Machine learning

interpretability

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Contents

- 1. Interpretability
- 2. Explanations
- 3. Explanations in machine learning
- 4. Linear models
 - Linear regression
 - Logistic regression
- 5. Filters and patterns
- 6. Local Interpretable Model-agnostic Explanations (LIME)
- 7. Feature selection

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Interpretability

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Interpretability

- what is interpretability?
- why care about interpretability?

• how do we get interpretability?

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4 / 37

Interpretability

- what is interpretability?
 - ► "Interpretability is the degree to which a human can understand the cause of a decision." (Miller cited in Molnar, 2020, p. 18)
 - ► "Interpretability is the degree to which a human can consistently predict the model's result" (Kim et al. cited in Molnar, 2020, p. 18)
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4 / 37

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 - ► from the EU GDPR: [the data subject should have] the right ... to obtain an explanation of the decision reached.

From https://en.wikipedia.org/wiki/Right_to_explanation

how do we get interpretability?

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4 / 37

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4/3/

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 - ▶ in cognitive neuroscience we want to know why something happened
 - ★ e.g. what is the difference between seeing houses and faces?
- how do we get interpretability?
 - ► the topic of today's lecture

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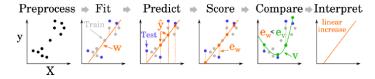
4 / 37

Machine learning recap

- create <u>features</u>
- make cross-validation scheme
- fit model
- interpret model

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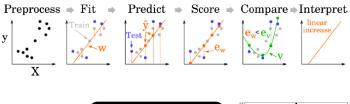
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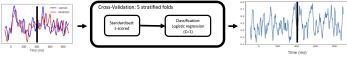
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5 / 37

Machine learning recap

- create <u>features</u>
- make cross-validation scheme
- fit model
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Top figure from King et al. (2018)

bottom figure mine.

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 ${\sf Explanations}$

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What is an explanation?

- 1. What is the <u>aim</u> of an explanation?
- 2. What is the structure of an explanation?

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8 / 37

The aim of explanations

Explanation and understanding

Knowledge of a fact¹

¹Fact is meant to include facts, statements, theories etc.

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9/3

The aim of explanations

Explanation and understanding

- Knowledge of a fact¹
- That the fact happened*

 $^{1}\mbox{Fact}$ is meant to include facts, statements, theories etc.

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The aim of explanations

Explanation and understanding

- Knowledge of a fact¹
- That the fact happened*
- Explanation: understand why the fact happened

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The aim of explanations

Explanation and understanding

- Knowledge of a fact¹
- That the fact happened*
- Explanation: understand why the fact happened

"What has to be added to knowledge to yield understanding". (Lipton, 2004, p. 21)

¹Fact is meant to include facts, statements, theories etc.

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The structure of explanations

- Explanandum: the fact to be explained
- Explanans: the statements that explains

Types of explanations¹

- Psychological explanation
- Functional explanation
- Mechanistic explanation
- Nomic explanation (also called nomological explanation)
- Casual explanation

¹For more see e.g. Bird (2003), esp. chapter 2 Mads Jensen (RFR, IMC, & CFIN)

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11 / 3

Contrastive explanation

• Explaining why *P* happened rather than *Q*.

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12 / 3

Contrastive explanation

- Explaining why P happened rather than Q.
- Fact and foil (*P* is the fact, *Q* the foil)

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Examples:

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12/37

Contrastive explanation

- Explaining why P happened rather than Q.
- Fact and foil (*P* is the fact, *Q* the foil)

Examples:

• Why did I go to London rather than Paris?

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12 / 37

Contrastive explanation

- Explaining why P happened rather than Q.
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Examples:

- Why did I go to London rather than Paris?
- Why did Clara rather than Johanne sneeze?

Contrastive explanation

- Explaining why P happened rather than Q.
- Fact and foil (*P* is the fact, *Q* the foil)

Examples:

- Why did I go to London rather than Paris?
- Why did Clara rather than Johanne sneeze?
- Why did the model predict cat rather than dog?

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12 / 37

Explanations in machine learning

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13 / 37

Explanations in machine learning

"An explanation usually relates the feature values of an instance to its model prediction in a humanly understandable way." (Molnar, 2020, p. 31)

Explanations in machine learning

"An explanation usually relates the feature values of an instance to its model prediction in a humanly understandable way." (Molnar, 2020, p. 31)

Taxonomy of interpretability

- intrinsic interpretability
 - ► simple structures
- post-hoc interpretability
 - ► interpretation after training the model

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14 / 37

Linear models

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15 / 3

Do linear models create good explanations?

