

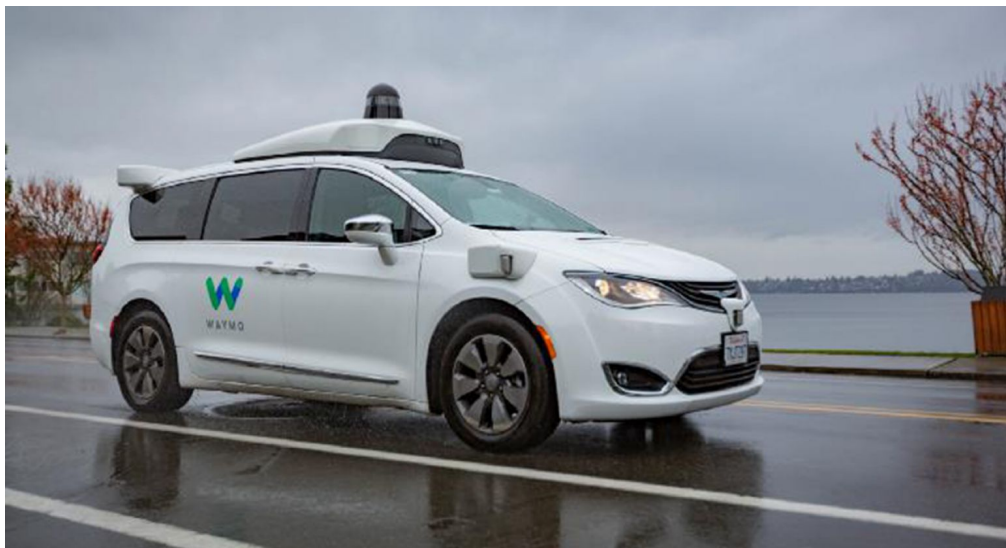
# Safe Reinforcement Learning

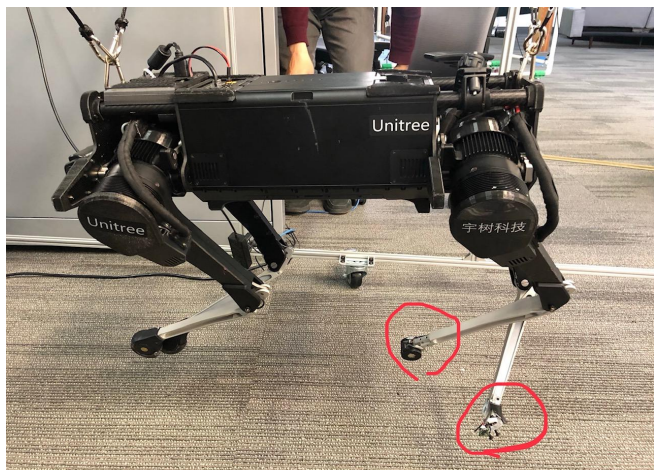
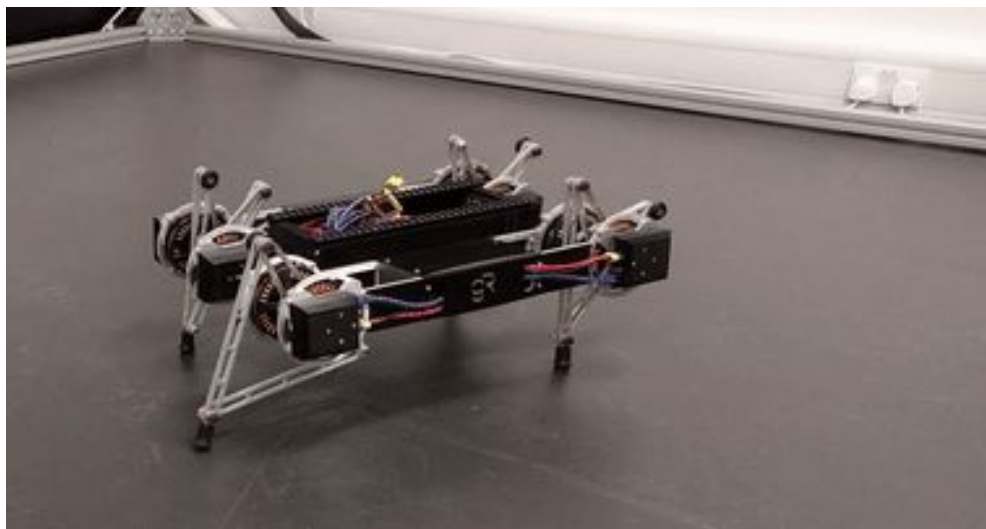
Jie Tan

