

NFA2ParikhImage

Caleb Cheng

2018 Summer Intern

Academia Sinica

Institute of Information Science

Non deterministic Finite Automaton

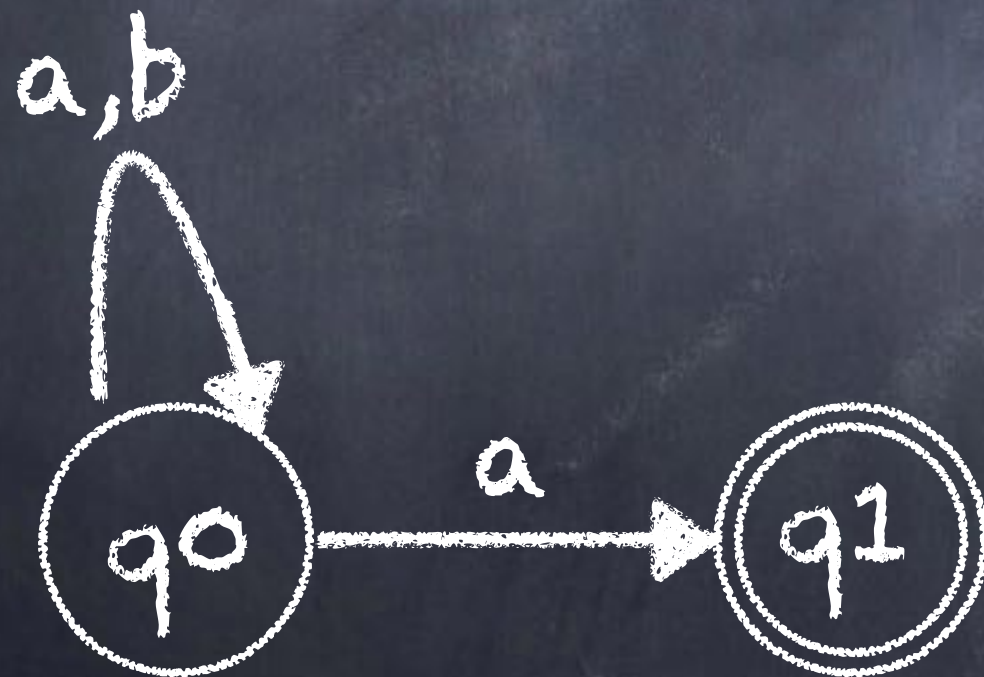
RegEx: $(a|b)^* a$

Accepts:

a
ba
aaa
aba
...

Does not Accepts:

b
bb
aab
...



Parikh Image

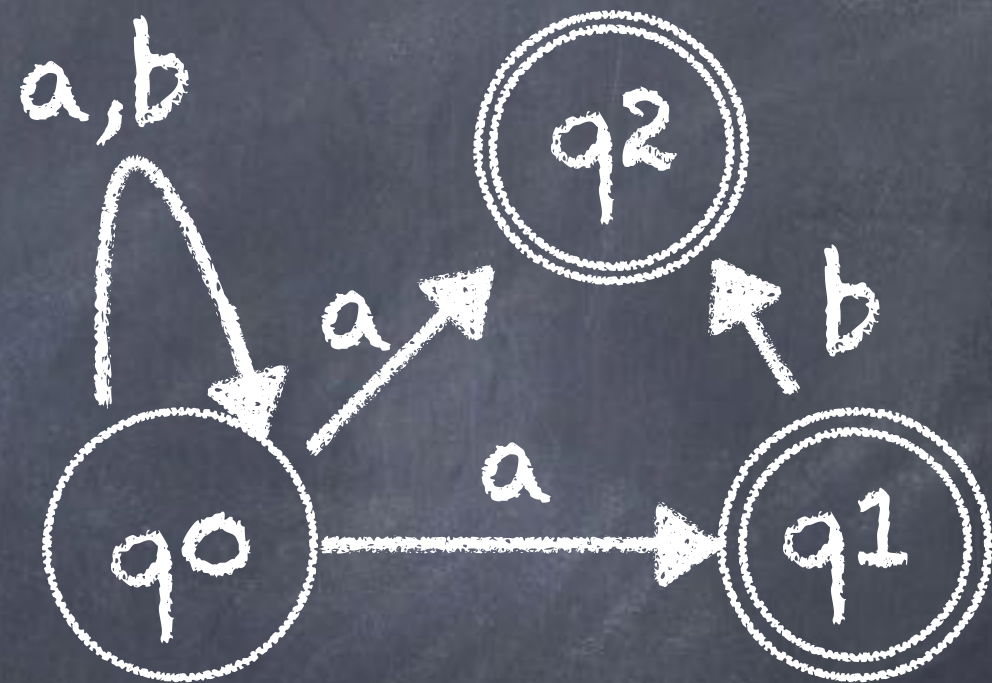
- The relation between the number of occurrences of each symbol
- useful for deciding whether or not a string with a given number of some terminals is accepted by a context-free grammar

