

# Machine learning interpretability

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AARHUS UNIVERSITY



INTERACTING MINDS CENTRE



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1. Interpretability
2. Explanations
3. Explanations in machine learning
4. Linear models
  - Linear regression
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6. Local Interpretable Model-agnostic Explanations (LIME)
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# Interpretability

# Interpretability

- what is interpretability?
- why care about interpretability?
- how do we get interpretability?

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  - ▶ “Interpretability is the degree to which a human can understand the cause of a decision.” (Miller cited in Molnar, 2020, p. 18)
  - ▶ “Interpretability is the degree to which a human can consistently predict the model’s result” (Kim et al. cited in Molnar, 2020, p. 18)
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# Interpretability

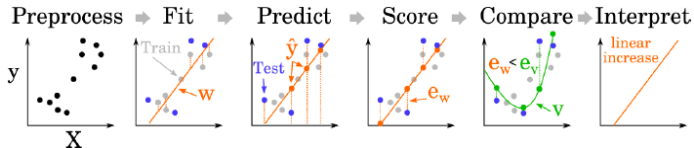
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  - ▶ in cognitive neuroscience we want to know *why* something happened
    - ★ e.g. what is the difference between seeing houses and faces?
- how do we get interpretability?
  - ▶ the topic of today’s lecture

# Machine learning recap

- create features
- make cross-validation scheme
- fit model
- interpret model

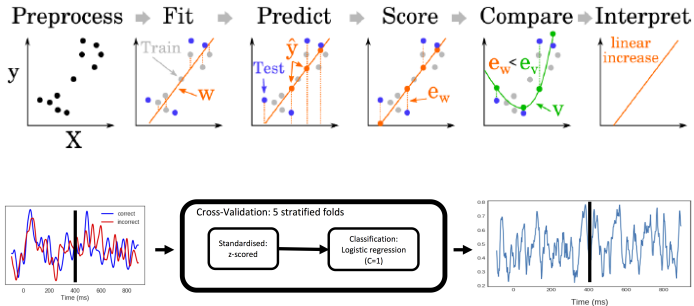
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Top figure from King et al. (2018)

bottom figure mine.

# Explanations

# Why care about explanations?



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Science . . .

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Science . . .

Example:

Explainable machine learning (interpretable ML)

# What is an explanation?

1. What is the aim of an explanation?
2. What is the structure of an explanation?

# The aim of explanations

## Explanation and understanding

- Knowledge of a fact<sup>1</sup>

---

<sup>1</sup>Fact is meant to include facts, statements, theories etc.

# The aim of explanations

## Explanation and understanding

- Knowledge of a fact<sup>1</sup>
- That the fact happened\*

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# The aim of explanations

## Explanation and understanding

- Knowledge of a fact<sup>1</sup>
- That the fact happened\*
- **Explanation:** understand why the fact happened

"What has to be added to knowledge to yield understanding".  
(Lipton, 2004, p. 21)

---

<sup>1</sup>Fact is meant to include facts, statements, theories etc.

# The structure of explanations

- **Explanandum:** the fact to be explained
- **Explanans:** the statements that explains



# Types of explanations<sup>1</sup>

- Psychological explanation
- Functional explanation
- Mechanistic explanation
- Nomic explanation (also called nomological explanation)
- Casual explanation

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<sup>1</sup>For more see e.g. Bird (2003), esp. chapter 2

# Contrastive explanation

- Explaining why  $P$  happened rather than  $Q$ .

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Examples:

- Why did I go to London rather than Paris?

# Contrastive explanation

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Examples:

- Why did I go to London rather than Paris?
- Why did Clara rather than Johanne sneeze?

# Contrastive explanation

- Explaining why  $P$  happened rather than  $Q$ .
- Fact and foil  
( $P$  is the fact,  $Q$  the foil)

Examples:

- Why did I go to London rather than Paris?
- Why did Clara rather than Johanne sneeze?
- Why did the model predict *cat* rather than *dog*?

# Explanations in machine learning



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*“An explanation usually relates the feature values of an instance to its model prediction in a humanly understandable way.” (Molnar, 2020, p. 31)*

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## Taxonomy of interpretability

- intrinsic interpretability
  - ▶ simple structures
- post-hoc interpretability
  - ▶ interpretation after training the model

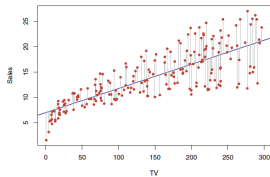
# Linear models

# Do linear models create good explanations?

*“Linear models create truthful explanations, as long as the linear equation is an appropriate model for the relationship between features and outcome.”*