"Linear models create truthful explanations, as long as the linear equation is an appropriate model for the relationship between features and outcome."

(Molnar, 2020, p. 63)

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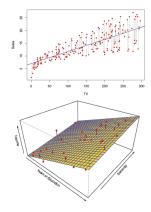
Linear regression (Figure from James et al., 2013) ◆□ → ◆□ → ◆ = → ◆ = → へ ○ へ ○ Mads Jensen (RFR, IMC, & CFIN) interpretability Linear regression (Figure from James et al., 2013) Mads Jensen (RFR, IMC, & CFIN) interpretability Linear regression pros: • weighted sum • well known • guarantee to find optimal weights

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(Figure from James et al., 2013)

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Linear regression



(Figure from James et al., 2013)

pros:

- weighted sum
- well known
- guarantee to find optimal weights

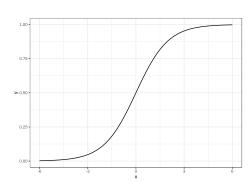
cons:

- can only represent linear relationships
- "interpretation of a weight can be unintuitive because it depends on all other features" (Molnar, 2020, p. 67)
- "Completely correlated features make it even impossible to find a unique solution" (Molnar, 2020, p. 68)
- interactions need to be handcrafted = ~~~~

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Logistic regression



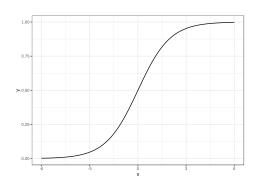
(Figure from Molnar, 2020)

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Logistic regression



pros:

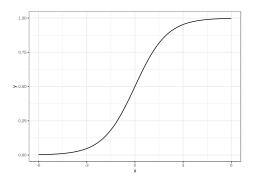
- provide probabilities
- fast

(Figure from Molnar, 2020)

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Logistic regression



pros:

- provide probabilities
- fast

cons:

- "interpretation of the weights is multiplicative and not additive" (Molnar, 2020, p. 75, my italics)
- can only represent linear relationships
- interactions need to be handcrafted

(Figure from Molnar, 2020)

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18 / 37

Filters and patterns

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19 / 37

Haufe et al. 2014

NeuroImage 87 (2014) 96-110

Contents lists available at ScienceDirect



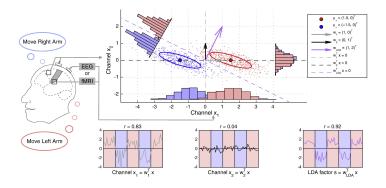
NeuroImage



CrossMark

Stefan Haufe ^{a,b,*}, Frank Meinecke ^{c,a}, Kai Görgen ^{d,e,f}, Sven Dähne ^a, John-Dylan Haynes ^{d,e,b}, Benjamin Blankertz ^D, Felix Bießmann ^{g,a,*}

On the interpretation of weight vectors ...



(Figure from Haufe et al., 2014)

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21 / 37

On the interpretation of weight vectors ...

	n 1 11	P. 1. 1. 1.1
	Forward model	Backward model
Alternative name	Generative model	Discriminative model
Model (linear case)	$\mathbf{x}(n) = \mathbf{A}\mathbf{s}(n) + \epsilon(n)$	$\mathbf{W}^{T}\mathbf{x}(n) = \hat{\mathbf{s}}(n)$
Purpose	Factorize the data into latent factors $s(n)$ and their corresponding activation	Extract latent factors $\hat{s}(n)$ from the data by multiplying with extraction
	patterns (columns of A), plus noise $\epsilon \epsilon(n)$.	filters (columns of W).
Interpretable	$\mathbf{A}, \mathbf{s}(n)$	$\hat{s}(n)$
Supervised case	Encoding: Replace latent factors $\mathbf{s}(n)$ by known external target variables $\mathbf{y}(n)$	Decoding: Seek latent factors $\hat{\mathbf{s}}(n)$ to approximate known external target
	or pre-estimated factors $\hat{\mathbf{s}}(n)$. Thus, estimate how $\mathbf{y}(n)$ or $\hat{\mathbf{s}}(n)$ are encoded in	variables $\mathbf{y}(n)$. Thus, estimate how $\mathbf{y}(n)$ can be decoded from the measurement.
	the measurement.	

