

Assignment

Date: (Sunday)
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1. If the data $x^7 + x^6 + x^5 + x + 1$ is transmitted using divisor $x^3 + 1$, find the CRC for the transmitted data.
2. Find the hamming code for the data 1011100101. If the 8th bit from right is corrupted in the hamming code, show how receive detects an error in the given position.
3. Find the Checksum for data 101010001100110001011100.

Q1) If the data $x^7 + x^6 + x^5 + x + 1$ is transmitted using divisor $x^3 + 1$, find the CRC for the transmitted data.

⇒ Soln,

Divisor : 1001

⇒ $4 - 1 = 3$

Data : 11100011

Sender

$$\begin{array}{r}
 1001 \overline{) 11100011000} \\
 \underline{\oplus 1001} \\
 01110 \\
 \underline{\oplus 1001} \\
 01110 \\
 \underline{\oplus 1001} \\
 01111 \\
 \underline{1001} \\
 0110
 \end{array}$$

$$1001 \overline{) 11100011000}$$

$$01101$$

$$\oplus 1001$$

$$01000$$

$$\oplus 1001$$

$$000100$$

CRC.

Transmitted Data $\rightarrow 11100011100$

Receiver

$$1001 \overline{) 11100011100}$$

$$\oplus 1001$$

$$01110$$

$$\oplus 1001$$

$$01110$$

$$\oplus 1001$$

$$01111$$

$$\oplus 1001$$

$$01101$$

$$\oplus 1001$$

$$01001$$

$$\oplus 1001$$

$$000000$$

Here, remainder is 0

Therefore,

There isn't corrupt in Data. Data is same as sender's data while receiving.

Q2) Find the CheckSum for the data 101010001100
110001011100

⇒ Soln

Sender

10101000

11001100

+ 01011100

Checksum: 11010001

1's Complement of checksum:

00101110

Transmitted Data: 11010001 00101110

Receiver

11010001

+ 00101110

Checksum: 11111111

Complement of checksum: 00000000

Here, Receiver side complement of checksum is zero(0)
So, the data is not corrupted.

(8-bits)

① 10101000

+ 11001100

01110100

+ 1

01110101

+ 01011100

11010001

Q3) Find the hamming code for the data 1011100101. If the 8th bit from right is corrupted in the hamming code, show how receive detects an error in the given position.

(Using Even parity)

Soln

Data : 1011100101

1 0 1 1 1 0 r_8 0 1 0 r_4 1 r_2 r_1

For r_1 : $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$
1 0 1 1 1 0 r_8 0 1 0 r_4 1 r_2 r_1

r_1 : 0 1 0 0 0 1 $\xrightarrow{\text{parity}}$ 0

For r_2 : $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$
1 0 1 1 1 0 r_8 0 1 0 r_4 1 r_2 r_1

r_2 : 1 1 1 0 1 1 $\xrightarrow{\text{parity}}$ 1

For r_4 : $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$
1 0 1 1 1 0 r_8 0 1 0 r_4 1 r_2 r_1

r_4 : 1 0 1 0 1 0 $\xrightarrow{\text{parity}}$ 1

For r_8 : $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$
1 0 1 1 1 0 r_8 0 1 0 r_4 1 r_2 r_1

r_8 : 1 0 1 1 1 0 $\xrightarrow{\text{parity}}$ 0

$$2^r \geq m+r+1$$

$$2^4 \geq 10+4+1$$

$$16 \geq 15 \checkmark$$

r_1, r_2, r_4, r_8

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Transmitted Data: (Hamming Code)

1 0 1 1 1 0 0 0 1 0 1 1 1 0



Now, If the 8th bit from right is corrupted hamming Code ;

1 0 1 1 1 0 0 0 1 0 1 1 1 0



Receiver

Corrupted Hamming Code → 1 0 1 1 1 0 0 0 1 0 1 1 1 0

Finding Parity bit of r_1, r_2, r_4 & r_8 :

$$r_1 : 0100010 \rightarrow 0$$

$$r_2 : 1110111 \rightarrow 0$$

$$r_4 : 1010101 \rightarrow 0$$

$$r_8 : 1011101 \rightarrow 1$$

$$r_8 r_4 r_2 r_1 : 1000 \Rightarrow 8$$

There is corrupted data in the 8th place