A. Giavaras

Contents

1	Motion Planning	2
1.1	Introduction	2
1.2	Safe navigation	2
	1.2.1 Time critical planning	4
1.3	Motion planning	5
1.4	Definitions	6
1.5	Questions	7
1.6	Assignements	7

1 Motion Planning

Motion planning is the problem of finding a continuous collision free path from an initial configuration (or state) to a goal. On board an autonomous vehicle, the capability to prevent collisions also depends on the sensing and control. Critically, motion planning is a necessary component for the safe operation of an autonomous vehicles. Apart from an efficient algorithm for motion planning, one should also consider the problem of embedding the motion planner into a software system in which all tasks are required to satisfy hard deadlines.

We will discuss such a framework that can be used as a basis for incorporating approximately complete motion planning algorithms within a hard real-time system. This framework ensures that deadlines can be satisfied, with only mild constraints on other software. Two motion planning algorithms are presented as a verification of the framework, and are applied to solving dynamic motion planning problems related to the safe and efficient navigation of autonomous systems.

1.1 Introduction

A challenging problem in the development of unmanned and autonomous systems is to develop navigation strategies that are efficient, by minimising metrics such as transit time and power usage, while also minimising the risk of collisions. This problem is subject to uncertainty and partial information regarding the state of the vehicle, the obstacles, and the responses of the vehicle to inputs. Robust strategies for safe and efficient navigation require replanning to compensate for uncertainty and changes in the environment. The success of such strategies is dependent on the quality of sensing, planning and control, and on the temporal interactions between those tasks.

The consequences of failing to perform sensing, planning or control within a suitable dead- line can result in failure to observe obstacles, produce safe paths or accurately track a path. Consistent failure to meet deadlines can have serious effects including poor performance with respect to mission objectives or loss of vehicle, such as when a collision occurs.

1.2 Safe navigation

Safe navigation depends on being able to plan paths or trajectories that prevent collisions with obstacles. In the case of autonomous vehicles these obstacles can be either static, such as terrain or buildings, or dynamic, such as other moving vehicles.

In cases where an environment contains only static obstacles the task of finding safe paths can be addressed by solving a motion planning problem [2]. A plan

produced in this way is only safe if the environment is fully observable and does not change over time, a case which does not occur except in highly structured workspaces.

Remark 1.1. Fully Observable Environment

More realistic environments would include obstacles that move over time and obstacles that must be detected using sensors. This more difficult task can be addressed by replanning when the environment changes, a process known as **dynamic motion planning**.

Using an analogy from control theory, motion planning can be thought of as open-loop, while dynamic motion planning can be considered its closed-loop equivalent. This highlights that the replanning is used to minimise errors resulting from unforeseen environmental changes. Furthermore, it is also useful to consider the task of safe navigation as a cycle of sensing, planning and control or actuation as shown in Figure 1.

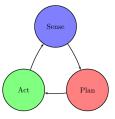


Fig. 1: Sensing, planning and control tasks.

The sensing task is responsible for mapping and localization. Mapping involves measuring, and in some cases predicting, locations of obstacles based on sensor observations. Localization is the task of finding the configuration (location and pose) of the vehicle. The quality of localization and mapping estimates is dependent on the types and properties of the sensors used. A significant external factor which influences localization and mapping relates to how quickly new observations are acquired, as compared to how quickly the vehicle moves.

The actuation task takes the sensed location of the vehicle and the path output of the mo- tion planner, and produces inputs to the actuators. These inputs are chosen so as to minimise path-tracking errors. The capability to track a path accurately depends on a number of factors including: the magnitude of environmental disturbances, sensors, actuators and the implementation of the controller, including the rate at which the controller is updated at.

The planning process uses a single mapping and localization estimate to produce a collision free path from the current configuration, to a goal configuration, determined based on the current mission objective. While planning is being conducted, no new information can be taken into account.

