cs113 Lab Build Script

Text written to file build.sh

| doctex lab.doc | pptexenv latex lab.tex | dvipdf lab.dvi

Bourne Shell

chmod 777 build.sh

Problem 15.21 Math

- Plug g(x) as x in f(x) and expand
 - f(2x-7)
 - -4(2x-7)+9
 - -8x+37
- Plug f(x) as x in g(x) and expand
 - g(-4x+9)
 - -2(-4x+9)-7
 - -8x+11

Problem 15.21

Let f be the relation on $\mathbb R$ defined by x f y if and only f(x)=-4x+9. Let g be the relation on $\mathbb R$ defined by x g y if and only g(x)=2x-7. Find $f\circ g$ and $g\circ f$.

Problem 15.21 SML

```
SML
datatype'a seq = Empty \mid Cons \ of'a * (unit -> 'a seq);
fun \ seqFrom \ i = Cons(i,fn() => seqFrom(i+1));
val \ nat = seqFrom \ 1;
fun\ takeSeg(0, \_) = []
   |takeSeq(\_,Empty) = []
   |takeSeq(i,Cons(n,s))| = n::takeSeq(i-1,s());
val\ test = takeSeq(10000, nat);
fun\ id(x) = x;
fun \ f(x) = (\sim 4 * x) + 9;
fun \ q(x) = (2*x)-7;
fun \ fg(x) = (\sim 8*x) + 37;
fun \ qf(x) = (\sim 8*x) + 11;
(map (fn x=> f(g(x))) test) = (map (fn x=> fg(x)) test);
|(map\ (fn\ x=>g(f(x)))\ test)=(map\ (fn\ x=>gf(x))\ test);
```

```
> datatype 'a seg = Empty | Cons of 'a * (unit -> 'a seg);
fun segFrom i = Cons(i.fn() => segFrom(i+1));
val nat = segFrom 1:
fun takeSeq(\hat{0}, ) = []
   |takeSeg(_,Empty) = []
   |takeSeg(i,Cons(n,s)) = n::takeSeg(i-1,s());
val test = takeSeg(10000.nat):
fun id(x) = x:
fun f(x) = (\sim 4 \times x) + 9:
fun g(x) = (2*x)-7;
fun \bar{f}g(x) = (~8*x) + 37;
fun g\bar{f}(x) = (~8*x) + 11:
(map (fn x=> f(g(x))) test) = (map (fn x=> fg(x)) test);
(map (fn x=> g(f(x))) test) = (map (fn x=> gf(x)) test);
datatype 'a seg = Cons of 'a * (unit -> 'a seg) | Empty
> val segFrom = fn: int -> int seg
> val nat = Cons (1, fn): int seq
> # # val takeSeg = fn: int * 'a seg -> 'a list
\Rightarrow val test = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, ...]: int list
> val id = fn: 'a -> 'a
> val f = fn: int -> int
> val g = fn: int -> int
> val fe = fn: int -> int
> val ef = fn: int -> int
> val it = true: bool
> val it = true: bool
```