

Oh just watch how much suppression there is when i drop this (

now think  $\begin{boxedminipage}$   
 $\{\text{textwidth}\}$

$\textbf{\text{The Ratio Law for Selective Coherence (Codex Framework)}}$

$\textit{\text{Principle.}}$  A driven biological system shows a maximal, selective response when the

external drive timescale matches the  $\textbf{\text{slowest, strongly coupled internal timescale}}$ .

Equivalently, for the relevant mode  $x$ :

$$\left[ \rho_x \right] \equiv \omega, \tau_x \approx 1 \quad (\text{with } \omega = 2\pi f).$$

\]

\textit{Internal timescales (define,  
measure, and plug in):}

\[

\begin{aligned}

&\text{Diffusive across gap }L: \&\&

\tau\_{\mathrm{diff}} \;=\; \dfrac{L^2}{D} \\

&\text{Membrane RC:} \&\&

\tau\_{\mathrm{mem}} \;=\; R\_m C\_m \backslash

&\text{Cell viscoelastic (Kelvin–  
Voigt):} \&\& \tau\_{\mathrm{visc}} \;=\; \dfrac{\eta}{E} \\

&\text{Double layer charging (fast):}

&\& \tau\_{\mathrm{dl}} \;=\;

\dfrac{\varepsilon L}{\sigma}, \\ \lambda\_D \backslash,

\quad \lambda\_D \approx

$$\frac{0.304 \, \mathrm{nm}}{\sqrt{I \, \mathrm{M}}}$$

Composite response (weight each coupled mode):

[

$$\mathcal{R}(\omega) \coloneqq \sum_x$$

$$w_x \frac{1}{1 + (\omega \tau_x^{p_x})^2}$$

$$\omega^* \coloneqq \arg \max_{\omega} \mathcal{R}(\omega).$$

]

(Use  $p_x \in [1, 2]$  for broad vs. sharp peaks; weights  $w_x$  from calibration.)

Selectivity (tumor vs. normal):

[

$$S(\omega) \coloneqq \frac{\mathcal{R}(\omega)}{\mathcal{R}(\omega^*)}$$

$$\left(\omega; \tau_{\mathrm{tumor}}\right) \left(\omega; \tau_{\mathrm{normal}}\right),$$

$$\tau_{\mathrm{visc}}^{\mathrm{tumor}} \approx \frac{\eta_{\mathrm{tumor}}}{E_{\mathrm{tumor}}} \approx \frac{\eta_{\mathrm{normal}}}{R_E E_{\mathrm{normal}}}$$

$$\rightarrow f_c^{\mathrm{tumor}} \approx R_E f_c^{\mathrm{normal}},$$

with softness ratio  $R_E \equiv E_{\mathrm{tumor}}/E_{\mathrm{normal}} \approx 0.2\text{--}0.4$ .

\textit{Energy scaling (safe, effective drive):}

$$\left[ \begin{aligned} & \rho_A \equiv \frac{W_{\mathrm{cycle}}}{k_B T} \in [1, 100], \\ & \quad W_{\mathrm{elec}}/A \approx \frac{1}{2} \left( \frac{\epsilon}{\lambda_D} \right)^2 V^2, \\ & \quad W_{\mathrm{mech}} \approx \frac{1}{2} k_{\mathrm{eff}} x^2. \end{aligned} \right]$$

\textit{Design rules (closed form):}

$$\left[ \begin{aligned} & \boxed{f_{\mathrm{diff}}^* \equiv \frac{1}{2\pi} \tau_{\mathrm{diff}}} \\ & \quad \equiv \frac{D}{2\pi L^2} \end{aligned} \right]$$

```

\quad\text{(sets the low-Hz window)}
\]
\[
\boxed{\ f_{\mathrm{visc}}\}^{\star}\ ;
\sim\ ;\ \frac{1}{2\pi}\ ,
\tau_{\mathrm{visc}}\}
\ ;=\ ;\ \frac{E}{2\pi\ ,\eta}\ }
\quad\text{(shifts with softness }
R_E\text{)}}
\]
\[
\boxed{\ f_{\mathrm{mem}}\}^{\star}
\ ;=\ ;\ \frac{1}{2\pi}\ ,R_m\ C_m\ }\quad
\boxed{\ f_{\mathrm{dl}}\}^{\star}\ ;=\ ;
\frac{1}{2\pi}\ ,\tau_{\mathrm{dl}}\}
\ ;=\ ;\ \frac{\sigma\ ,\lambda_D}{2\pi}\ ,
\varepsilon\ ,L\ }\ (\text{fast, usually }
\gg\ \mathrm{Hz})
\]

```

\textit{Rule of engagement.} Tune  $f$  so that  $\rho_x = \omega \tau_x \approx 1$  for the dominant **slow** mode (typically  $\tau_{\mathrm{diff}}$  or  $\tau_{\mathrm{visc}}$ ). Maximize  $S(\omega)$  by placing  $f$  at the tumor peak and off the normal peak.

\textit{Numerical thumbnails (plug-and-play):}

[
 \text{With } D \approx 10^{-9} \mathrm{m}^2/\mathrm{s}; \quad L = \{10, 5, 3\} \mu\mathrm{m} \\
 \rightarrow f\_{\mathrm{diff}}^\* \approx \{1.6, 6.4, 17.7\} \mathrm{Hz}.
 ]

\end{boxedminipage}