Step

1. set variables (x, in, out, r...)
2. set flags
3. check connectivity
4. produce z3 constraints
5. test result using z3

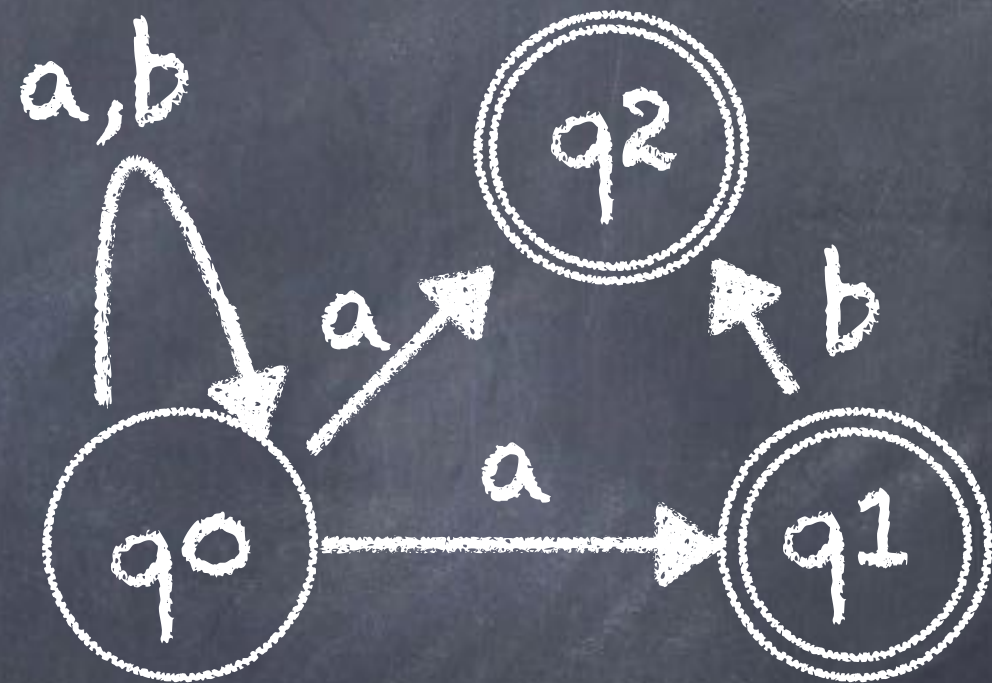
Variables and Parameters

- start_q0 (Bool)
- t_q0 (Bool)
- flag_q0_1 (Bool)
- flag_q0_2 (Bool)
- flag_q0_3 (Bool)



Variables and Parameters

- r_a (Int)
- $x_{q0_a_q1}$ (Int)
- in_{q0} (Int)
- out_{q0} (Int)



Step

1. set variables (x, in, out, r...)
2. set flags
3. check connectivity
4. produce z3 constraints
5. test result using z3

Flags (pseudocode)

for q in states:

if q is terminal state and not initial state:

$\text{flag_q_1} = \text{true}$

$\text{in_q} = \text{out_q} + 1$

else if q is initial state and not not terminal state:

