

Neural Language Models

Week 2 - Word Embeddings and Word2Vec

NLP Course 2025

September 28, 2025

Using Optimal Readability Template

From Words as IDs to Words as Meanings

The Problem

- Words are just **IDs**
- No semantic similarity
- "cat" and "dog" equally different as "cat" and "democracy"
- Can't generalize

The Solution

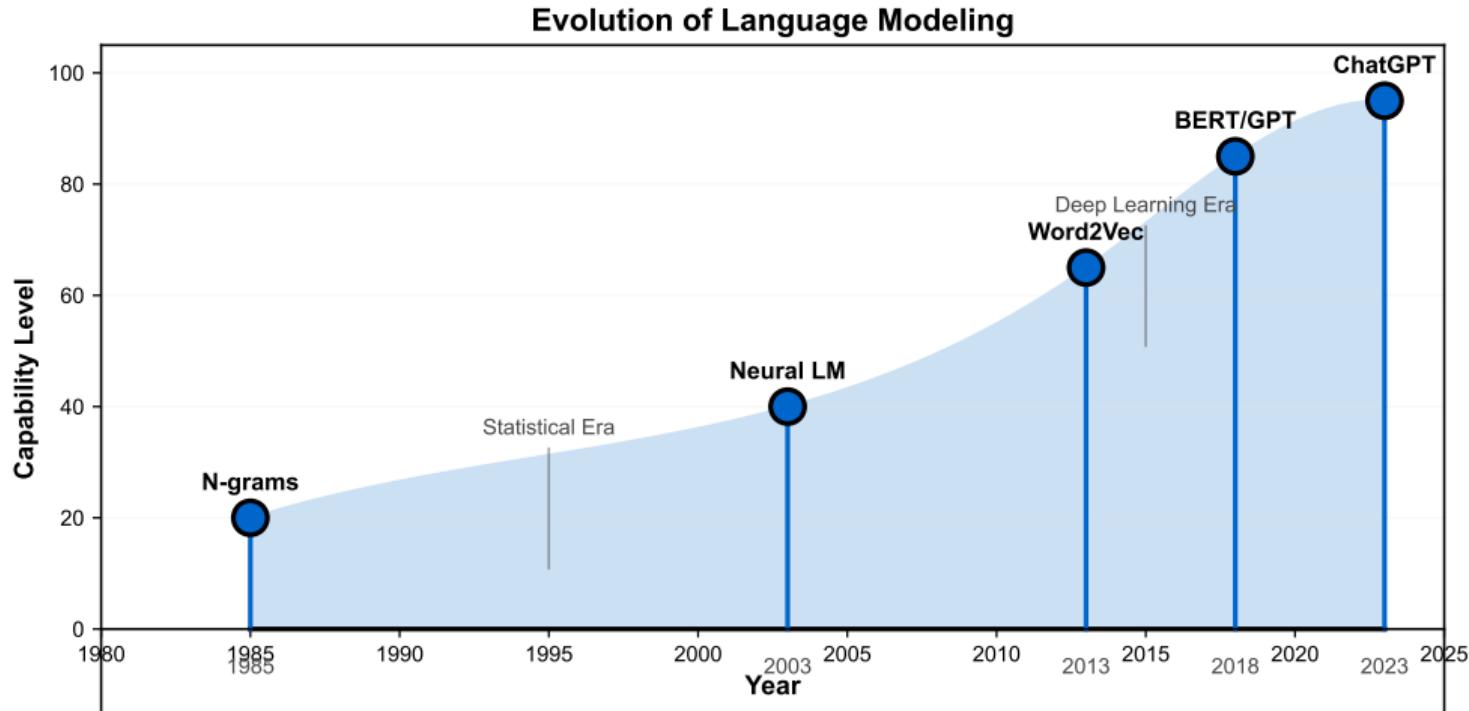
- Words as **vectors**
- Similar words nearby
- Math operations work!
- King - Man + Woman = Queen

The Impact

- Powers all modern NLP
- **1M+** developers use
- Semantic search
- Foundation for GPT/BERT

Core Insight: You shall know a word by the company it keeps

The Evolution of Language Modeling



Interactive: Word Association Game

Fill in the blank:

1. The cat sat on the _____
2. I drink my coffee with milk and _____
3. The capital of France is _____
4. She opened the door with her _____

How did you know?

