

CONSIDER  $\mathcal{B} = \{u \in \tau(a, b) \mid (a, b) \in \tau\}$

Then:  $\mathcal{P} = \{u \subseteq \tau(T) \mid \forall x \in u \exists B \in \mathcal{B} \text{ st } (x \in B) \wedge (B \subseteq u)\}$

By Thm, this is a topology, (Munkres)

NOW consider the poset  $(\mathcal{P}, \subseteq) \equiv \mathcal{P}$

We know  $\Pi$  of  $(\mathcal{P}, \subseteq)$  is  $\tau(T)$

While,  $\perp$  is  $\emptyset$ , trivially.

AS WELL,  $\emptyset \subseteq u \forall u \in \mathcal{P}$ , So  $\mathcal{P}$  is a meet Semilattice

&  $u \in \tau(T) \forall u \in \mathcal{P}$ , So  $\mathcal{P}$  is a join Semilattice.

$\mathcal{P} = \bigwedge \text{mathfrak{P}}$ ,  $\mathcal{P} = \bigvee \text{mathfrak{P}}$