

**G T G T**

**5 E 5 E**

**N O N O**

**O S O S**

**G T G T**

**5 E 5 E**

**N O N O**

**O S O S**

**G T G T**

**5 E 5 E**

**CS 2614**  
**Second Midterm Exam**  
**Fall 2024**

Name: \_\_\_\_\_

Student Number: \_\_\_\_\_

*Solutions*

1. Place all bookbags and other materials in the back of classroom.
2. You may NOT use a calculator/phone/laptop in any way or have it at your desk.
3. No references are allowed.
4. State all assumptions and show your work.
5. Place your answer in the spaces provided.
6. Answer all questions

<b>Problem</b>	<b>% credit</b>
1 (10%)	
2 (10%)	
3 (20%)	
4 (15%)	
5 (15%)	
6 (10%)	
7 (20%)	
<b>Total</b>	

**Question 1 [10 marks]**

What is wrong with the following register transfer statements?

- a)  $zT: PC \leftarrow AR, PC \leftarrow PC+1$

PC cannot be simultaneously changed.

- b)  $xT: R1 \leftarrow R1', R1 \leftarrow R2$

R1 cannot be concurrently changed.

**Question 2 [10 marks]**

Design a combinational circuit using a Read-Only Memory (ROM) that converts a 3-bit binary input representing a decimal number (0 to 7) into its corresponding Gray code output. Gray code is a binary numeral system where two successive values differ in only one bit.

- (a) Draw the truth table showing the 3-bit binary input values (000 to 111) and their respective Gray code outputs. [5 marks]

INPUT			OUTPUT		
$x_2$	$x_1$	$x_0$	$y_2$	$y_1$	$y_0$
0	0	0	0	0	0
0	0	1	0	0	1
0	1	0	0	1	1
0	1	1	0	1	0
1	0	0	1	1	0
1	0	1	1	0	1
1	1	0	1	0	0
1	1	1	0	0	0

- (b) Determine the required size of the ROM (in terms of addressable memory locations and bits per location). [5 marks]

