```
ln[1]:= Id = \{\{1, 0\}, \{0, 1\}\};
In[2]:= X = PauliMatrix[1];
In[3]:= Z = PauliMatrix[3];
In[4]:= Z01 = KroneckerProduct[Z, Z, Id];
In[5]:= Z02 = KroneckerProduct[Z, Id, Z];
In[6]:= Z12 = KroneckerProduct[Id, Z, Z];
log[T]:= UGamma1 = MatrixExp[-IG1 (3 IdentityMatrix[8] - Z01 - Z02 - Z12) /2];
In[8]:= UGamma1Transpose = Refine[ConjugateTranspose[UGamma1], {Element[G1, Reals]}];
log_{i=0} UGamma2 = MatrixExp[-IG2 (3 IdentityMatrix[8] - Z01 - Z02 - Z12) /2];
In[10]= UGamma2Transpose = Refine[ConjugateTranspose[UGamma2], {Element[G2, Reals]}];
ln[11] := UP = { {1}, {0}};
ln[12]:= DW = \{\{0\}, \{1\}\};
ln[13]:= Plus3 = HadamardMatrix[2^3].KroneckerProduct[UP, UP, UP];
In[14]:= RxBeta1 = MatrixExp[-I * B1 * PauliMatrix[1]];
In[15]:= RxBeta1Transpose = MatrixExp[I * B1 * PauliMatrix[1]];
In[16]:= RxBeta2 = MatrixExp[-I * B2 * PauliMatrix[1]];
In[17]:= RxBeta2Transpose = MatrixExp[I * B2 * PauliMatrix[1]];
In[18]:= RotationBeta1 = KroneckerProduct[RxBeta1, RxBeta1, RxBeta1];
In[19]:= RotationBeta1Transpose =
       KroneckerProduct[RxBeta1Transpose , RxBeta1Transpose , RxBeta1Transpose];
In[20]:= RotationBeta2 = KroneckerProduct[RxBeta2, RxBeta2, RxBeta2];
In[21]:= RotationBeta2Transpose =
       KroneckerProduct[RxBeta2Transpose , RxBeta2Transpose , RxBeta2Transpose ] ;
I_{n[22]} = Fa = Simplify [(1 - Simplify ExpToTrig Simplify (Transpose [Plus3].UGamma1Transpose.]
                  RotationBeta1Transpose.UGamma2Transpose.RotationBeta2Transpose.
                   (Z01).RotationBeta2.UGamma2.RotationBeta1.UGamma1.Plus3)]]]) / 2];
In[23]:=
In[24]:= Zn02 = KroneckerProduct[Z, Id, Z, Id, Id];
In[25]:= Zn12 = KroneckerProduct[Id, Z, Z, Id, Id];
In[26]:= Zn01 = KroneckerProduct[Z, Z, Id, Id, Id];
In[27]:= Zn24 = KroneckerProduct[Id, Id, Z, Id, Z];
In[28]:= Zn23 = KroneckerProduct[Id, Id, Z, Z, Id];
ln[29]: U5Gamma1 = MatrixExp[-IG1 (5 IdentityMatrix[2^5] - Zn02 - Zn01 - Zn12 - Zn24 - Zn23) / 2];
In[30]:= U5Gamma1Transpose = Refine[ConjugateTranspose[U5Gamma1], {Element[G1, Reals]}];
ln[31] = U5Gamma2 = MatrixExp[-IG2 (5 IdentityMatrix[2^5] - Zn02 - Zn01 - Zn12 - Zn24 - Zn23) / 2];
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In[32]:= U5Gamma2Transpose = Refine[ConjugateTranspose[U5Gamma2], {Element[G2, Reals]}];
In[33]:= Rotation5Beta1 = KroneckerProduct[RxBeta1, RxBeta1, RxBeta1, RxBeta1, RxBeta1];
In[34]:= Rotation5Beta1Transpose = KroneckerProduct[RxBeta1Transpose,
         RxBeta1Transpose , RxBeta1Transpose , RxBeta1Transpose ];
In[35]:= Rotation5Beta2 = KroneckerProduct[RxBeta2, RxBeta2, RxBeta2, RxBeta2, RxBeta2];
In[36]:= Rotation5Beta2Transpose = KroneckerProduct[RxBeta2Transpose,
         RxBeta2Transpose, RxBeta2Transpose, RxBeta2Transpose, RxBeta2Transpose];
In[37]:= PulsState5 = HadamardMatrix[2^5].KroneckerProduct[UP, UP, UP, UP, UP];
In[38]:= Fb = Simplify[ExpToTrig[
           Simplify \ \big\lceil \ (Transpose \ [PulsState5] \ . U5Gamma1Transpose \ . Rotation5Beta1Transpose \ .
              U5Gamma2Transpose.Rotation5Beta2Transpose.((IdentityMatrix[2^5] - Zn12) / 2).
              Rotation5Beta2.U5Gamma2.Rotation5Beta1.U5Gamma1.PulsState5)]]];
In[39]:=
In[40]:= CostFunc[G1_, B1_, G2_, B2_] = Simplify[2 Fa + 4 Fb][[1, 1]];
In[41]:= FindMaximum[{CostFunc[G1, B1, G2, B2],
        0 < G1 < 3.14 \&\& 0 < B1 < 3.14 \&\& 0 < G2 < 3.14 \&\& 0 < B2 < 3.14 \}, \{G1, B1, G2, B2\}
Out[41]= \{3.99411, \{G1 \rightarrow 0.415866, B1 \rightarrow 0.406461, G2 \rightarrow 0.90357, B2 \rightarrow 0.147523\}\}
```