- Context provides meaning
- Similar contexts → similar words
- Pattern recognition

This is Word2Vec's insight:

- Learn from **billions** of contexts
- Words in similar contexts get **similar vectors**
- Mathematics captures semantics

Where Word Embeddings Power Your Life (2025)

Search Engines

- Google semantic search
- Bing neural matching
- DuckDuckGo instant answers

Translation

- Google Translate
- DeepL
- Microsoft Translator

Business Tools

- Grammarly corrections
- Resume matching
- Customer support bots

Virtual Assistants

- Siri/Alexa understanding
- Google Assistant
- ChatGPT responses

Recommendations

- Netflix shows
- Spotify Discover
- YouTube suggestions

Market Size

- \$2.7B by 2025
- 1M+ developers
- 500M+ daily users

The 2013 Breakthrough: Mathematical Semantics

$$\text{King} - \text{Man} + \text{Woman} = \text{Queen}$$

The Discovery:

- Vectors encode **relationships**
- Arithmetic operations preserve meaning
- Geometry captures semantics

Why This Matters:

- Computers understand **analogies**
- Transfer learning possible
- One model, many tasks
- Foundation for all modern NLP

More Examples:

- Paris - France + Italy = **Rome**
- Bigger - Big + Small = **Smaller**
- Walking - Walk + Swim = **Swimming**

Word2Vec paper: 16,000+ citations

Semantic relationships become vector arithmetic

The Distributional Hypothesis

Linguistic Foundation (1954):

"You shall know a word by the company it keeps" - J.R. Firth

What it means:

- Words with similar **contexts** have similar **meanings**
- Context = surrounding words
- Meaning emerges from usage

Example contexts for "bank":

- "deposit money in the bank"
- "sitting by the river bank"
- Different contexts → different meanings

How Word2Vec uses this:

1. Scan billions of sentences
2. Track which words appear together
3. Words in similar contexts get similar vectors
4. Geometry encodes semantics

The Magic:

- No human labeling needed
- Learns from raw text
- Scales to millions of words
- Works for any language

From Sparse to Dense: The Representation Revolution

One-Hot Encoding (Old Way):

- Vocabulary size: 50,000
- cat = [0,0,1,0,0,...,0]
- dog = [0,0,0,1,0,...,0]

Dense Embeddings (Word2Vec):

- Embedding size: 300
- cat = [0.2, -0.4, 0.7, ...]
- dog = [0.3, -0.3, 0.6, ...]

Problems:

- 50,000 dimensions!
- No similarity: $\text{cat} \cdot \text{dog} = 0$
- Can't generalize
- Massive memory usage

Benefits:

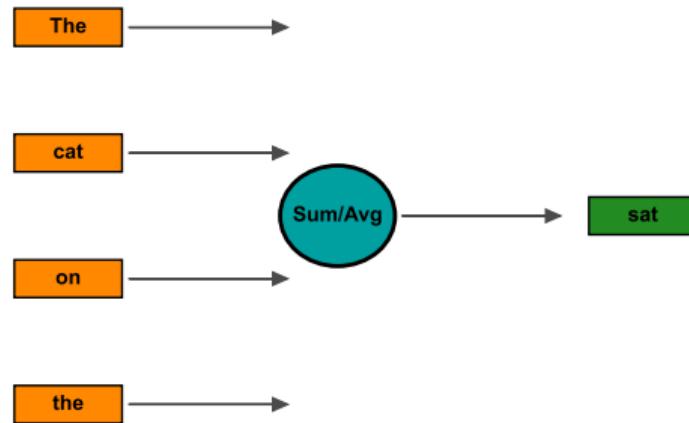
- 99.4% smaller!
- Similarity: $\text{cat} \cdot \text{dog} = 0.8$
- Generalizes to new contexts
- Efficient computation

