

**Exercise 1:** Write a function that computes the level of output generated by a constant returns to scale Cobb-Douglas production function, i.e., such that it computes  $A \cdot K^\alpha \cdot L^{1-\alpha}$ .

```
In [1]: # Exercise 1:
def cobbdouglas(K=1, L=1, A=1, alpha=0.3):
    y = A * (K**alpha) * (L**(1-alpha))
    return y
print(cobbdouglas(4,9,2,0.5))
#12.0
```

12.0

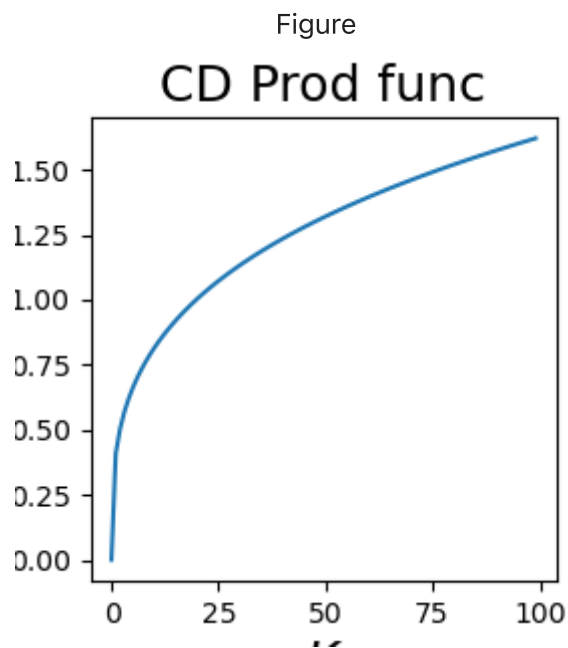
**Exercise 2:** Use the function you created and plot the production function as a function of  $K$  for given values of  $A$  and  $L$ . **Hint:** Use the `np.linspace(0, 5, 100)` function to create an array of values of  $K$  with 100 point between 0 and 5.

```
In [27]: # Exercise 2:
import numpy as np
import matplotlib as mpl
import matplotlib.pyplot as plt
%matplotlib widget

K = np.linspace(0,5,100)
i=0
while i in K:
    cobbdouglas(K[i])
    i += 1
    break

fig, CD = plt.subplots(figsize=(3,3))
CD.plot(cobbdouglas(K))
CD.label=(r'$y=A*(K**alpha)*(L**(1-alpha))$')
CD.set_xlabel(r'$K$', fontsize=18)
CD.set_ylabel(r'$Y$', fontsize=18)
CD.set_title(r'CD Prod func', fontsize=18)
```

Out[27]: Text(0.5, 1.0, 'CD Prod func')



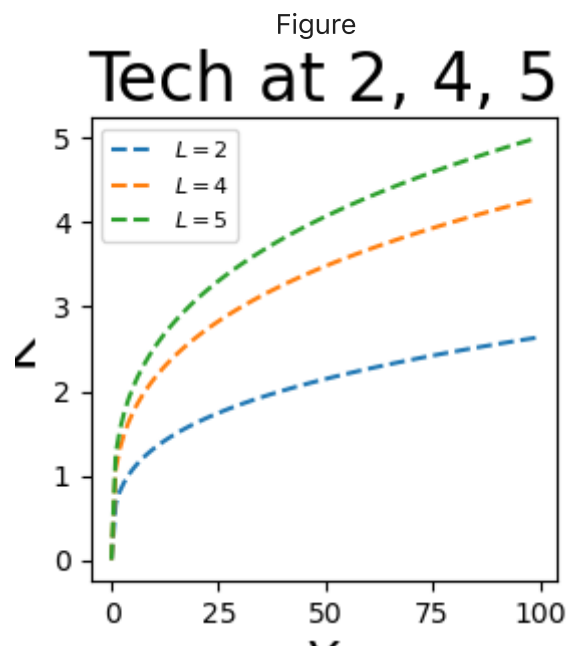
**Exercise 3:** Show with a plot the effect of increasing  $A$  from 1 to 2, 4, or 5.

```
In [28]: # Exercise 3:
fig, A = plt.subplots(figsize=(3,3))

A.plot(cobbdouglas(K,2), linestyle='--', label=r'$L=2$')
A.plot(cobbdouglas(K,4), linestyle='--', label=r'$L=4$')
A.plot(cobbdouglas(K,5), linestyle='--', label=r'$L=5$')
A.set_title(r'Tech at 2, 4, 5', fontsize=24)
A.set_xlabel(r'$Y$', fontsize=18)
A.set_ylabel(r'$K$', fontsize=18)

plt.legend(fontsize=8)
```

Out[28]: <matplotlib.legend.Legend at 0x16a4e7cd0>



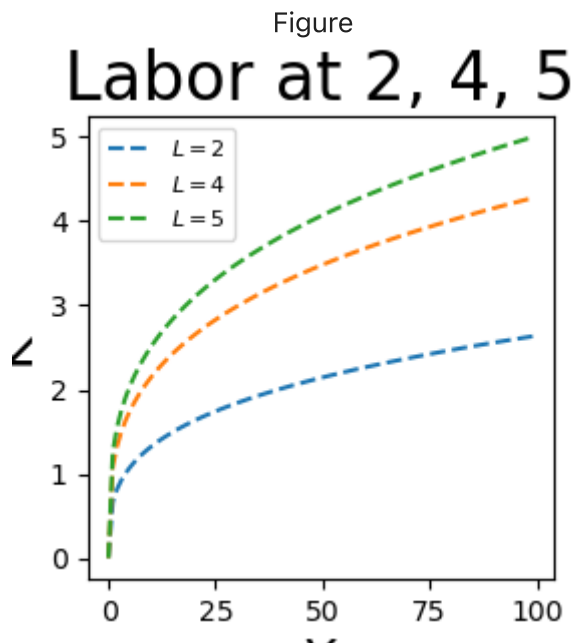
**Exercise 4:** Show with a plot the effect of increasing  $L$  from 1 to 2, 4, 5.

```
In [29]: # Exercise 4:
fig, L = plt.subplots(figsize=(3,3))

L.plot(cobbdouglas(K,2), linestyle='--', label=r'$L=2$')
L.plot(cobbdouglas(K,4), linestyle='--', label=r'$L=4$')
L.plot(cobbdouglas(K,5), linestyle='--', label=r'$L=5$')
L.set_title(r'Labor at 2, 4, 5', fontsize=24)
L.set_xlabel(r'$Y$', fontsize=18)
L.set_ylabel(r'$K$', fontsize=18)

plt.legend(fontsize=8)
```

Out[29]: <matplotlib.legend.Legend at 0x16a4a32e0>



**Exercise 5:** Save the previous plots into **png**, **jpeg**, and **pdf** files.

```
In [5]: # Exercise 5:
plt.savefig('./pics/cobbdouglas.png')
plt.savefig('./pics/cobbdouglas.pdf')
plt.savefig('./pics/cobbdouglas.jpeg')
```