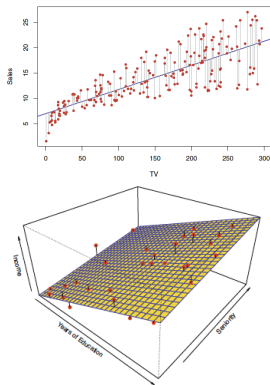
*(Molnar, 2020, p. 63)*

# Linear regression



(Figure from James et al., 2013)

# Linear regression

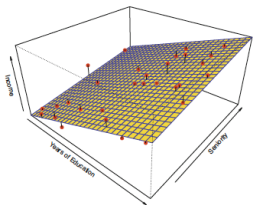
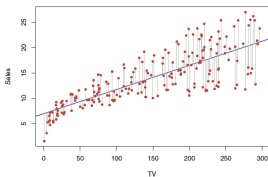


(Figure from James et al., 2013)

# Linear regression

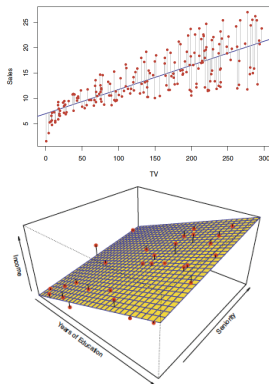
pros:

- weighted sum
- well known
- guarantee to find optimal weights



(Figure from James et al., 2013)

# Linear regression



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pros:

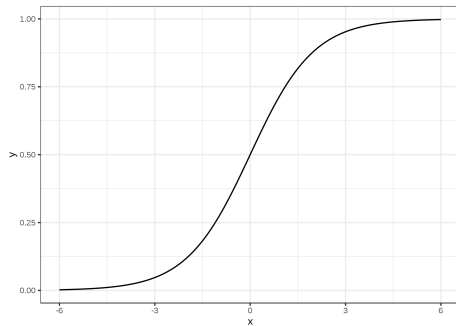
- weighted sum
- well known
- guarantee to find optimal weights

cons:

- can only represent linear relationships
- “interpretation of a weight can be unintuitive because it depends on all other features” (Molnar, 2020, p. 67)
- “Completely correlated features make it even impossible to find a unique solution” (Molnar, 2020, p. 68)
- interactions need to be handcrafted



# Logistic regression

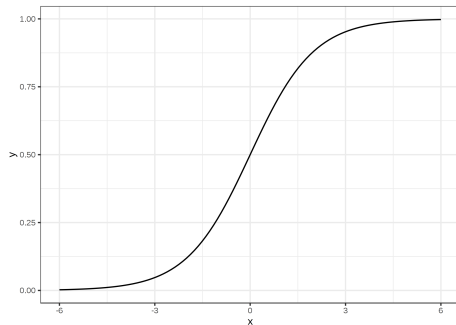


(Figure from Molnar, 2020)

# Logistic regression

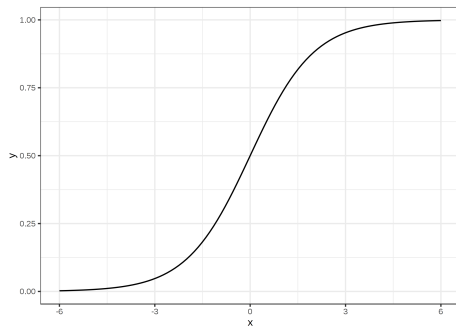
pros:

- provide probabilities
- fast



(Figure from Molnar, 2020)

# Logistic regression



(Figure from Molnar, 2020)

pros:

- provide probabilities
- fast

cons:

- “interpretation of the weights is *multiplicative* and not additive” (Molnar, 2020, p. 75, my italics)
- can only represent linear relationships
- interactions need to be handcrafted

# Filters and patterns

NeuroImage 87 (2014) 96–110



Contents lists available at ScienceDirect

NeuroImage

journal homepage: [www.elsevier.com/locate/ynimg](http://www.elsevier.com/locate/ynimg)

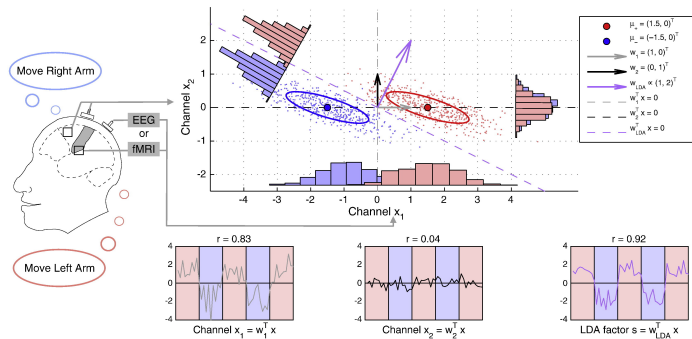


## On the interpretation of weight vectors of linear models in multivariate neuroimaging<sup>☆</sup>



Stefan Haufe<sup>a,b,\*</sup>, Frank Meinecke<sup>c,a</sup>, Kai Gorgen<sup>d,e,f</sup>, Sven Dahne<sup>a</sup>, John-Dylan Haynes<sup>d,e,b</sup>, Benjamin Blankertz<sup>f,b</sup>, Felix Bießmann<sup>g,a,\*</sup>