From 50,000 sparse dimensions to 300 dense dimensions

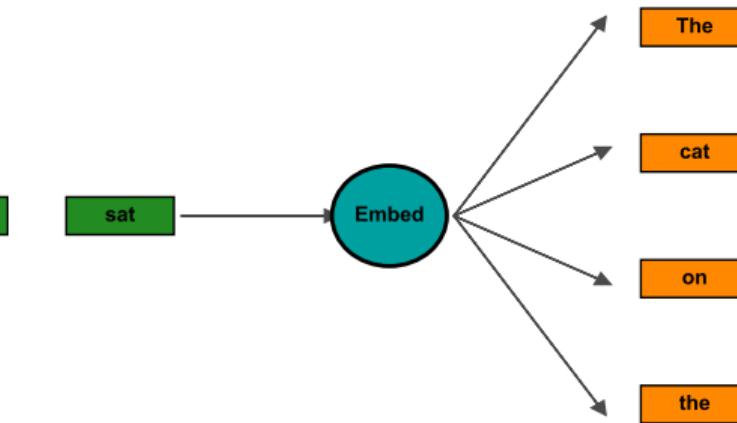
Word2Vec: Two Architectures

Word2Vec Architecture Comparison

CBOW: Context → Center



Skip-gram: Center → Context



Skip-gram: The Architecture That Won

Training Objective: Predict context from center word

Given: "The cat sat on the mat"

Input: "cat" (center word)

Outputs to predict:

- "The" (position -1)
- "sat" (position +1)
- Sometimes: "on" (+2), "the" (-2)

Window size = 2:

- Look 2 words left/right
- 4 predictions per center word
- More context = better vectors

Why Skip-gram wins:

- Better on **rare words**
- More training examples
- Superior semantic quality
- Used by Google, Facebook

Training data from one sentence:

- (cat, The)
- (cat, sat)
- (sat, cat)
- (sat, on)
- ... many more pairs

Building Word2Vec in PyTorch

```
1 import torch
2 import torch.nn as nn
3
4 class Word2Vec(nn.Module):
5     def __init__(self, vocab_size, embed_dim):
6         super().__init__()
7         # Two embedding matrices
8         self.center_embeddings = nn.Embedding(
9             vocab_size, embed_dim
10        )
11         self.context_embeddings = nn.Embedding(
12             vocab_size, embed_dim
13        )
14
15     def forward(self, center, context):
16         # Get embeddings
17         center_embeds = self.center_embeddings(center)
18         context_embeds =
19             self.context_embeddings(context)
20
21         # Dot product = similarity
22         scores = torch.sum(
23             center_embeds * context_embeds, dim=1
24        )
25
26         return scores
```

Key Design Choices:

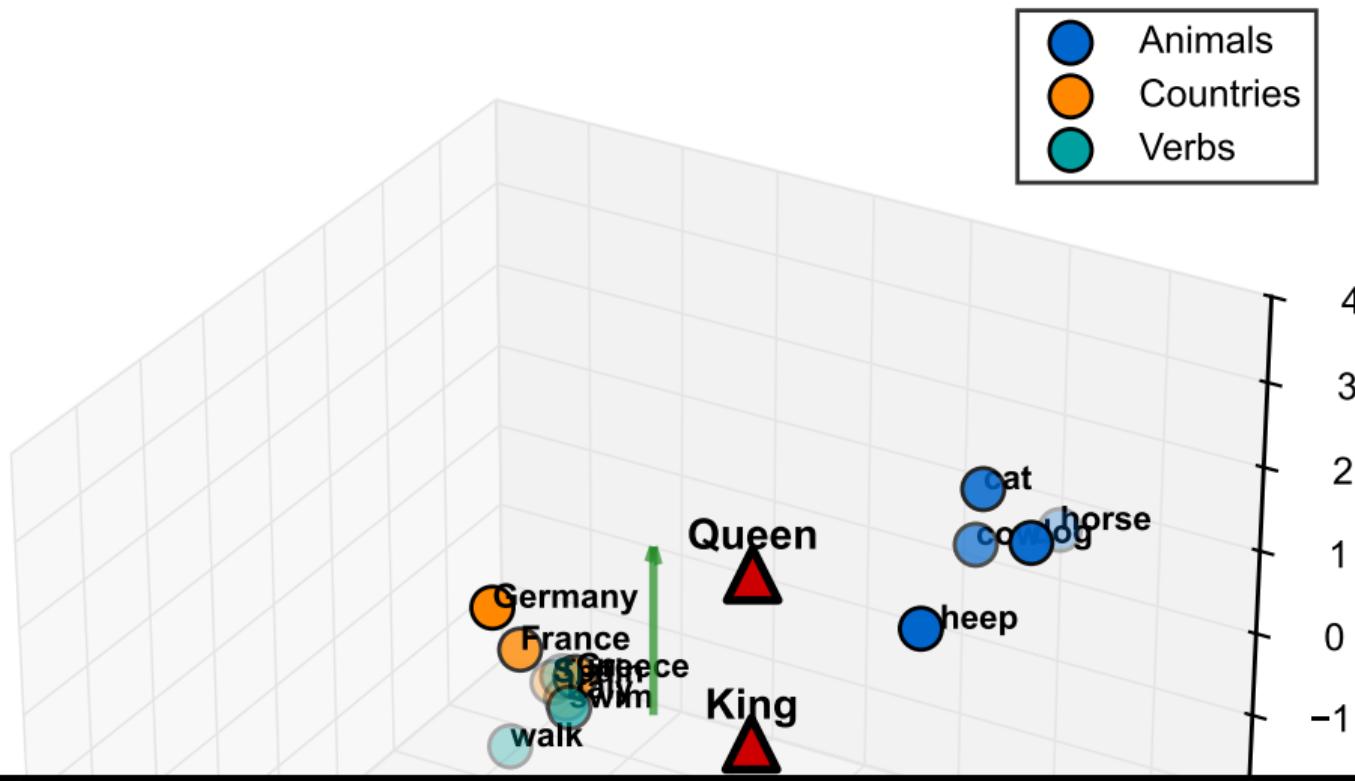
- **Two matrices:** center and context
- Embedding dim: typically **300**
- Dot product for similarity
- Simple = fast training

