

# Longitudinal Control for Self-driving Cars

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## 1 Longitudinal control

### 2 Questions

1. What is the order of the following transfer function?

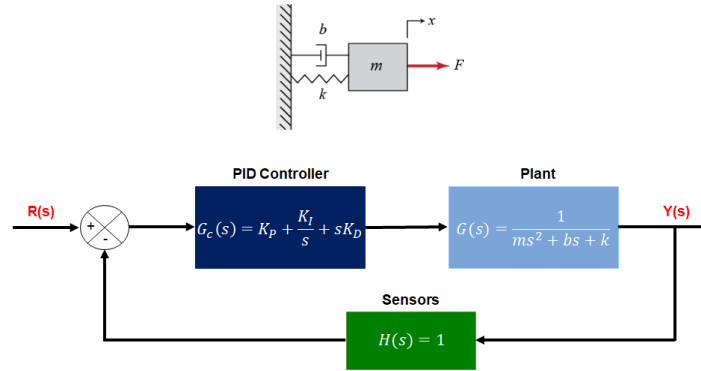
$$G(s) = \frac{s - 10}{s^2 + 2s + 1} \quad (1)$$

- (a) This is the first order transfer function
  - (b) This is the second order transfer function
  - (c) This is the third order transfer function
  - (d) This is the fifth order transfer function
  - (e) None of the above
2. What are the poles and zeros of the following transfer function?

$$G(s) = \frac{s^2 + 3s - 10}{s^2 - 2s - 12} \quad (2)$$

- (a) The poles are -3 and 4; the zeros are 2 and -5
  - (b) The poles are -4 and 3; the zeros are 5 and -2
  - (c) The poles are 2 and -5; the zeros are -3 and 4
  - (d) The poles are 5 and -2; the zeros are -4 and 3
  - (e) None of the above
3. What might be your action as a system control engineer if you need to increase the overshoot of a control loop system? (Select all that apply)
- (a) Increase  $K_I$
  - (b) Decrease  $K_I$
  - (c) Decrease  $K_P$
  - (d) Increase  $K_D$
  - (e) Increase  $K_P$
  - (f) Decrease  $K_D$
4. Consider the Mass-Spring-Damper System shown in the figure below.

As a system control engineer, you constructed the following closed loop transfer function to represent the Mass-Spring-Damper System. What is the correct transfer function for this closed loop?



(a) Transformation function 1

$$G(s) = \frac{K_D s^2 + sK_P + K_I}{K_P + \frac{K_I}{s} + K_D s} \quad (3)$$

(b) Transformation function 2

$$G(s) = \frac{K_P + \frac{K_I}{s} + K_D s}{K_D s^2 + sK_P + K_I} \quad (4)$$

(c) Transformation function 3

$$G(s) = \frac{ms^2 + bs + k + K_P \frac{K_I}{s} + K_D s}{K_P + \frac{K_I}{s} + K_D s} \quad (5)$$

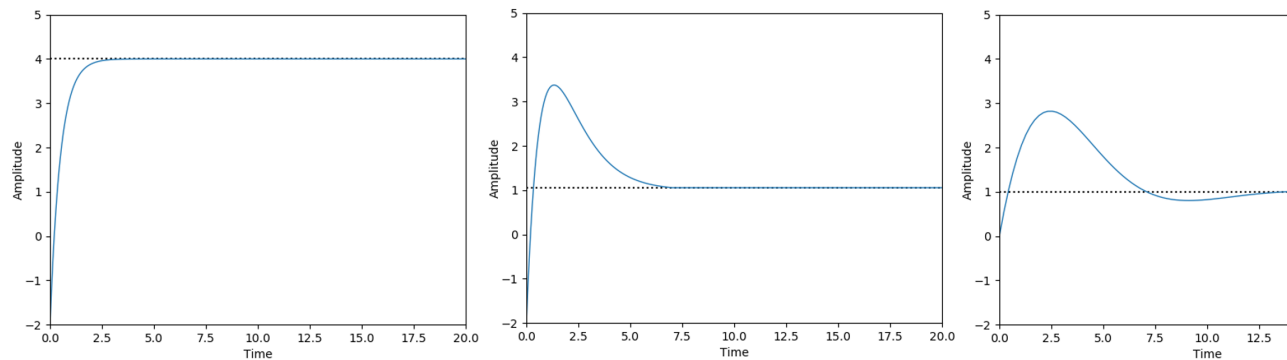
(d) Transformation function 4

$$G(s) = \frac{K_D s^2 + sK_P + K_I}{ms^3 + (b + K_D)s^2 + (k + K_P)s + K_I} \quad (6)$$

