

Question 1.

1. Consider a 1-dimensional time-series with values $[2, 1, 3, 4, 7]$.
Perform a convolution with a 1-dimensional filter $[1, 0, 1]$ without padding.

$$(2*1) + (1*0) + (3*1) = 5$$

$$(1*1) + (3*0) + (4*1) = 5$$

$$(3*1) + (4*0) + (7*1) = 10$$

$$[5, 5, 10]$$

2. Compute the convolution of the below input with the horizontal edge detection filter.
Use a stride of 1 without padding.

6	3	4	4	5	0	3
4	7	4	0	4	0	4
7	0	2	3	4	5	2
3	7	5	0	3	0	7
5	8	1	2	5	4	2
8	0	1	0	6	0	0
6	4	1	3	0	4	5

INPUT

1	1	1
0	0	0
-1	-1	-1

HORIZONTAL EDGE
DETECTING FILTER

$$(6*1) + (3*1) + (4*1) + (4*0) + (7*0) + (4*0) + (7*-1) + (0*-1) + (2*-1) = 4$$

$$(3*1) + (4*1) + (4*1) + (7*0) + (4*0) + (0*0) + (0*-1) + (2*-1) + (3*-1) = 6$$

$$(4*1) + (4*1) + (5*1) + (4*0) + (0*0) + (4*0) + (2*-1) + (3*-1) + (4*-1) = 4$$

$$(4*1) + (5*1) + (0*1) + (0*0) + (4*0) + (0*0) + (3*-1) + (4*-1) + (5*-1) = -3$$

$$(5*1) + (0*1) + (3*1) + (4*0) + (0*0) + (4*0) + (4*-1) + (5*-1) + (2*-1) = -3$$

$$(4*1) + (7*1) + (4*1) + (7*0) + (0*0) + (2*0) + (3*-1) + (7*-1) + (5*-1) = 0$$

$$(7*1) + (4*1) + (0*1) + (0*0) + (2*0) + (3*0) + (7*-1) + (5*-1) + (0*-1) = -1$$

$$(4*1) + (0*1) + (4*1) + (2*0) + (3*0) + (4*0) + (5*-1) + (0*-1) + (3*-1) = 0$$

$$(0*1) + (4*1) + (0*1) + (3*0) + (4*0) + (5*0) + (0*-1) + (3*-1) + (0*-1) = 1$$

$$(4*1) + (0*1) + (4*1) + (4*0) + (5*0) + (2*0) + (3*-1) + (0*-1) + (7*-1) = -2$$

$$(7*1) + (0*1) + (2*1) + (3*0) + (7*0) + (5*0) + (5*-1) + (8*-1) + (1*-1) = -5$$

$$(0*1) + (2*1) + (3*1) + (7*0) + (5*0) + (0*0) + (8*-1) + (1*-1) + (2*-1) = -6$$

$$(2*1) + (3*1) + (4*1) + (5*0) + (0*0) + (3*0) + (1*-1) + (2*-1) + (5*-1) = 1$$

$$(3*1) + (4*1) + (5*1) + (0*0) + (3*0) + (0*0) + (2*-1) + (5*-1) + (4*-1) = 1$$

$$(4*1) + (5*1) + (2*1) + (3*0) + (0*0) + (7*0) + (5*-1) + (4*-1) + (2*-1) = 0$$

$$\begin{aligned}
(3*1) + (7*1) + (5*1) + (5*0) + (8*0) + (1*0) + (8*-1) + (0*-1) + (1*-1) &= 6 \\
(7*1) + (5*1) + (0*1) + (8*0) + (1*0) + (2*0) + (0*-1) + (1*-1) + (0*-1) &= 11 \\
(5*1) + (0*1) + (3*1) + (1*0) + (2*0) + (5*0) + (1*-1) + (0*-1) + (6*-1) &= 1 \\
(0*1) + (3*1) + (0*1) + (2*0) + (5*0) + (4*0) + (0*-1) + (6*-1) + (0*-1) &= -3 \\
(3*1) + (0*1) + (7*1) + (5*0) + (4*0) + (2*0) + (6*-1) + (0*-1) + (0*-1) &= 4
\end{aligned}$$

$$\begin{aligned}
(5*1) + (8*1) + (1*1) + (8*0) + (0*0) + (1*0) + (6*-1) + (4*-1) + (1*-1) &= 3 \\
(8*1) + (1*1) + (2*1) + (0*0) + (1*0) + (0*0) + (4*-1) + (1*-1) + (3*-1) &= 3 \\
(1*1) + (2*1) + (5*1) + (1*0) + (0*0) + (6*0) + (1*-1) + (3*-1) + (0*-1) &= 4 \\
(2*1) + (5*1) + (4*1) + (0*0) + (6*0) + (0*0) + (3*-1) + (0*-1) + (4*-1) &= 4 \\
(5*1) + (4*1) + (2*1) + (6*0) + (0*0) + (0*0) + (0*-1) + (4*-1) + (5*-1) &= 2
\end{aligned}$$

4	6	4	-3	-3
0	-1	0	1	-2
-5	-6	1	1	0
6	11	1	-3	4
3	3	4	4	2

3. Perform a 4×4 max pooling at stride 1 of the above same input.

$$\begin{aligned}
\text{Max}(6,3,4,4,7,4,0,7,0,2,3,3,7,5,0) &= 7 \\
\text{Max}(3,4,4,5,7,4,0,4,0,2,3,4,7,5,0,3) &= 7 \\
\text{Max}(4,4,5,0,4,0,4,0,2,3,4,5,5,0,3,0) &= 5 \\
\text{Max}(4,5,0,3,0,4,0,4,3,4,5,2,0,3,0,7) &= 7
\end{aligned}$$

$$\begin{aligned}
\text{Max}(4,7,4,0,7,0,2,3,3,7,5,0,5,8,1,2) &= 8 \\
\text{Max}(7,4,0,4,0,2,3,4,7,5,0,3,8,1,2,5) &= 8 \\
\text{Max}(4,0,4,0,2,3,4,5,5,0,3,0,1,2,5,4) &= 5 \\
\text{Max}(0,4,0,4,3,4,5,2,0,3,0,7,2,5,4,2) &= 7
\end{aligned}$$

$$\begin{aligned}
\text{Max}(7,0,2,3,3,7,5,0,5,8,1,2,8,0,1,0) &= 8 \\
\text{Max}(0,2,3,4,7,5,0,3,8,1,2,5,0,1,0,6) &= 8 \\
\text{Max}(2,3,4,5,5,0,3,0,1,2,5,4,1,0,6,0) &= 6 \\
\text{Max}(3,4,5,2,0,3,0,7,2,5,4,2,0,6,0,0) &= 7
\end{aligned}$$

$$\begin{aligned}
\text{Max}(3,7,5,0,5,8,1,2,8,0,1,0,6,4,1,3) &= 8 \\
\text{Max}(7,5,0,3,8,1,2,5,0,1,0,6,4,1,3,0) &= 8 \\
\text{Max}(5,0,3,0,1,2,5,4,1,0,6,0,1,3,0,4) &= 6 \\
\text{Max}(0,3,0,7,2,5,4,2,0,6,0,0,3,0,4,5) &= 7
\end{aligned}$$

7	7	5	7
8	8	5	7
8	8	6	7
8	8	6	7