Training Process:

1. Sample (center, context) pairs
2. Compute similarity scores
3. Maximize correct pairs
4. Minimize random pairs

Full implementation: 50 lines of code!

Word Embeddings in 3D Space



The Softmax Challenge

Converting scores to probabilities:

$$\text{softmax}(z_i) = \frac{e^{z_i}}{\sum_{j=1}^V e^{z_j}}$$

The Problem:

- Vocabulary size $V = 50,000$
- Must compute all 50,000 scores
- Denominator sums 50,000 exponentials
- Every training step!

Computational cost:

- Per sample: $O(V \cdot d)$
- 1B training samples
- = 15 trillion operations

The Solution: Negative Sampling

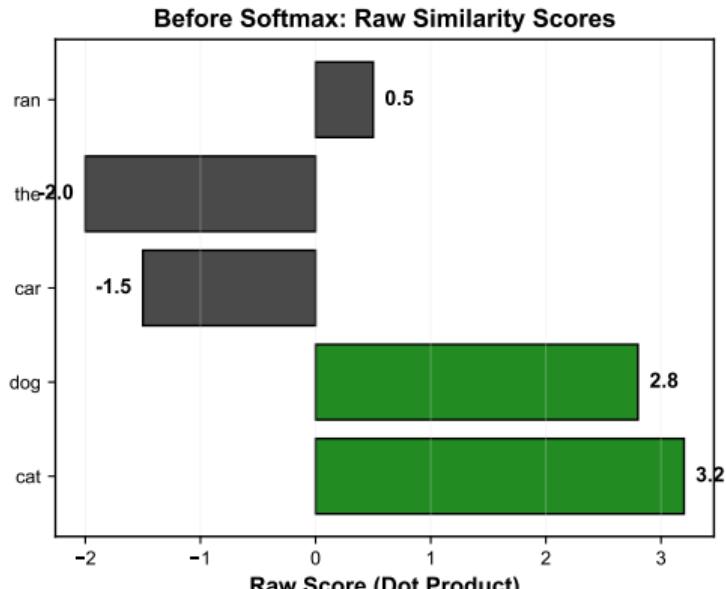
- Don't compute all 50,000
- Just sample 5-20 negatives
- 99.96% speedup!
- Quality stays the same

New objective:

