

Architecture: circuits, assembly vs. machine languages

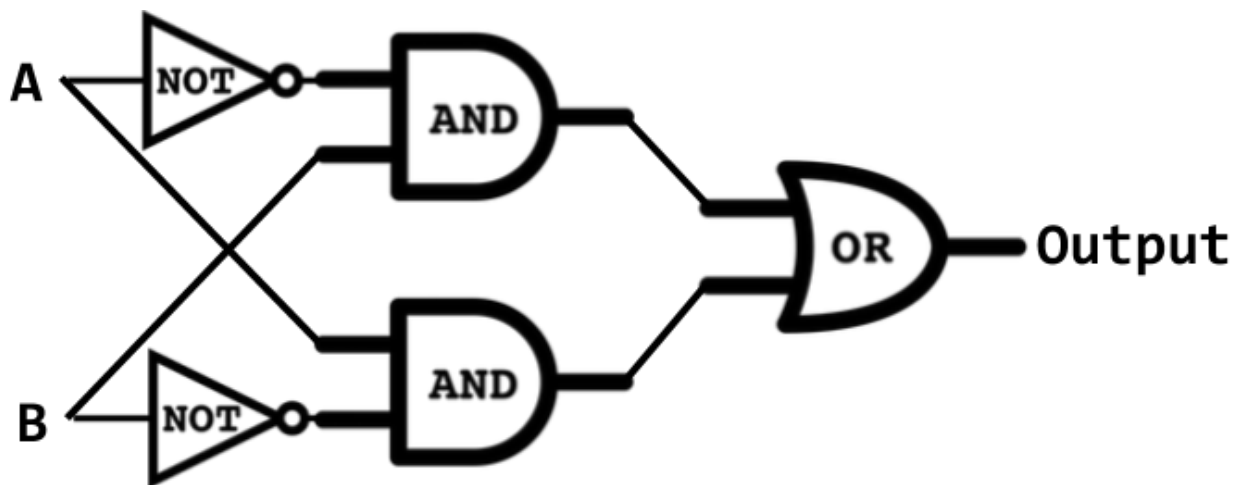
COSC 208, Introduction to Computer Systems, 2022-03-10

1-bit circuits

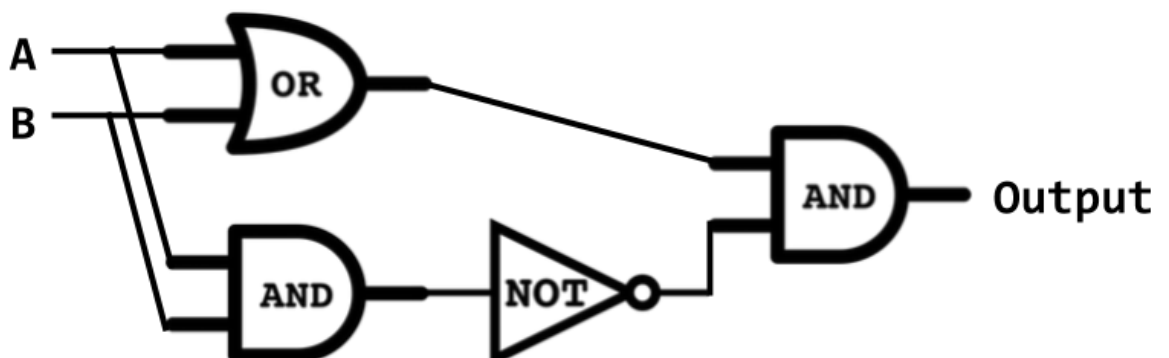
- Connect logic gates to perform a more complex operation
- Design the truth table: e.g., $A \neq B$

A	B	$A \neq B$
0	0	0
0	1	1
1	0	1
1	1	0

- For each row where the output value is 1:
 - Determine how to make each input 1 — e.g., either A or $\text{NOT}(A)$
 - Conjoin the two subexpressions — e.g., $\text{NOT}(A) \text{ AND } B$
- Create the disjunction of the expressions for each row — e.g., $(\text{NOT}(A) \text{ AND } B) \text{ OR } (A \text{ AND } \text{NOT}(B))$
- Create a circuit from left to right, starting with the inner-most subexpressions



- Can we build a circuit that uses fewer gates?
 - $A \text{ XOR } B$
 - $(A \text{ OR } B) \text{ AND } (\text{NOT } (A \text{ AND } B))$



Q1: Create a 1-bit circuit for $A \leq B$ using *AND*, *OR*, *NOT* gates

A	B	$A \leq B$
–	–	-----
0	0	1
0	1	1
1	0	0
1	1	1

$((\text{NOT } A) \text{ AND } (\text{NOT } B)) \text{ OR}$
 $((\text{NOT } A) \text{ AND } B) \text{ OR}$
 $(A \text{ AND } B)$