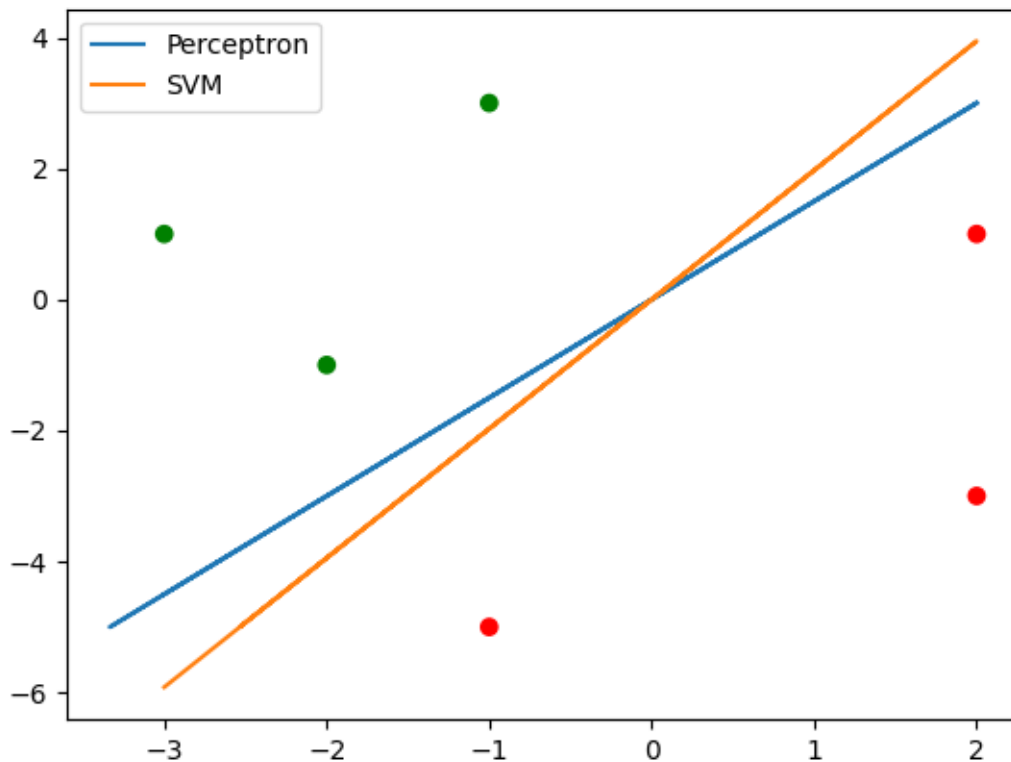


Exercise 1

See Referencesappendix for code.



(a) Perceptron Learning:

Updating vector $w = (0, 0)$ using $(x, y) = ((2, 1), -1)$
 $w = (-2, -1) \rightarrow w = (0, 0) + y = -1 * x = (2, 1)$

Updating vector $w = (-2, -1)$ using $(x, y) = ((-1, 3), 1)$
 $w = (-3, 2) \rightarrow w = (-2, -1) + y = 1 * x = (-1, 3)$

Margin: 0.3076923076923077

(b) SVM Learning:

0.0 $w^* : (-0.6074814098863559, 0.30790724037405226)$
 Margin: 1.9555332420486629

Appendix

Code for Exercise 1

```
1 from matplotlib import pyplot
2 from sklearn.svm import LinearSVC
3
4 S = [
5     ((2, 1), -1),
6     ((-1, 3), 1),
7     ((-3, 1), 1),
8     ((-2, -1), 1),
9     ((-1, -5), -1),
10    ((2, -3), -1),
11 ]
12
13
14 def plot(S, w_perc, w_svm):
15     # scatter points
16     x_values = [s[0][0] for s in S]
17     y_values = [s[0][1] for s in S]
18     colors = ['green' if s[1] == 1 else 'red' for s in S]
19
20     pyplot.scatter(x_values, y_values, c=colors)
21
22     # plot linear separators
23     x_min = min(x_values)
24     x_max = max(x_values)
25     y_min = min(y_values)
26     y_max = max(y_values)
27
28     for w in [w_perc, w_svm]:
29         ortho_w = (-w[1], w[0])
30
31         p_1 = (x_min, ortho_w[1] * (x_min / ortho_w[0]))
32         p_2 = (x_max, ortho_w[1] * (x_max / ortho_w[0]))
33         p_3 = (ortho_w[0] * (y_min / ortho_w[1]), y_min)
34         p_4 = (ortho_w[0] * (y_max / ortho_w[1]), y_max)
35
36         p_x_values = (p_1[0], p_2[0], p_3[0], p_4[0])
37         p_y_values = (p_1[1], p_2[1], p_3[1], p_4[1])
38
39         pyplot.plot(p_x_values, p_y_values, label=('Perceptron' if w==w_perc
40 else 'SVM'))#
41
42     pyplot.legend()
43
44     # save to file
45     pyplot.savefig(f'exercice_01.png')
46
47 def sgn(value) -> int:
48     if value > 0:
49         return 1
50     elif value == 0:
51         return 0
52     else:
53         return -1
54
55
```

```

56 def dot_product(a, b) -> int:
57     return a[0] * b[0] + a[1] * b[1]
58
59
60 def check_consistency(S, w) -> bool:
61     for s in S:
62         if sgn(dot_product(s[0], w)) != s[1]:
63             return False
64     return True
65
66
67 def perceptron(S) -> tuple:
68     w = (0, 0)
69     while not check_consistency(S, w):
70         for s in S:
71             if sgn(dot_product(s[0], w)) != s[1]:
72                 w_old = w
73                 # w <- w + yx
74                 w_x = w[0] + s[1] * s[0][0]
75                 w_y = w[1] + s[1] * s[0][1]
76                 w = (w_x, w_y)
77                 # printing formatted for latex. Just copy and paste
78                 print(f'Updating vector $w={w_old}$ using $(x,y)={s}$ \\\n')
79                 print(
80                     f'$w={w}$ \\\rightarrow w={w_old} + y={s[1]} * x={s[0]}$
81                     \\\n\\bigskip \n')
82     return w
83
84 def margin(S, w) -> float:
85     distances = [abs(dot_product(w, s[0]))/(dot_product(w, w)) for s in S]
86     distances = sorted(distances)
87     return distances[0]
88
89
90 def svm(S) -> tuple:
91     classifier = LinearSVC(fit_intercept=False) # force heterogenous (
92     fit_intercept=False)
93     classifier.fit([[s[0][0], s[0][1]] for s in S], [s[1] for s in S])
94     print(classifier.intercept_)
95     return (classifier.coef_[0][0], classifier.coef_[0][1])
96
97 if __name__ == '__main__':
98     print(f'Perceptron Learning: \\\n\\bigskip \n')
99     w_perc = perceptron(S)
100    print(f'Margin: ${margin(S,w_perc)}$')
101
102    print(f'SVM Learning: \\\n\\bigskip \n')
103    w_svm = svm(S)
104    print(f'$w^*: {w_svm}$ \\\n')
105    print(f'Margin: ${margin(S, w_svm)}$')
106
107    plot(S, w_perc, w_svm)

```