The capability to navigate safely depends on the quality of sensing, planning and control, and the interaction between those tasks. Interactions between tasks include direct coupling due to transfers of inputs and outputs, and indirect coupling that results from time taken for each task to execute. Excessive delays by any task could result in a collision.

1.2.1 Time critical planning

The combination of minimal computational resources, high cost of failure through collision and inter-coupling between the software tasks necessitate careful consideration of software design alternatives on-board autonomous vehicles.

The need to support long-term missions with minimal human interaction imposes constraints on the design of autonomous systems. In particular, vehicle designers must find an appropriate trade-off between [1]

- Payload
- Energy storage
- Endurance
- Sensing
- Actuation
- Computing capability

Constraints on computational resources tend to introduce trade-offs between performance and other factors that tend to be less critical in traditional software design. For example, an open issue in energy aware computing involves finding a suitable compromises between the power consumption and speed required to execute a piece of software [1]. Similarly, safety critical software systems are required to produce results within a time limit or risk catastrophic failure. With regard to planning for autonomous vehicles, failure to identify new plans within an acceptable time limit can potentially result in a collision. For this reason the hard real-time aspect of the computing constraints becomes crucial.

Remark 1.2. Temporal Inter-Coupling

The temporal inter-coupling which occurs between sensing, planning and actuation is a phenomenon that is frequently ignored in planning literature. The rare examples in which the problem is considered [BV02, HKLR02], make the assumptions that minor collisions are acceptable. In this work, the cost of a collision of an autonomous system makes such an assumption unacceptable.

Remark 1.3. Anytime Algorithms

Perhaps the best known results for planning under time constraints are those based on any- time algorithms [BD89]. These algorithms progressively refine an initial solution, improving quality as time permits. Such an approach is less applicable in cases like motion planning subject to kinematic and dynamic constraints, where finding an initial solution is time consuming.

Work on real-world autonomous systems is targeted towards deployment in complex, unstructured, time-variant and partially observable environments. The need to achieve safe navigation in these types of environments necessitates the use of dynamic motion planning algorithms. Safe operation of an autonomous system requires that critical tasks (sensing, planning and control), execute in a timely manner. Failure to do this can lead to errors in localization (vehicle state), mapping (obstacle state and geometries), path tracking, and most importantly for this work, path generation. Sufficiently large errors in any of these areas can result in degradation in mission performance, or in the worst case, failure due to collisions [1].

1.3 Motion planning

Safe and efficient navigation is a task of significant interest in robotics, and particularly mobile robotics. It involves finding a continuous path that can be followed from an initial configuration (or state) to a goal configuration. A safe path is one that prevents collisions with obstacles, and an efficient path is one which minimises cost. In real-world environments, safe navigation depends on sensing, motion planning and control.

Safe and efficient navigation is a task of significant interest in robotics, and particularly mobile robotics. It involves finding a continuous path that can be followed from an initial configuration (or state) to a goal configuration. A safe path is one that prevents collisions with obstacles, and an efficient path is one which minimises cost. In real-world environments, safe navigation depends on sensing, motion planning and control. One of the challenges of safe navigation relates to the quantity and reliability of information available about the environment. Put simply, if there are inaccuracies in the estimated location of the vehicle or obstacles, then there is risk that a collision will occur. To ensure that an accurate model of the environment is available, vehicles are equipped with sensors capable of measuring the workspace around the vehicle. Sensor observations are used to identify the current state of the vehicle, localisation, and to identify the location of portions of the workspace which contain obstacles, mapping. The combined tasks of localisation and mapping are typically described as Simultaneous Localisation and Mapping (SLAM) [LDW91], and

are a major topic in robotics research today.

At a given time, given the current best estimate of the location of the vehicle and obstacles, it is possible to consider the task of finding an open-loop collision-free path from the current vehicle state to a goal state. Any errors in localisation or mapping could result in paths being planned through obstacles. Furthermore, old plans can become invalidated if new obstacles are observed, or if the vehicle cannot accurately track a path.