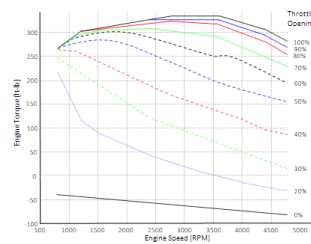
(e) None of the above

5. You are given the step response of a few different PID controllers using the same gains for the same first order transfer function. Determine a possible set of controllers that generated these step responses:

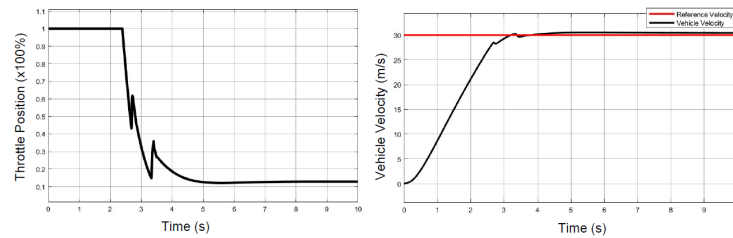
- (a) 1st response by PI; 2nd response by PD; 3rd response by PID
- (b) 1st response by PD; 2nd response by PI; 3rd response by PID
- (c) 1st response by PI; 2nd response by PID; 3rd response by PD
- (d) 1st response by PD; 2nd response by PID; 3rd response by PI
- (e) None of the above



6. What is the output of a typical output of a Longitudinal control module?  
 (Select all that apply)
- (a) Reference velocity
  - (b) Throttle angle
  - (c) Steering angle
  - (d) Brake position
7. Based on the engine map in the figure below, determine the throttle angle needed to produce 250 ft-lb of torque given that the current engine speed is 3500 RPM.



8. The results of a simulation of the control response to a step change in desired speed of a dynamic vehicle model with a PID controller are shown in the figures below. There are two spikes on these figures: one spike is between 2 and 3 seconds, another spike is between 3 and 4 seconds. What is the reason of these spikes?
- (a) Engine-transmission torque loss
  - (b) Tire slip
  - (c) Nonlinear engine map

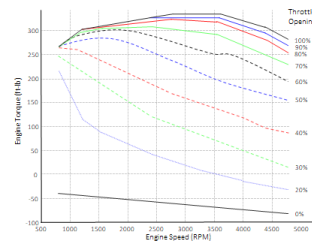


- (d) High level controller simplification: changing the integral to a summation over fixed length time steps in the Integral term
- (e) None of the above
9. What type of control system is shown in the figure below?



- (a) Feedback control
- (b) Feedforward control
- (c) Feedback-feedforward control
- (d) None of the above
10. What types of inaccuracies are corrected by a feedback controller?
- (a) Disturbances
- (b) Nonlinear engine map
- (c) Errors in the plant model
- (d) High level controller simplification: changing the integral to a summation over fixed length time steps in the Integral term
11. What assumptions are essential for creation of a longitudinal feedforward input? (Select all that apply)
- (a) The tire slip angle and ratio are negligible
- (b) The vehicle is at steady state
- (c) The plant system is linear
- (d) Torque from the engine passes directly to the transmission without loss
12. What are the sources of the load torque considered for a longitudinal feedforward look-up table computation? (Select all that apply)
- (a) Rolling resistance

- (b) Sliding resistance
  - (c) Gravitational resistance
  - (d) Cornering force
  - (e) Aerodynamic resistance
  - (f) Static friction
13. A vehicle is being operated on a highway with the reference velocity of  $126\text{ km/h}$  ( $35\text{ m/s}$ ) in gear 4 and it overcomes the total load torque of  $300\text{ ft-lb}$ . This vehicle specification includes effective wheel radius of  $0.35\text{ m}$  and 4th gear ratio of 2. What throttle angle is required for maintaining the the current speed of the vehicle? Use the below engine map for your computation.



## References

- [1] SAE *Taxonomy of Driving* [https://www.sae.org/standards/content/j3016\\_201806/?PC=DL2BUY](https://www.sae.org/standards/content/j3016_201806/?PC=DL2BUY)
- [2] SAE *SAE J3016 Taxonomy and Definitions Document* [https://drive.google.com/open?id=1xtOqFVJvOElXjXqf4RAwXZkI\\_EwbxFMg](https://drive.google.com/open?id=1xtOqFVJvOElXjXqf4RAwXZkI_EwbxFMg)
- [3] Åström K. J., Murray R. M. *Feedback Systems. An Introduction for Scientists and Engineers*
- [4] Philip , Florent Altche1, Brigitte dAndrea-Novet, and Arnaud de La Fortelle *The Kinematic Bicycle Model: a Consistent Model for Planning Feasible Trajectories for Autonomous Vehicles?* HAL Id: hal-01520869, <https://hal-polytechnique.archives-ouvertes.fr/hal-01520869>
- [5] Marcos R. O., A. Maximo *Model Predictive Controller for Trajectory Tracking by Differential Drive Robot with Actuation constraints*