# On the interpretation of weight vectors ...



(Figure from Haufe et al., 2014)

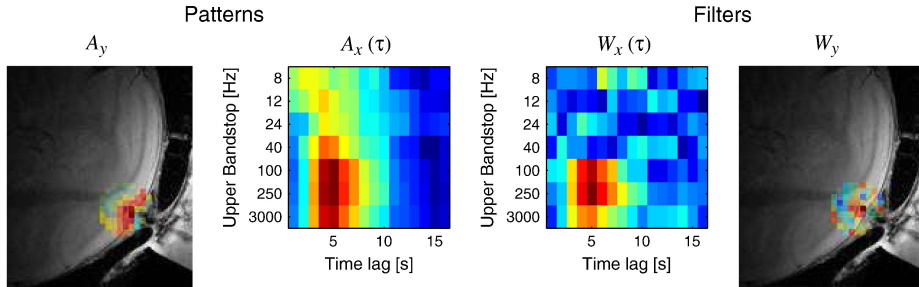
# On the interpretation of weight vectors ...

	Forward model	Backward model
Alternative name	Generative model	Discriminative model
Model (linear case)	$\mathbf{x}(n) = \mathbf{A}\mathbf{s}(n) + \epsilon(n)$	$\mathbf{W}^T \mathbf{x}(n) = \hat{\mathbf{s}}(n)$
Purpose	Factorize the data into <i>latent factors</i> $\mathbf{s}(n)$ and their corresponding <i>activation patterns</i> (columns of $\mathbf{A}$ ), plus noise $\epsilon \in(n)$ .	Extract <i>latent factors</i> $\hat{\mathbf{s}}(n)$ from the data by multiplying with <i>extraction filters</i> (columns of $\mathbf{W}$ ).
Interpretable	$\mathbf{A}, \mathbf{s}(n)$	$\hat{\mathbf{s}}(n)$
Supervised case	Encoding: Replace latent factors $\mathbf{s}(n)$ by known external target variables $\mathbf{y}(n)$ or pre-estimated factors $\hat{\mathbf{s}}(n)$ . Thus, estimate how $\mathbf{y}(n)$ or $\hat{\mathbf{s}}(n)$ are <i>encoded</i> in the measurement.	Decoding: Seek latent factors $\hat{\mathbf{s}}(n)$ to approximate known external target variables $\mathbf{y}(n)$ . Thus, estimate how $\mathbf{y}(n)$ can be <i>decoded</i> from the measurement.

(table from Haufe et al., 2014)

$\mathbf{x}(n)$  M-dimensional vector of observed data  
 $\mathbf{A}$   $M \times K$  matrix of patterns in forward models  
 $\mathbf{W}$   $M \times K$  matrix of filters in backward model  
 $\mathbf{s}(n), \hat{\mathbf{s}}(n)$  K-dimensional vector of latent factors

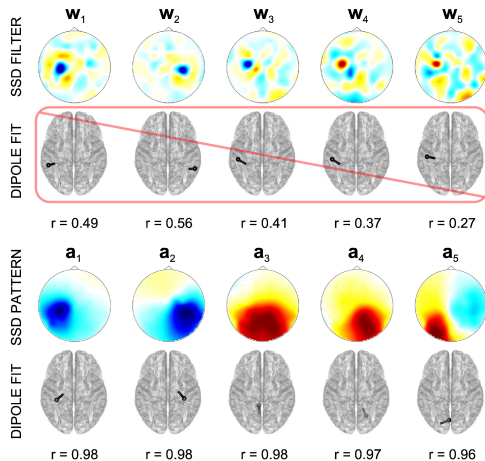
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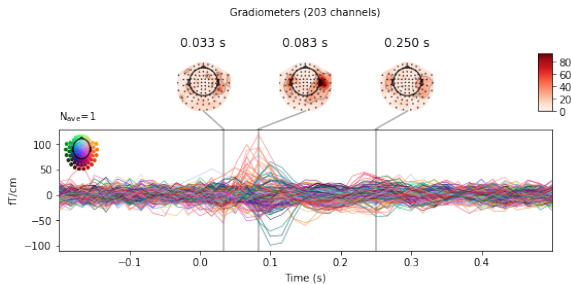
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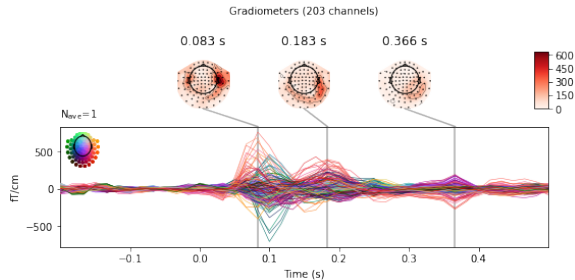
(Figure from Haufe et al., 2014)

