the p-value > &=0.01.

  So, Accept Ho at &=0.01.

- Problem to Test

Ho: Design is insignificant Hy: Design is Significant

### Conclusion:

The design is insignificant.

919) Let A, H, D and L represents A cer, HP, Dell and Lenovo laptop and following information represents their operating time in hours before charge is required.

Carryout analysis of the design at 1% level of significance.

working Steps

1. Find out that Which design of experiment is it

- If design is RBD then Calculate treatment (t)=4 and Block(b)=6

(A,H,D,L)

2. Mathematical Model Yij = U+Ti+Bj+ejj

Jij = Yield or observation due to ith freatment and jth block.

H = General Mean

Ti = Effect due to ith treatment

Bj = Effect due to jth block

eij= Error due to ith treatment and ith block

3. Calculate,

$$TSS = SST + SSR + SSE$$
Where, 
$$TSS = \frac{5}{7} \frac{5}{7} \frac{1}{7} - \frac{6^{2}}{7}$$

$$SST = \frac{5}{7} \frac{5}{7} \frac{1}{7} - \frac{6^{2}}{7}$$

$$SSB = \frac{5}{7} \frac{7}{12} - \frac{6^{2}}{7}$$

$$SSE = 7SS - SST - SSB$$

5. Check For value and For value with a Corresponding p-value if p-value > & level of significance than Accept HoT and HoB. Otherwise Reject.

### loutput

laptop 3 1.015 0.3382 0.945 0.44

Block 5 1.954 0.3908 1.092 0.405

Residuals 15 5.368 0.3579

-> problem to Test

HoT: Treatment of Lesign is insignificant HIT: Treatment of design is significant

Hob: Block of design is insignificant H1B: Block of design is significant

• The F value of treatment is 0.945 with a corresponding P-value is 0.44. Since, P-value = 0.44 > x=0.01 Accept HoT at x=0.01.

The Fvalue of Block is 1.092 with a Corresponding p-value is 0.405, since, p-value=0.405 > x=0.01

Accept Hob at x=0.01

Hence, in

Treatment of design is significant.

Block of design is insignificant.

(The design used in this analysis is a Randomized Block Design (RBD), where laptops are grouped into blocks and treatments (laptop brands) are randomly assigned within each block.)

Q20) Let A, H, D and L represents Acer, HP, Dell and Lenovo laptop and following information represents their operating time in hours before Charge is required.

Carryout analysis of the design at 5%. level of Significance.

working steps

1. Find out which design of experiment is it.

- If design is LSD then calculate, treatment (t) = (4), row = 4, column = 4 (A,H,D,2)

2. Mathematical Model

3. Calculate,

Where, 
$$TSS = \frac{2}{i.j.} \frac{y_{ijk}}{N} - \frac{G^2}{N}$$

$$SSR = \frac{2}{i.j.} \frac{T_{i...}^2}{m} - \frac{G^2}{N}$$

$$SSC = \frac{2}{i.j.} \frac{T_{i...}^2}{m} - \frac{G^2}{N}$$

$$SST = \frac{2}{i.j.} \frac{T_{i...}^2}{m} - \frac{G^2}{N}$$

$$SSE = TSS - SSR - SSC - SST$$

Table 4. ANOVA -cal MS 52 MSR = SSR/m-1 FR=MSR/MSE df SV SSR FC=MSC/MSE msc=ssc/m-1 m-1Row FT = MST/MSE SSC m-1 MST=SST/m-1 Column SST m-1 Treatment MSE=SSE/(m-1)(m-2) SSE (m-1)(m-2)ESSOR Total  $m^2-1$ TSS Ftab

Ftab Fa [m-1, (m-1)(m-2)]

5. Check Fy value, an Fy value, Fc value with a Corresponding P-value, if p-value > x-level of Significance then Accept Hot, HorsHoc. Reject otherwise.

// Output pr(>F) value Mean Se Sum Sq Df 0.288 1.588 1.620 0.5400 laptop 3. 7.350 0.4517 1.328 1.355 Low 0-203 0.7117 2.093 2.135 Column 0.3400 2.040 Residuals .6

Problem To Test

HoT: Treatment of design is insignificant

HIT: Treatment of design is significant

Hop: Yow of design is insignificant

Hop: Yow of design is significant

Hoc: Column of design is insignificant

Hoc: Column of design is Significant

Hoc: Column of design is Significant

The fivalue of treatment is 1.588 with a corresponding p-value is 0.288. Since, p-value = 0.288 > d=0.05.

Accept HoT at d=0.05 level of significance.

- The F-value of Row is 1.328 with a corresponding P-value is 0.350. Since, p-value > <=0.05.

  A CCEPT HOR at <=0.05 level of significance.
- The F-Value of Column is 9.093 with a Corresponding P-value is 0.203. Since, P-value  $> \alpha = 0.05$ . A Ccept HoC at  $\alpha = 0.05$  level of significance.

Hence,

Treatment of design is insignificant. Row of design is insignificant. Column of design is insignificant.

[ The design used in this analysis is an Into Latin Square Design (LSD), with laptops grouped into blocks (row and column), and treatments (laptop brands) assigned within each block.]