$$8 \times 3 = 24 \text{ bits}$$

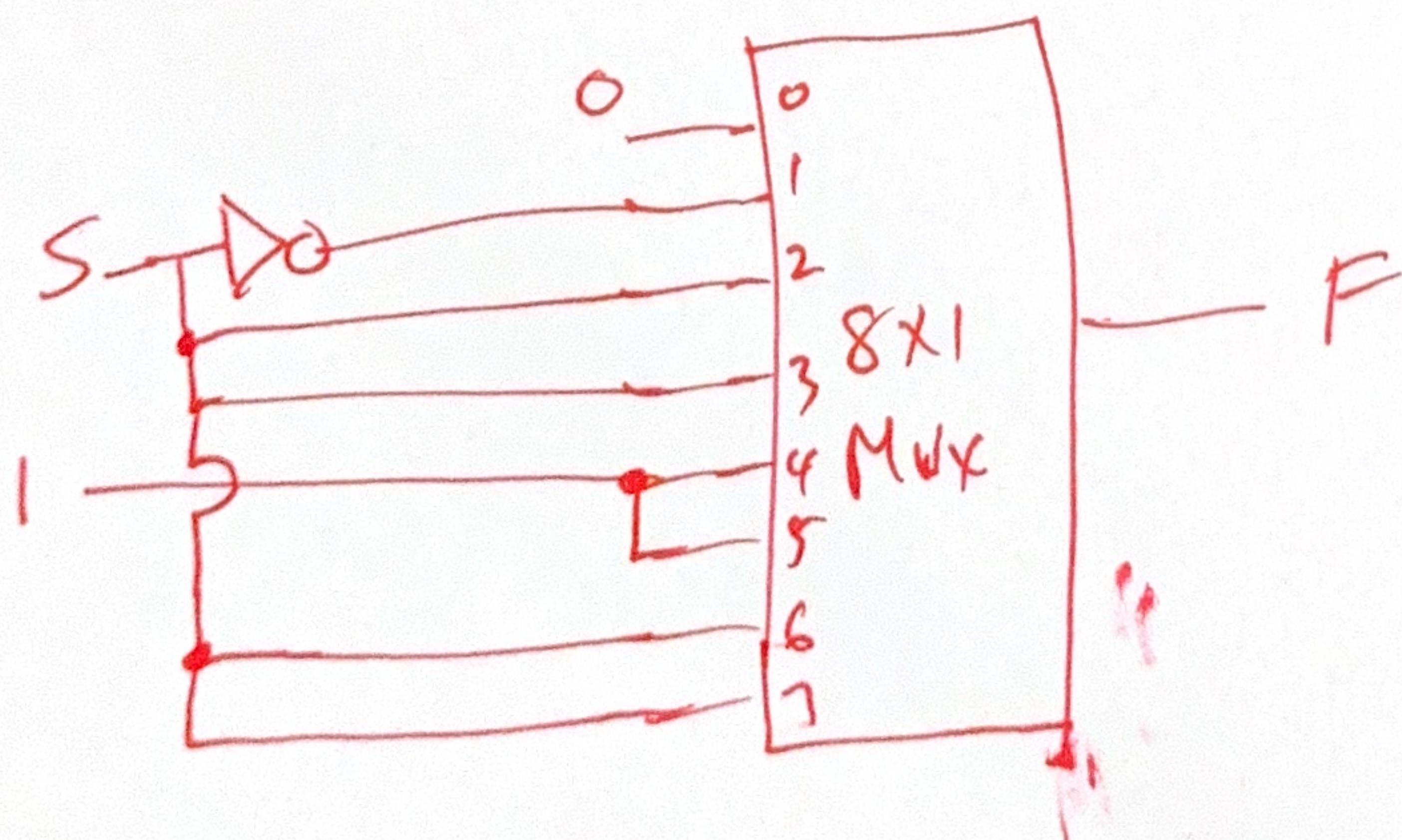
**Question 3 [20 marks]**

We want to implement the following Boolean function with an 8x1 multiplexer.  
 $F(P, Q, R, S) = \sum(2, 5, 7, 8, 9, 10, 11, 13, 15)$

- (a) Complete the truth table for the function F

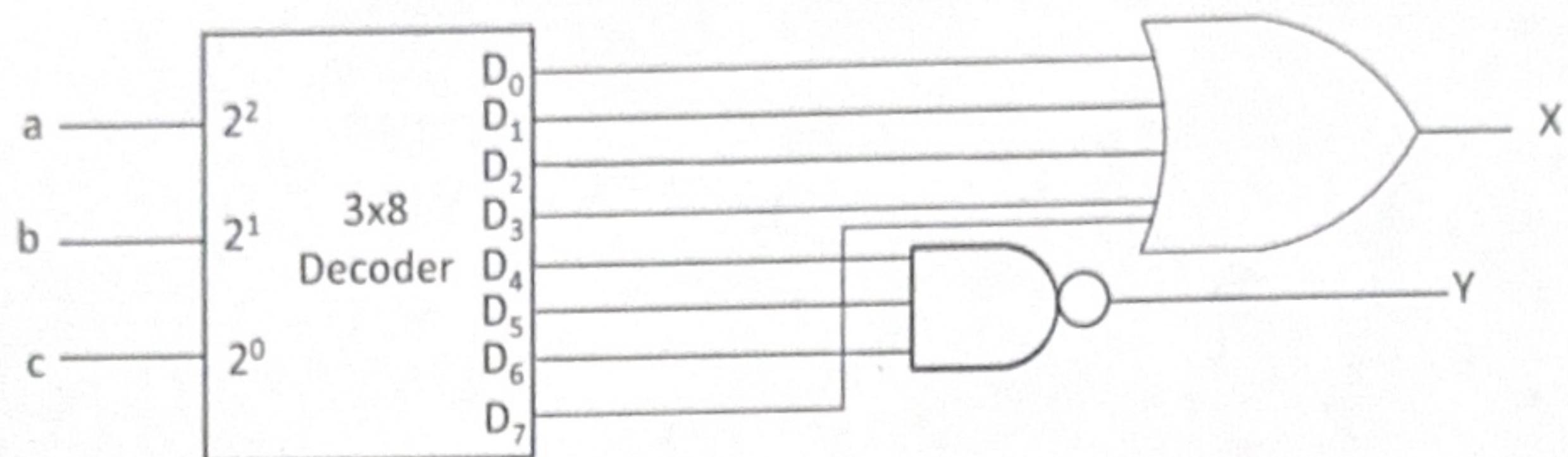
P	Q	R	S	F	$F=0$
0	0	0	0	0	{ 0
0	0	0	1	0	{ 0
0	0	1	0	1	{ S'
0	0	1	1	0	{ S
0	1	0	0	0	{ S
0	1	0	1	1	{ S
0	1	1	0	0	{ S
0	1	1	1	1	{ 1
1	0	0	0	1	{ 1
1	0	0	1	1	{ 1
1	0	1	0	1	{ 1
1	0	1	1	1	{ S
1	1	0	0	0	{ S
1	1	0	1	1	{ S
1	1	1	0	0	{ S
1	1	1	1	1	