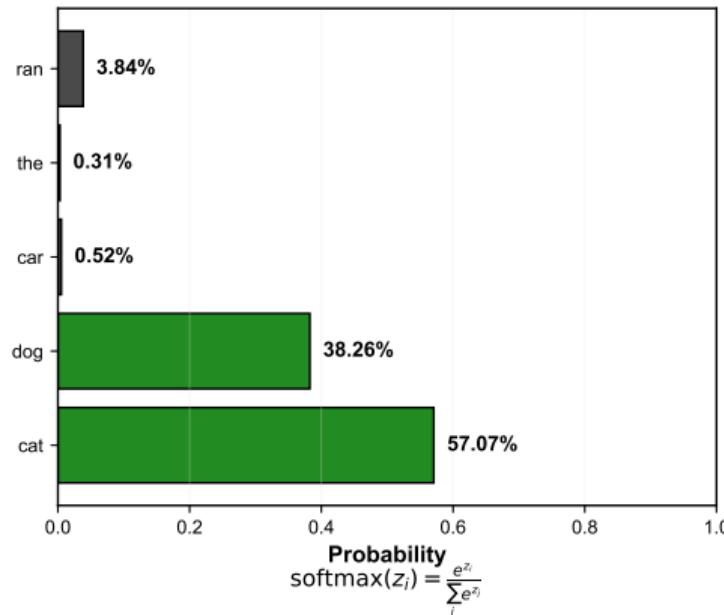
- Maximize: $P(\text{correct context})$
- Minimize: $P(\text{random words})$
- Binary classification $\times 6$
- Much faster training

