

1 introduction

Man i'm typing words but I need math

$$\begin{aligned}Time &= \frac{n}{k} + \frac{n}{k} = \frac{2n}{k} + \frac{3n}{k} + \dots + \frac{kn}{k} \\&= \sum_{i=2}^k i \frac{n}{k} \\&= \frac{n}{k} \sum_{i=2}^k i \\&= \frac{n}{k} \frac{(k+2)(k-1)}{2} \\&= O(nk)\end{aligned}\tag{1}$$

$$\begin{aligned}Base\ Case : T(1) &= (1) \log(1) + (1) = 1 \\&= T(1) = 1\end{aligned}$$

Induction hypothesis : For any number $n > 1$, $n \log n + n$ is true

$$Inductive\ Step : T(n) = (n) \log(n) + (n)$$

$$T(n) = n \log n + n$$

$$T(n) = 2T\left(\frac{n}{2}\right) + n$$

$$= 2\left(\left(\frac{n}{2}\right) \log\left(\frac{n}{2}\right) + \left(\frac{n}{2}\right)\right) + n$$

$$= n \log\left(\frac{n}{2}\right) + n + n$$

$$= n \log n - n + n + n$$

$$= n \log n + n$$

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