# On the interpretation of weight vectors ...

filters (coefficients/weights)

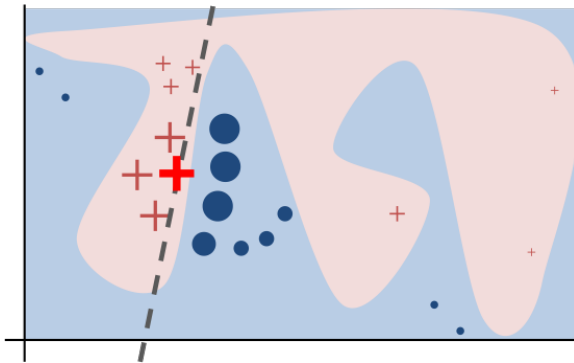


patterns



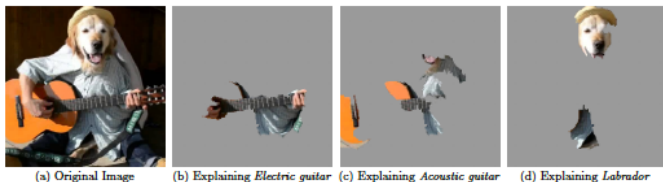
# Local Interpretable Model-agnostic Explanations (LIME)

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(Figure from Ribeiro et al., 2016)

# Local Interpretable Model-agnostic Explanations (LIME)



(Figure from Ribeiro et al., 2016)

# Local Interpretable Model-agnostic Explanations (LIME)

Prediction probabilities



atheism

christian



## Text with highlighted words

From: johnchad@triton.unm.edu (jchadwic)

Subject: Another request for Darwin Fish

Organization: University of New Mexico, Albuquerque

Lines: 11

NNTP-Posting-Host: triton.unm.edu

Hello Gang,

There have been some notes recently asking where to obtain the DARWIN fish.

This is the same question I have and I have not seen an answer on the net. If anyone has a contact please post on the net or email me.

(Figure from <https://github.com/marcotcr/lime>)

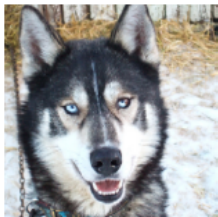
# Local Interpretable Model-agnostic Explanations (LIME)

Explaining prediction of 'Cat' in pros and cons



(Figure from <https://github.com/marcotcr/lime>)

# Local Interpretable Model-agnostic Explanations (LIME)

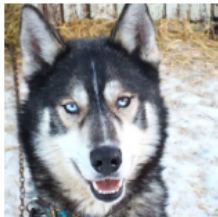


(a) Husky classified as wolf

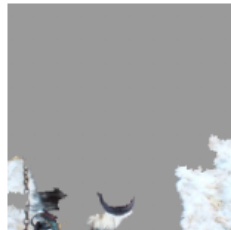
(Figure from Ribeiro et al., 2016)



# Local Interpretable Model-agnostic Explanations (LIME)



(a) Husky classified as wolf



(b) Explanation

(Figure from Ribeiro et al., 2016)

# Feature selection

# Feature selection

## Example: MNE sample data

sensor space:

- 102 magnetometers, 204 gradiometers
- downsampled to 60 Hz
- $X = (123 * 306 * 43)$
- X has 13.158 features in each row and 1,613,145 data points in total

source space:

- 5124 source space points
- downsampled to 60 Hz
- $X = (123 * 5124 * 43)$
- X has 220.332 in each row and 27,100,836 data points in total

# Feature selection

before fitting

after fitting

# Feature selection

before fitting

- variance thresholding
- univariate feature selection
  - ▶ select k best features
  - ▶ select percentile
  - ▶  $\chi^2$ , f-test

after fitting

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## before fitting

- variance thresholding
- univariate feature selection
  - ▶ select k best features
  - ▶ select percentile
  - ▶  $\chi^2$ , f-test

## after fitting

- select based on weights/coefficients
- recursive feature elimination
- model based:
  - ▶ l1-based feature selection
  - ▶ feature importance from a tree based model

# Questions?

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# References I

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