

6.1. Calculate probabilities using the uniform distribution rule, combinatorics, and permutation equations.

Ex: A population contains 6 women and 7 men.

1. What is the probability that we select a group of size 5 that contains 2 women and 3 men?

6.2. For a discrete random variable  $X$ , that is *NOT* a specific family of random variables.

Ex: Let  $X$  be the number of times that a randomly selected driver (from a large population) had to take their drivers test before passing. The probabilities for each value of  $X$  is given in the table below.

$X$	$P(X=x)$
1	0.8
2	0.15
3	0.05

1. What is the mean of  $X$ ?
2. What is the variance of  $X$ ?
3. What is the standard deviation of  $X$ ?

### 6.3. For a Bernoulli random variable $X$ .

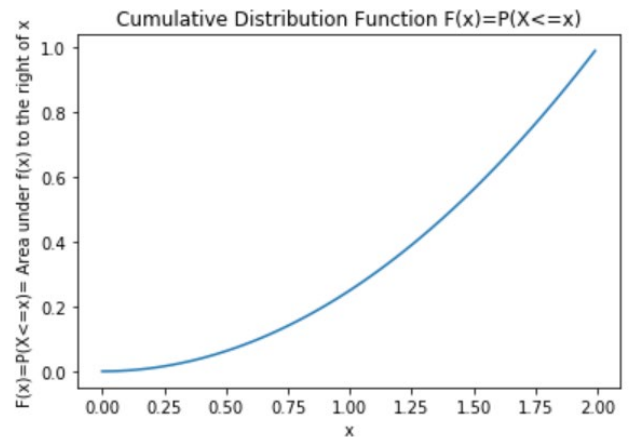
Ex: Let  $Y$  represent a random variable that  $=1$  if a randomly selected UIUC applicant got was accepted into UIUC and  $=0$  if they were not accepted into UIUC. We know that  $P(Y=1)=0.62$ .

1. What kind of random variable is  $Y$ ?
2. What is  $P(Y=0)$ ?
3. What is the mean of  $Y$ ?
4. What is the variance of  $Y$ ?
5. What is the standard deviation of  $Y$ ?

6.4 For a continuous random variable  $X$ , *that is not of a specific family of random variables*.

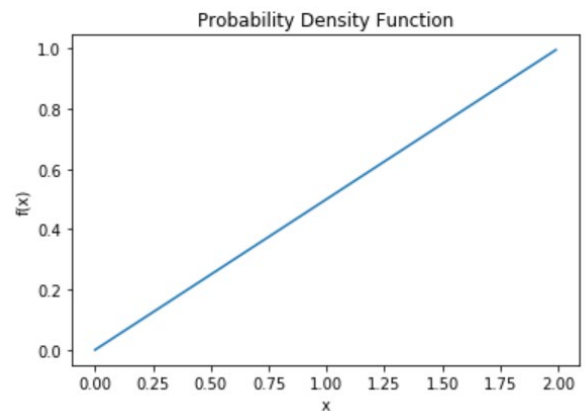
Ex: The probability density function and the cumulative distribution functions for a certain continuous random variable below.

1. Use the cdf to calculate  $P(X \leq 1.5)$ .



2. Use the cdf to calculate  $P(X > 1.5)$ .

3. Use the pdf to calculate  $P(X \leq 1.5)$ .



4. Use the pdf to calculate  $P(X > 1.5)$ .

## 6.7 Calculate probabilities using the rules of combining probabilities.

Ex: Let A be the event of randomly selecting a student from a calculus class that got an A on the final exam. Let B the event of randomly selecting a student from a calculus class that got a B on the final exam. Suppose the  $P(A)=0.2$  and  $P(B)=0.6$ .

1. Are A and B mutually exclusive?
2. Are A and B independent or dependent?
3. What is the probability of randomly selecting a single student that got both an A and a B on the exam?
4. What is the probability of selecting a student that got an A or a B on the exam?
5. Finally, let the event 'passed' be the event that the randomly selected calculus student passed the final exam. Suppose that  $P(\text{passed})=0.95$ . What is the probability that the student got an A on the final exam, given that we know that the student passed the final exam?