Softmax Computation Explained

Softmax: Converting Scores to Probabilities



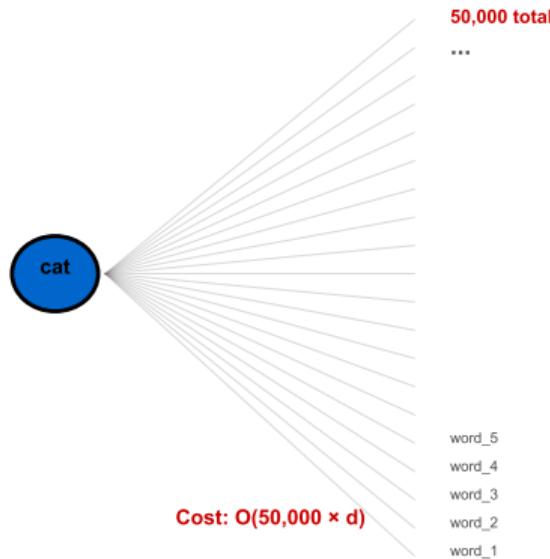
After Softmax: Normalized Probabilities



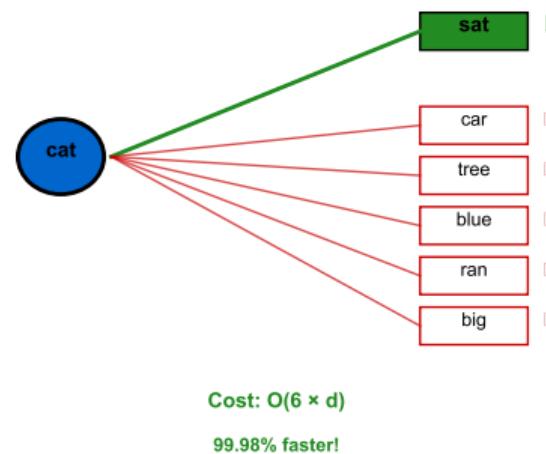
Negative Sampling: Before and After

Negative Sampling: The Optimization That Made Word2Vec Practical

Full Softmax: Compute All 50,000 Words

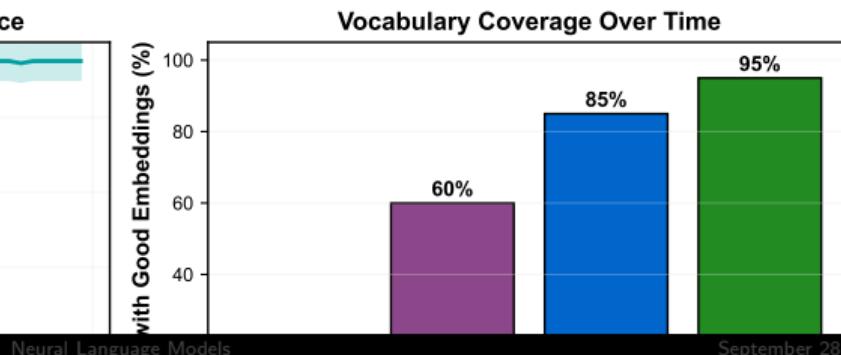
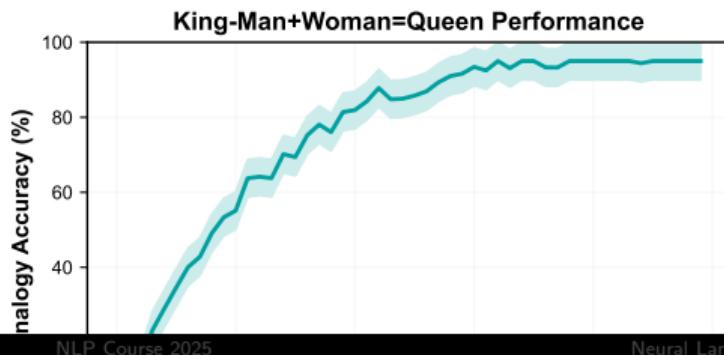
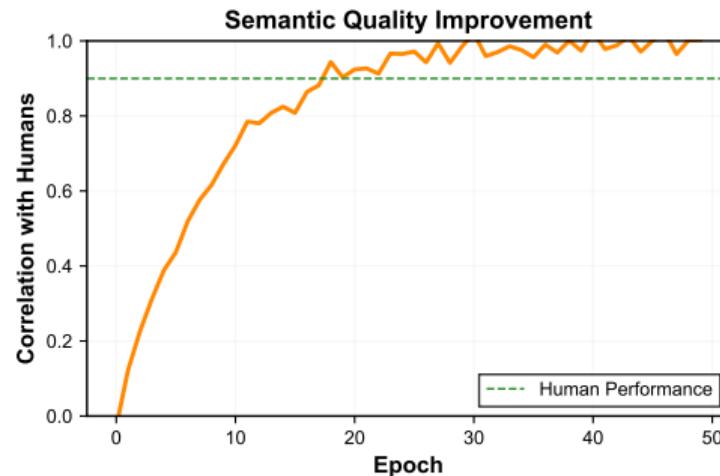
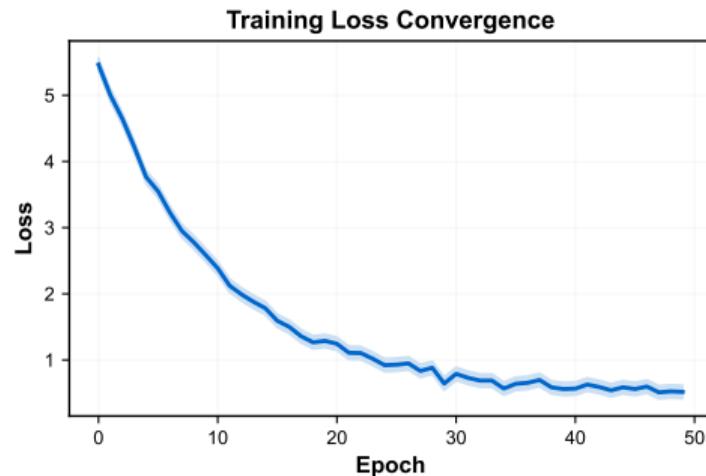


Negative Sampling: Only 5-20 Words



Training Dynamics and Convergence

Word2Vec Training Dynamics



Semantic Arithmetic in Action

Semantic Arithmetic: Mathematical Operations on Meaning

Gender Relationship

$$\begin{array}{ccccc} \text{King} & - & \text{Man} & + & \text{Woman} \\ & & & & = \\ & & & & \text{Queen} \end{array}$$

Capital Cities

$$\begin{array}{ccccc} \text{Paris} & - & \text{France} & + & \text{Italy} \\ & & & & = \\ & & & & \text{Rome} \end{array}$$

Verb Conjugation

$$\begin{array}{ccccc} \text{Walking} & - & \text{Walk} & + & \text{Swim} \\ & & & & = \\ & & & & \text{Swimming} \end{array}$$

Comparative Forms

$$\begin{array}{ccccc} \text{Bigger} & - & \text{Big} & + & \text{Small} \\ & & & & = \\ & & & & \text{Smaller} \end{array}$$

How Do We Know It Works?