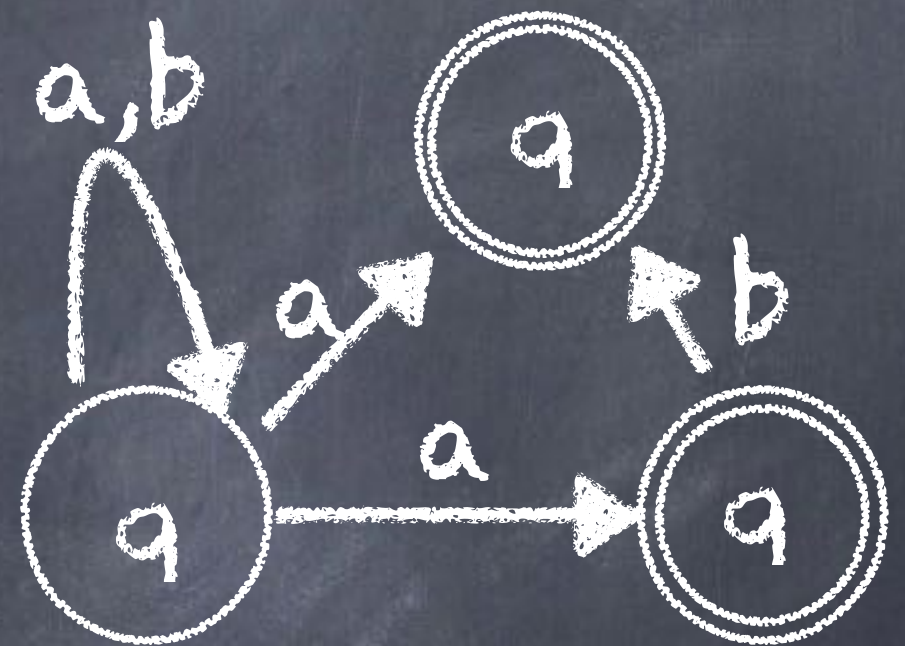
$\text{flag_q_2} = \text{true}$

$\text{in_q} = \text{out_q} - 1$

else

$\text{flag_q_3} = \text{true}$

$\text{in_q} = \text{out_q}$



Step

1. set variables (x, in, out, r...)
2. set flags
3. check connectivity
4. produce z3 constraints
5. test result using z3

Check connectivity

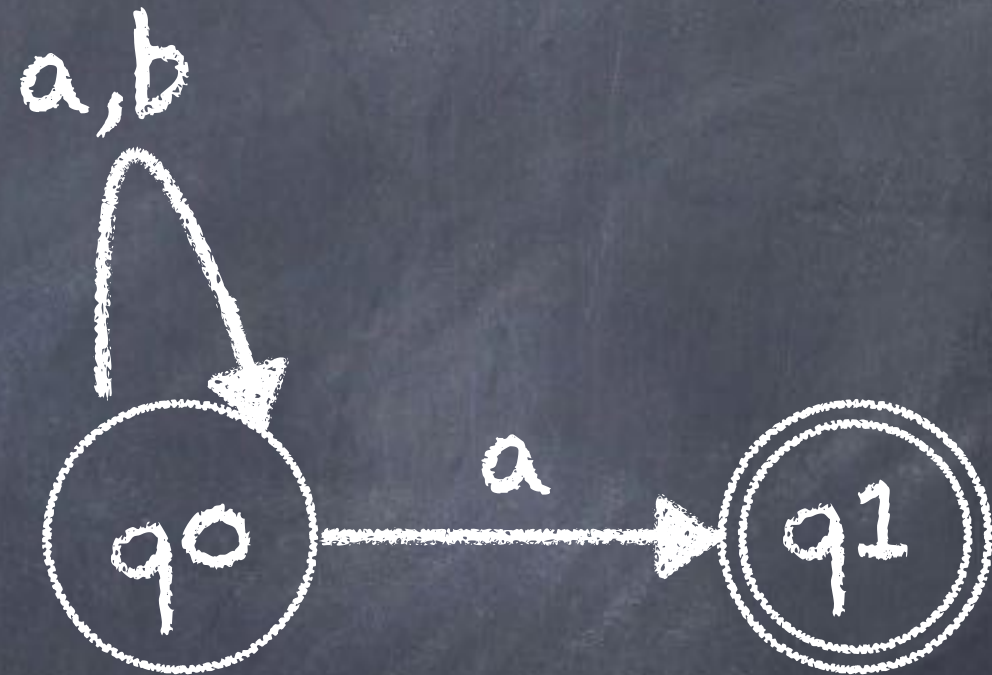
- Depth First Search
- if not reachable from the initial state, set out to 0

Step

1. set variables (x, in, out, r...)
2. set flags
3. check connectivity
4. produce z3 constraints
5. test result using z3