Vehicle control involves attempting to accurately follow a planned path or trajectory. To this end, the outputs to the actuators are determined so as to minimise the deviation of the state of the vehicle from the specified path. There are several well known approaches for solving this problem, including modern and classical control techniques [Oga01]. In the field of control, other excellent resources are available that consider the issues related to the control for flight [Bla91, SL03], and underwater [Fos94] vehicles. In the context of planning, safe navigation involves an incremental process of sensing, planning and control. Failure of any of those subsystems to provide accurate or timely results can result in a collision.

1.4 Definitions

The geometry of a motion planning problem is described, at least initially, in terms of a workspace. The workspace, W, can be thought of as a mathematical representation of the physical space, in which the boundaries of both the vehicle and the known obstacles are encoded. The workspace is normally represented as a three dimensional Euclidean space \mathbb{R}^3 .

The geometry of vehicles and obstacles within the workspace can be represented in a va- riety of ways. Typically these methods include either polygonal models such as triangular meshes, or semi-algebraic models.

Within the workspace, the position of the vehicle can be encoded as a configuration, \mathbf{q} or a state. A vehicles configuration can be described by an n-dimensional vector where the vehicle has n degrees of freedom. For example, a rigid body moving in the plane has a configuration vector with three elements $\mathbf{q} = (x, y, \theta)^T$; a two dimensional position (x, y) and a heading θ . A rigid body in three dimensions can be represented as a configuration vector with six elements $(x, y, z, \phi, \theta, \psi)^T$, a three dimensional position, and an orientation specified in terms of Euler angles (yaw, pitch and roll).

For a given vehicle configuration, the vehicle occupies a certain portion of the workspace, $A(q) \subset W$. The portion of the workspace occupied by a set of m stationary obstacles can be described as:

$$B_i \subset W, i \in [1, 2, ..., m]$$
 (1)

The total affect of all of the obstacles in the workspace can be expressed as

$$B = \bigcup_{i \in [1, m]} B_i. \tag{2}$$

This leads to the definition that a collision occurs if the area occupied by the vehicle would intersect with that of any of the obstacles, that is if

$$A(q) \cup B \neq \emptyset \tag{3}$$

The breakthrough work in path planning was the paper by Lozano-Perez [LP83], who showed that path planning problems can be formulated in terms of a configuration space, C, which allows the geometric and topological complexities of all planning problems to be modelled using a consistent set of mathematical tools. The configuration space consists of all of the possible valid configurations, but it can be further refined into two subsets, the set of configurations that the vehicle can safely occupy, which is the free space \mathcal{F} , and the set of configurations which, when occupied, would result in collision, C_{obs} .

By transforming the problem from one of planning in the workspace to a configuration space, the task of motion planning becomes one of finding a continuous path. A path can be expressed as a parameterised continuous map, $\tau: s \to q$, where the initial configuration is q_i at $\tau(0)$ and the final configuration is q_f at $\tau(1)$.

In order for a path to be collision free, all configuration $\tau(s), \forall s \in [0,1]$, must be in \mathcal{F} . In cases where the configuration space changes over time, it is customary to refer to a path parameterised by time as a trajectory. If a system to be modelled is subject to kinematic or dynamic effects, then it is necessary to consider the derivatives of configuration during planning. For example, a model that includes kinematics and dynamics will result in a state space X, where each state, $x \in X$ encodes a configuration, q, velocity, \dot{q} , and acceleration, \ddot{q} such that $x \in (q, \dot{q}, \ddot{q})$.

1.5 Questions

1.6 Assignements

References

[1] Walker A. B., Hard Real-Time Motion Planning for Autonomous Vehicles, PhD Thesis, Swinburne University, 2011.

 $[2]\,$ LaValle S. M., Planning Algorithms, Cambridge, 2006.