Exercise 1

(a) Using Theorem 3.6:

$$\Pr_{T \mathcal{D}^m} (\forall h \in \mathcal{H} : |err_T(h) - err_D(h)| \le \epsilon) > 1 - \delta$$

$$\Pr_{T \mathcal{D}^m} (\forall h \in \mathcal{H} : |err_T(h) - err_D(h)| \le \epsilon) > 0.9$$

$$\Rightarrow \delta = 0.1$$

$$m \ge \frac{1}{2\epsilon^2} \log \left(\frac{2|\mathcal{H}|}{\delta} \right)$$

$$143 \ge \frac{1}{2\epsilon^2} \log \left(\frac{2 \cdot 2^3}{0.1} \right)$$

$$143 \ge \frac{1}{2\epsilon^2} (\log(2^4) - \log(0.1))$$

$$143 \ge \frac{1}{2\epsilon^2} (4 - \log(0.1))$$

$$\epsilon^2 \ge \frac{(4 - \log(0.1))}{1432}$$

$$|\epsilon| \ge \sqrt{\frac{(4 - \log(0.1))}{286}}$$

$$\Rightarrow \epsilon \ge \sqrt{\frac{(4 - \log(0.1))}{286}}$$

$$\epsilon \ge \sqrt{\frac{(4 - \log(0.1))}{286}}$$

$$\Pr_{T \mathcal{D}^m} (\forall h \in \mathcal{H} : |err_T(h) - err_D(h)| \le \epsilon) > 0.9$$

$$\Pr_{T \mathcal{D}^m} \left(\forall h \in \mathcal{H} : |0.03 - err_D(h)| \le \sqrt{\frac{(4 - \log(0.1))}{286}} \right) > 0.9$$

$$\Rightarrow err_D(h) \le 0.03 + \sqrt{\frac{(4 - \log(0.1))}{286}} \simeq 0.05560114718 \simeq 0.06$$

(b) Using Theorem 3.4:

 $\Pr_{T \ \mathcal{D}^m} (\forall h \in \mathcal{H} : \text{if } h \text{ is consistent with } T, \text{ then } err_D(h) \leq \epsilon) 1 - \delta$ $\Pr_{T \ \mathcal{D}^m} (\forall h \in \mathcal{H} : \text{if } h \text{ is consistent with } T, \text{ then } err_D(h) \leq 0.01) 0.9$ $\Rightarrow \epsilon = 0.01, \delta = 0.1$

$$m \ge \frac{1}{\epsilon} \ln \left(\frac{|\mathcal{H}|}{\delta} \right)$$

$$m \ge \frac{1}{0.01} \ln \left(\frac{2^3}{0.1} \right)$$

$$m \ge 100(\ln(3) - \ln(0.1)) \sim 100 \cdot 3.40119738166 = 340.1197$$

$$\Rightarrow m > 341$$

Exercise 2

- (a)
- (b)

Exercise 3

- (a)
- (b)

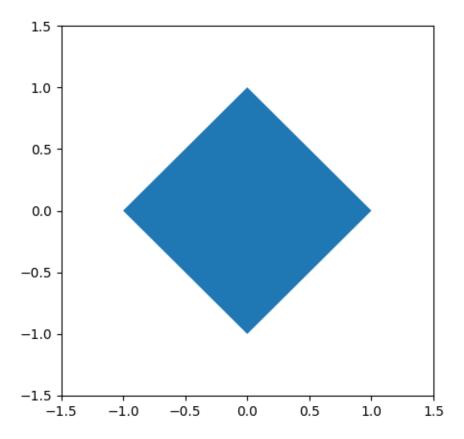
Exercise 4

- (a)
- (b)

Exercise 5

- (a)
- (b)

Exercise 6



(a) (i)

(ii) Similarly to how in l=2 the "corners" of the unit circle are the 2 unit vectors and their negations (so 4 in total), the "corners" of the unit circle in l=3 are the 3 unit vectors and their negations (so 6 in total). Combined with the edges and facing connecting them they make for a "diamond" shape.

(b)
$$vol(B_1^2) = (\sqrt{1^2 + 1^2})^2 = 2$$
 and $vol(B_1^3) = 2 \cdot \frac{(\sqrt{1^2 + 1^2})^2 \cdot 1}{3} = \frac{4}{3}$

(c) Cover B_1^l by 2k cylinders. The thickness of the cylinders is $t := \frac{1}{k}$. Thus, the radius of the *i*th cylinder above (or below) is $r_i := 1 - (i - 1) \cdot t$. Therefore, the volume of the *i*th

cylinder is $t \cdot r_i^{l-1} \cdot vol(B_1^{l-1})$. Thus:

$$\begin{split} vol(B_1^l) & \leq 2 \sum_{i=1}^k t \cdot r_i^{l-1} \cdot vol(B_1^{l-1}) \\ & = \left(2 \sum_{i=1}^k \frac{1}{k} \left(1 - \frac{i-1}{k}\right)^{l-1}\right) \cdot vol(B_1^{l-1}) \\ & = \left(2 \sum_{i=0}^{k-1} \frac{1}{k} \left(1 - \frac{i}{k}\right)^{l-1}\right) \cdot vol(B_1^{l-1}) \\ & = \left(2 \frac{1}{k} \left(1^{l-1} + (1 - \frac{1}{k})^{l-1} + \dots + (1 - \frac{k-1}{k})^{l-1}\right)\right) \cdot vol(B_1^{l-1}) \\ & = \left(2 \left(\frac{k^{l-1}}{k^l} + (\frac{(k-1)^{l-1}}{k^l}) + \dots + (\frac{1^{l-1}}{k^l}) + (\frac{0^{l-1}}{k^l})\right)\right) \cdot vol(B_1^{l-1}) \\ & = \left(2 \sum_{i=0}^k \left(\frac{i^{l-1}}{k^l}\right)\right) \cdot vol(B_1^{l-1}) \end{split}$$

We can use the ratio test on the series S:

$$\lim_{k \to \infty} \left| \frac{\left(\frac{(i+1)^{l-1}}{k^l}\right)}{\left(\frac{i^{l-1}}{k^l}\right)} \right| = \left| \frac{i+1}{i}^{l-1} \right| = \left| (1+\frac{1}{i})^{l-1} \right| > 1$$

Huh? Something is wrong here

Appendix