

$$\beta_j := \beta_0 - \alpha \left(\frac{\partial \text{RSS}}{\partial \beta} \right) \rightarrow \text{Error}$$

$$\frac{\partial \text{RSS}}{\partial \beta} = \frac{\partial (y_{\text{true}} - y_{\text{pred}})^2}{\partial \beta} \quad \text{--- (1)}$$

$$= \frac{1}{2} \frac{\partial (y_{\text{true}} - (\beta_0 + \vec{\beta}_1 x))^2}{\partial \beta} \quad \text{--- (2)}$$

Using Chain Rule $\rightarrow g(f(x))$

$$\textcircled{3} (y_{\text{true}} - (\beta_0 + \vec{\beta}_1 x)) \cdot \frac{\partial (y_{\text{true}} - (\beta_0 + \vec{\beta}_1 x))}{\partial \beta}$$

$$\textcircled{4} (y_{\text{true}} - (\beta_0 + \vec{\beta}_1 x)) \cdot 0 - (0 + 1(x))$$

$$\textcircled{5} (y_{\text{true}} - (\beta_0 + \vec{\beta}_1 x)) \cdot x$$

$$\boxed{\beta_j := \beta_0 - \alpha (y_{\text{true}} - (\beta_0 + \vec{\beta}_1 x)) \cdot x}$$