- (b) Implement the function in part (a) using an **8 x 1** multiplexer.



**Question 4 [15 marks]**

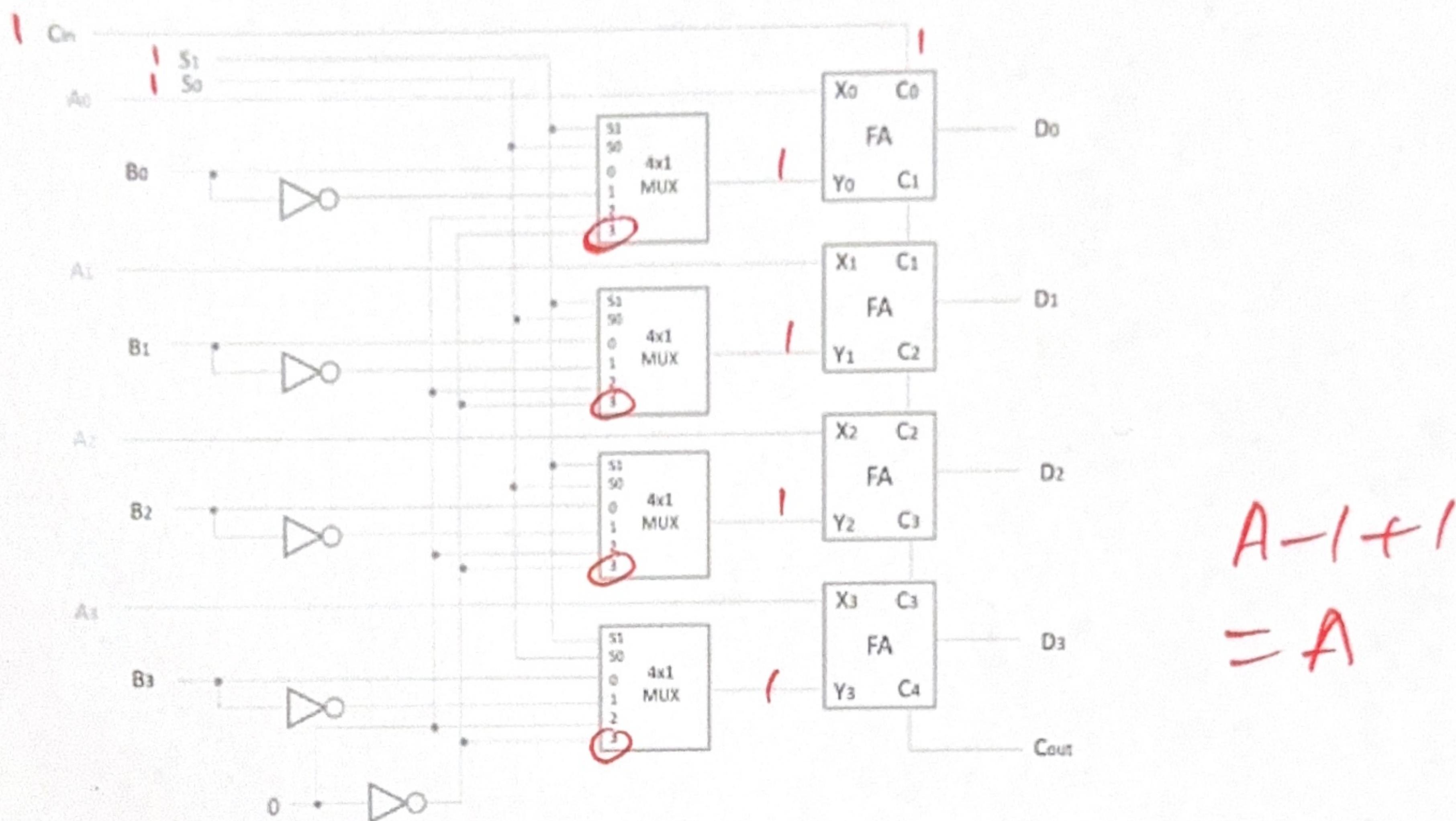
Fill in the truth table for the output functions X, Y of the circuit shown below.