Output

- $$\begin{aligned}
 & \text{(assert (and (and (and (and (and (and} \\
 & \quad (\text{and (and (and (and (and (and (and (and} \\
 & \quad (\text{and (and (and (= r_a (+ x_q0_a_q0} \\
 & \quad \text{x_q0_a_q1))(= r_b x_q0_b_q0))(= out_q0} \\
 & \quad \text{(+ x_q0_a_q0 (+ x_q0_b_q0 x_q0_a_q1))))} \\
 & \quad \text{(= out_q1 0))(= in_q0 (+ x_q0_a_q0} \\
 & \quad \text{x_q0_b_q0))(= in_q1 x_q0_a_q1))start_q0} \\
 & \quad \text{(not start_q1))(= t_q0 0))(= 1 t_q1))(or} \\
 & \quad \text{(or flag_q0_1 flag_q0_2)flag_q0_3))(=} \\
 & \quad \text{flag_q0_1 (and (and (not start_q0))(= t_q0} \\
 & \quad \text{1))(= in_q0 (+ out_q0 1)))))(= flag_q0_2} \\
 & \quad \text{(and (and start_q0 (= t_q0 0))(= in_q0 (-} \\
 & \quad \text{out_q0 1)))))(= flag_q0_3 (and (= in_q0} \\
 & \quad \text{out_q0)(not (xor start_q0 (= t_q0 1))))))} \\
 & \quad \text{(or (or flag_q1_1 flag_q1_2)flag_q1_3))(=} \\
 & \quad \text{flag_q1_1 (and (and (not start_q1))(= t_q1} \\
 & \quad \text{1))(= in_q1 (+ out_q1 1)))))(= flag_q1_2} \\
 & \quad \text{(and (and start_q1 (= t_q1 0))(= in_q1 (-} \\
 & \quad \text{out_q1 1)))))(= flag_q1_3 (and (= in_q1} \\
 & \quad \text{out_q1)(not (xor start_q1 (= t_q1 1)))))))))
 \end{aligned}$$



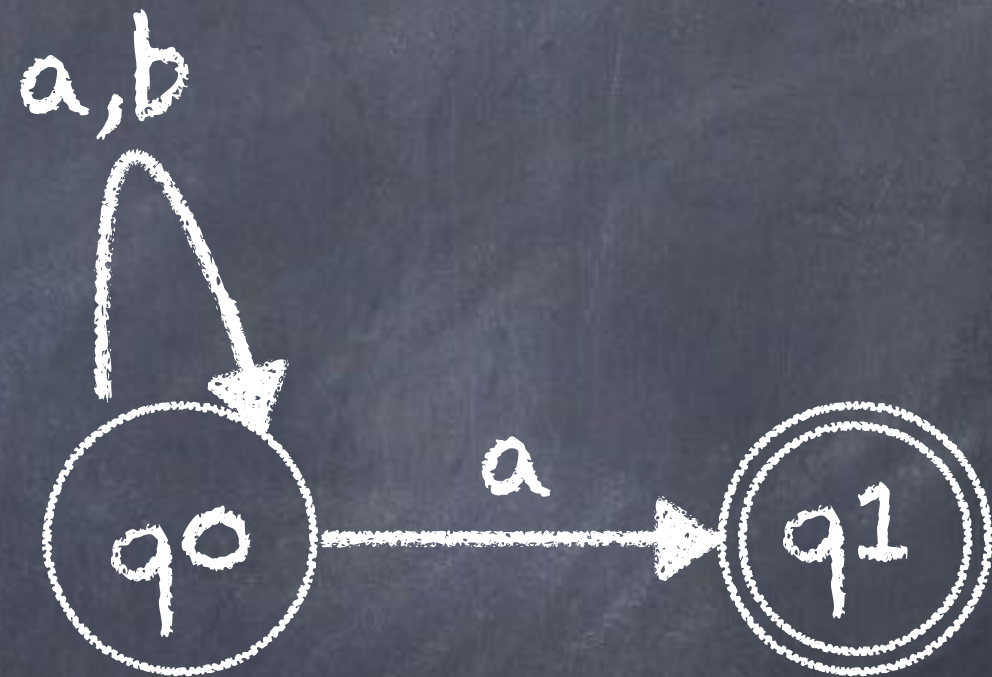
Step

1. set variables (x, in, out, r...)
2. set flags
3. check connectivity
4. produce z3 constraints
5. test result using z3

Test by z3

SAT

- (define-fun x_q0_b_q0 () Int 0)
- (define-fun x_q0_a_q0 () Int 0)
- (define-fun flag_q1_3 () Bool false)
- (define-fun flag_q1_2 () Bool false)
- (define-fun in_q1 () Int 1)
- (define-fun flag_q1_1 () Bool true)
- (define-fun flag_q0_3 () Bool false)
- (define-fun flag_q0_1 () Bool false)
- (define-fun flag_q0_2 () Bool true)
- (define-fun t_q1 () Int 1)
- (define-fun t_q0 () Int 0)
- (define-fun start_q1 () Bool false)
- (define-fun start_q0 () Bool true)
- (define-fun x_q0_a_q1 () Int 1)
- (define-fun in_q0 () Int 0)
- (define-fun out_q1 () Int 0)
- (define-fun out_q0 () Int 1)
- (define-fun r_b () Int 0)
- (define-fun r_a () Int 1)



Reference

- <https://hal.archives-ouvertes.fr/hal-00159525/document>

Code

- <https://github.com/CodingSheep1229/NFA2ParikhImageCI>

Q & A

THE END

thank you