Intrinsic Evaluation:

Word Similarity Tasks:

- Human ratings: cat-dog = 7.5/10
- Model similarity: cosine(cat, dog)
- Correlation with humans
- WordSim-353 dataset

Analogy Tasks:

- a:b :: c:?
- Berlin:Germany :: Paris:?
- Google analogy dataset
- 90%+ accuracy

Extrinsic Evaluation:

Downstream Tasks:

- Sentiment analysis
- Named entity recognition
- Machine translation
- Question answering

Real-world metrics:

- Search relevance ↑15%
- Translation BLEU ↑3.2
- Classification F1 ↑8%
- All from better embeddings!

Good embeddings improve everything downstream

Challenges: Not Everything Is Perfect

1. Polysemy Problem:

- "bank" (financial) = "bank" (river)
- One vector for all meanings
- Averages different senses
- Solution: Contextual embeddings (BERT)

2. Rare Words:

- Need many examples
- "serendipity" appears rarely
- Poor vectors for rare words
- Solution: Subword embeddings

3. Bias Amplification:

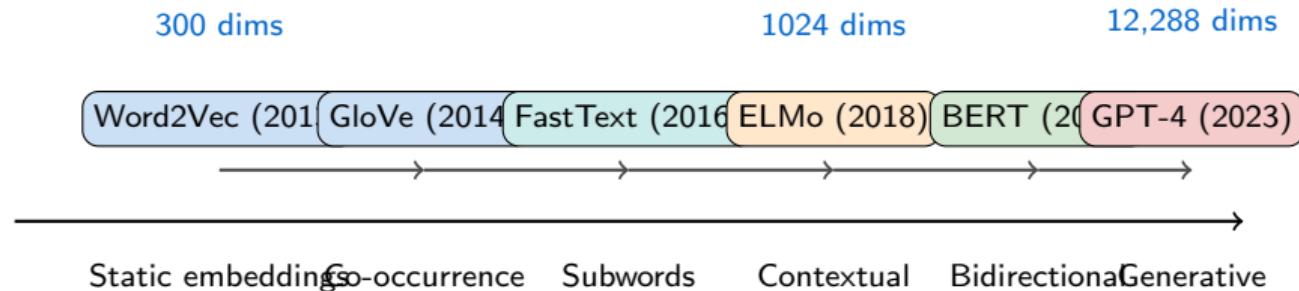
- Learns societal biases
- Doctor:Male :: Nurse:Female
- Amplifies stereotypes
- Active research area

4. Static Embeddings:

- Fixed after training
- Can't adapt to new contexts
- No fine-tuning possible
- Solution: Transformer models

These limitations led to BERT and GPT development

From Word2Vec to ChatGPT: The Journey



Word2Vec's Legacy:

- Proved embeddings work
- Inspired contextual models
- Still used in production
- Foundation for all modern NLP

What Changed:

- Static → Contextual
- 300 dims → 12,000+ dims
- Word-level → Subword
- Millions → Billions of parameters

Build It: Semantic Search Engine

```
1 import numpy as np
2 from gensim.models import Word2Vec
3
4 def semantic_search(query, documents, model):
5     """Find semantically similar documents"""
6
7     # Vectorize query
8     query_vec = document_vector(query, model)
9
10    # Vectorize all documents
11    doc_vectors = [
12        document_vector(doc, model)
13        for doc in documents
14    ]
15
16    # Compute similarities
17    similarities = [
18        cosine_similarity(query_vec, doc_vec)
19        for doc_vec in doc_vectors
20    ]
21
22    # Return ranked results
23    ranked = sorted(
24        zip(documents, similarities),
25        key=lambda x: x[1],
26        reverse=True
27    )
28
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```

How it works:

1. Convert query to vector
2. Convert documents to vectors
3. Find nearest neighbors
4. Return ranked results

Real Examples:

Query: "animal pets"

Results:

- "dog training tips"
- "cat care guide"
- "hamster habitats"

No keyword matching needed!

Week 2 Summary: Words Have Meaning!

- Words as **IDs** → Words as **vectors**
- Distributional hypothesis: **Context defines meaning**
- Word2Vec: **Skip-gram** + **Negative sampling**
- Mathematical semantics: King - Man + Woman = Queen
- From 50,000 sparse → **300 dense** dimensions
- Powers modern NLP: Search, translation, chatbots
- Limitations led to BERT/GPT development

Key Technical Insights:

- Dot product captures similarity
- Negative sampling avoids softmax bottleneck
- Embeddings are the foundation of all modern NLP

Next Week: Recurrent Neural Networks
How do we process sequences using embeddings?