

Homework 3

| Id | Refund | Marital Status | Taxable Income | Cheat |
|----|--------|----------------|----------------|-------|
| 1 | Yes | Single | Over 100K | Yes |
| 2 | No | Married | Under 100K | No |
| 3 | Yes | Single | Over 100K | Yes |
| 4 | Yes | Married | Over 100K | Yes |
| 5 | No | Single | Over 100K | No |
| 6 | Yes | Single | Under 100K | No |
| 7 | No | Married | Over 100K | No |
| 8 | No | Single | Over 100K | No |
| 9 | Yes | Single | Under 100K | No |
| 10 | Yes | Married | Over 100K | Yes |

지니계수(Gini index)를 사용하여 최대 깊이 분류 트리(maximum depth classification tree)를 찾으세요.

$$\begin{aligned}
 \text{Gini} &= 1 - \left(\frac{\text{num of Yes}}{\text{total}} \right)^2 - \left(\frac{\text{num of No}}{\text{total}} \right)^2 \\
 &= 1 - \left(\frac{4}{10} \right)^2 - \left(\frac{6}{10} \right)^2 \\
 &= 1 - 0.16 - 0.36 = 1 - 0.52 \\
 &= 0.48
 \end{aligned}$$

1. Refund 예측

- Refund = Yes
 - Cheat = Yes : 4명
 - Cheat = No : 2명
- Refund = No
 - Cheat = Yes : 0명
 - Cheat = No : 4명

→ Gini 계수 : 0.267

2. Marital Status 예측

- Marital Status = Single
 - Cheat = Yes : 3명
 - Cheat = No : 4명
- Marital Status = married
 - Cheat = Yes : 1명
 - Cheat = No : 2명

→ 0.476

Refund Gini 계수 ↓ : 첫 번째 분할

→ 각 분할에 대해 반복

3. Taxable income 예측

- over look
 - Cheat = Yes : 4
 - Cheat = No : 4
- Under look
 - Cheat = Yes : 0
 - Cheat = No : 2

→ 0.4