(table from Haufe et al., 2014)

x(n) M-dimensional vector of observed data A M \times K matrix of patterns in forward models W M \times K matrix of filters in backward model $s(n), \hat{s}(n)$ K-dimensional vector of latent factors

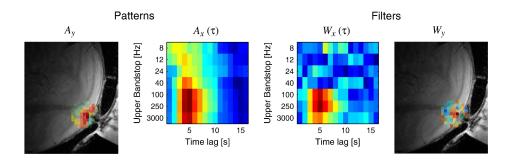
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22 / 37

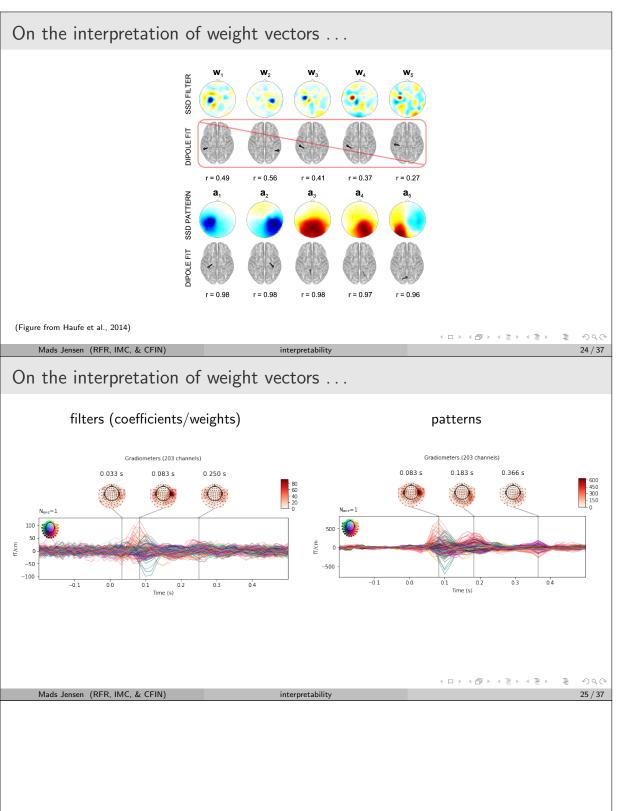
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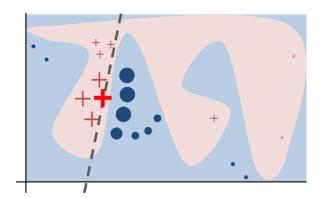
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Local Interpretable Model-agnostic Explanations (LIME)

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(Figure from Ribeiro et al., 2016)

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Local Interpretable Model-agnostic Explanations (LIME)









(Figure from Ribeiro et al., 2016)

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Local Interpretable Model-agnostic Explanations (LIME)

Prediction probabilities atheism

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christian

Text with highlighted words From: johnchad@triton.unm.edi (johadwic)
Subject: Another request for Darwin Fish
Organization: University of New Mexico, Albuquerque

NNTP-Posting-Host: triton.unm.edu

Hello Gang,

There have been some notes recently asking where to obtain the DARWIN fish. This is the same question I have and I have not seen an answer on the net. If anyone has a contact please post on the net or email me.

 $({\sf Figure\ from\ https://github.com/marcotcr/lime})$

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Local Interpretable Model-agnostic Explanations (LIME)

Explaining prediction of 'Cat' in pros and cons



 $(\mathsf{Figure}\ \mathsf{from}\ \mathsf{https:}//\mathsf{github.com/marcotcr/lime})$

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30 / 37

Local Interpretable Model-agnostic Explanations (LIME)



(a) Husky classified as wolf

(Figure from Ribeiro et al., 2016)

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Local Interpretable Model-agnostic Explanations (LIME)



(a) Husky classified as wolf



(b) Explanation

(Figure from Ribeiro et al., 2016)

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Feature selection

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32 / 37

Feature selection

Example: MNE sample data

sensor space:

- 102 magnetometers, 204 gradiometers
- downsampled to 60 Hz
- X = (123 * 306 * 43)
- X has 13.158 features in each row and 1,613,145 data points in total

source space:

- 5124 source space points
- downsampled to 60 Hz
- X = (123 * 5124 * 43)
- X has 220.332 in each row and 27,100,836 data points in total

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33 / 37

Feature selection

before fitting

after fitting

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Feature selection

before fitting

- variance thresholding
- univariate feature selection
 - ► select k best features
 - ► select percentile
 - \blacktriangleright χ^2 , f-test

after fitting

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34 / 37

Feature selection

before fitting

- variance thresholding
- univariate feature selection
 - ► select k best features
 - ► select percentile
 - $ightharpoonup \chi^2$, f-test

after fitting

- select based on weights/coefficients
- recursive feature elimination
- model based:
 - ► I1-based feature selection
 - ► feature importance from a tree based model

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34 / 3

Questions?

- 1. Interpretability
- 2. Explanations
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36 / 37

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