A	B	C	X	Y
0	0	0	1	1
0	0	1	1	1
0	1	0	1	1
0	1	1	1	1
1	0	0	0	1
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

### Question 5 [15 marks]

Consider the following 4-bit arithmetic circuit where  $A_0$  to  $A_3$ , and  $B_0$  to  $B_3$  are the bits of two registers A and B.  $S_1$ ,  $S_0$  and  $C_{in}$  are the select inputs.



If the select inputs  $S_1 = 1$ ,  $S_0 = 1$ ,  $C_{in} = 1$ , what arithmetic operation is performed by the circuit?

Ans: Transfer.

**Question 6 [10 marks]**

We want to complement the four least significant bits of Register A by Exclusive Or (XOR) operation of Register A with another Register B. Specify the contents of Register B. All registers are 8 bits wide.

$$\begin{array}{r} A = x \ x \ x \ x \ x \ x \\ B = 0 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \\ \hline x \ x \ x \ x \ x' x' x' \end{array}$$

Ans: B= 0000 1111

**Question 7 [20 marks]**

The 8-bit registers AR, BR, CR and DR initially have the following values:

$$\begin{aligned} AR &= 11110010 = F2 \\ BR &= 11111111 = FF \\ CR &= 10111001 = B9 \\ DR &= 11101010 = EA \end{aligned}$$

Determine the 8-bit values in each register after the execution of the following INDEPENDENT microoperations. Specify the values in hexadecimal numbers.

	AR	BR	CR	DR
$AR \leftarrow AR + BR$	F1	FF	B9	EA
$CR \leftarrow CR \setminus DR, BR \leftarrow BR + 1$	F2	00	A8	EA
$AR \leftarrow AR - CR$	39	FF	B9	<del>39</del> EA

a) 
$$\begin{array}{r} 1111111 \\ 11110010 \\ + 1111111 \\ \hline \boxed{1} 11110001 = F1_H \end{array}$$

b) 
$$\begin{array}{r} 10111001 \\ 11101010 \\ \wedge \\ \hline CR = 10101000 = A8_H \end{array}$$

$$BR = \frac{+}{\overline{10000000}} = 00$$

c) 
$$\begin{array}{r} 11110010 \\ (CR)' 01000111 \\ + \\ \hline DR = \boxed{1} 00111001 = 39_H \end{array}$$

$$\begin{array}{l} CR = 10111001 \\ (CR)' = 01000111 \end{array}$$