CS 8803 Deep Reinforcement Learning for Intelligent Control

04/06/2022

# Why Safety





# Goals

- Definition of safety
- Two ways to improve safety during learning
  - Constrained Markov Decision Process
  - Safe learning via shielding

# Brainstorming: What are Unsafe Behaviors?

- Autonomous cars: collision
- Legged robots: falling
- Robot manipulators: destroying the object in manipulation
- Investing: losing  $x\%$  of values in the portfolio
- Data center cooling: overheating the servers
- Power grid: power supply shortage
- ...

# Safety as Constraints

- Autonomous cars: collision  $d < 0$
- Legged robots: falling  $h < 0.5m$
- Robot manipulators: destroying the object in manipulation  $f_{\text{contact}} > 7N$
- Investing: losing x% of values in the portfolio  $\$ < 1M$
- Data center cooling: overheating the servers  $t > 104^{\circ}F$
- Power grid: power supply shortage  $E_{\text{generator}} - E_{\text{consumer}} < 0$
- ...

# Three Levels of Constraints

**Soft Constraints**

Safety Level I

**Probabilistic Constraints**

Safety Level II

**Hard Constraints**

Safety Level III

# Three Levels of Constraints

## Soft Constraints

Safety Level I



## Probabilistic Constraints

Safety Level II

## Hard Constraints

Safety Level III

$$\mathbb{E} \left[ \sum_{t=0}^T f_s(s_t, a_t) \right] \geq 0$$



# Three Levels of Constraints

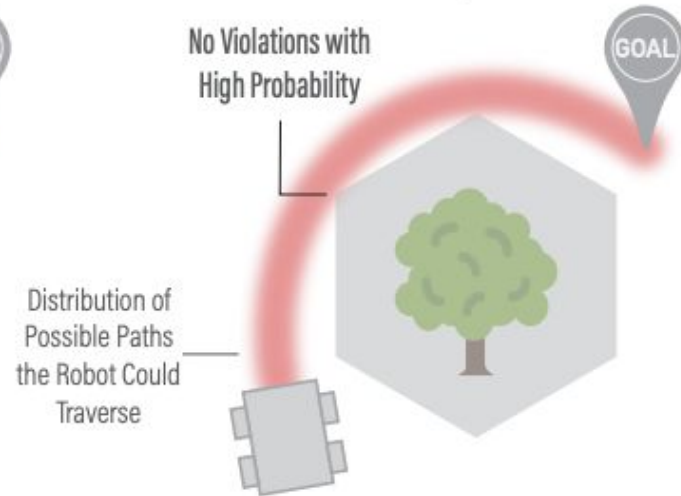
## Soft Constraints

Safety Level I



## Probabilistic Constraints

Safety Level II



## Hard Constraints

Safety Level III

$$\mathbb{E} \left[ \sum_{t=0}^T f_s(s_t, a_t) \right] \geq 0$$

$$Pr(f_s(s_t, a_t) \geq 0) > 1 - \epsilon$$

# Three Levels of Constraints

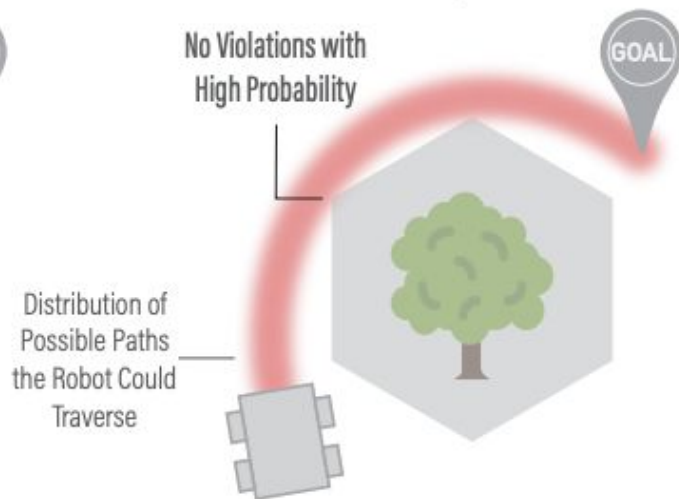
## Soft Constraints

Safety Level I



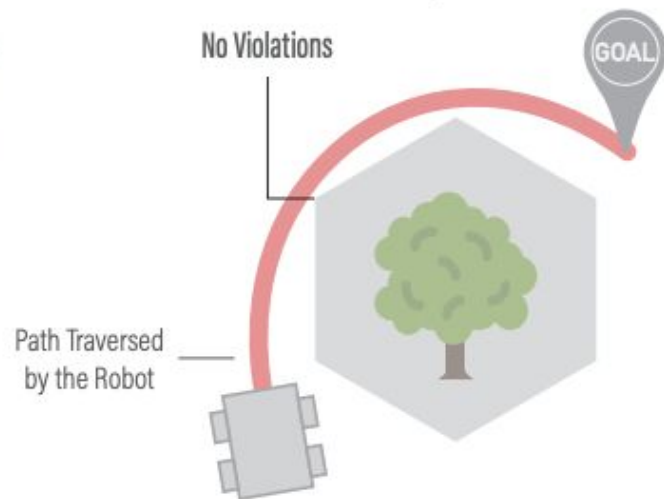
## Probabilistic Constraints

Safety Level II



## Hard Constraints

Safety Level III

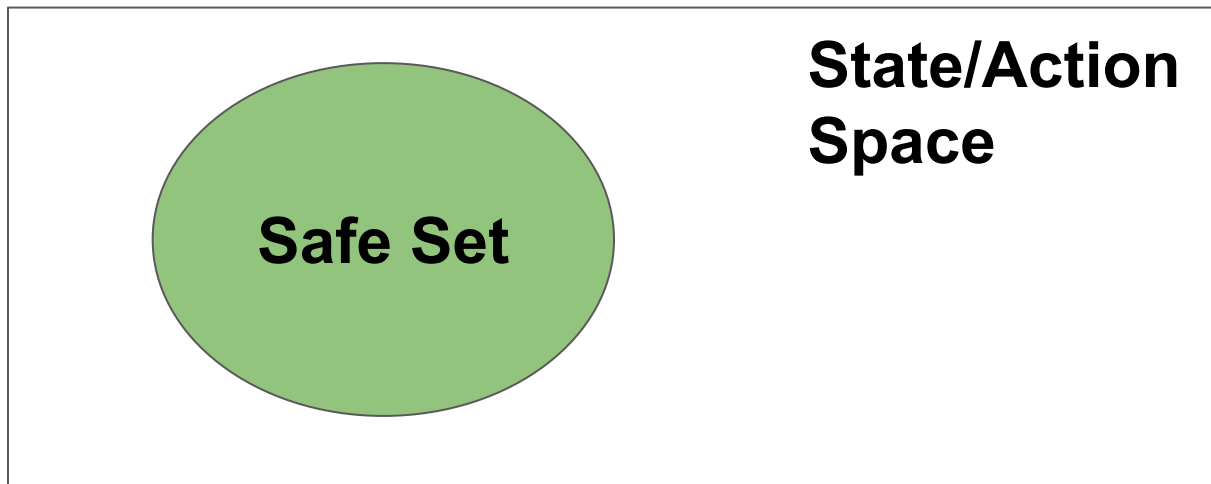


$$\mathbb{E} \left[ \sum_{t=0}^T f_s(s_t, a_t) \right] \geq 0$$

$$Pr(f_s(s_t, a_t) \geq 0) > 1 - \epsilon$$

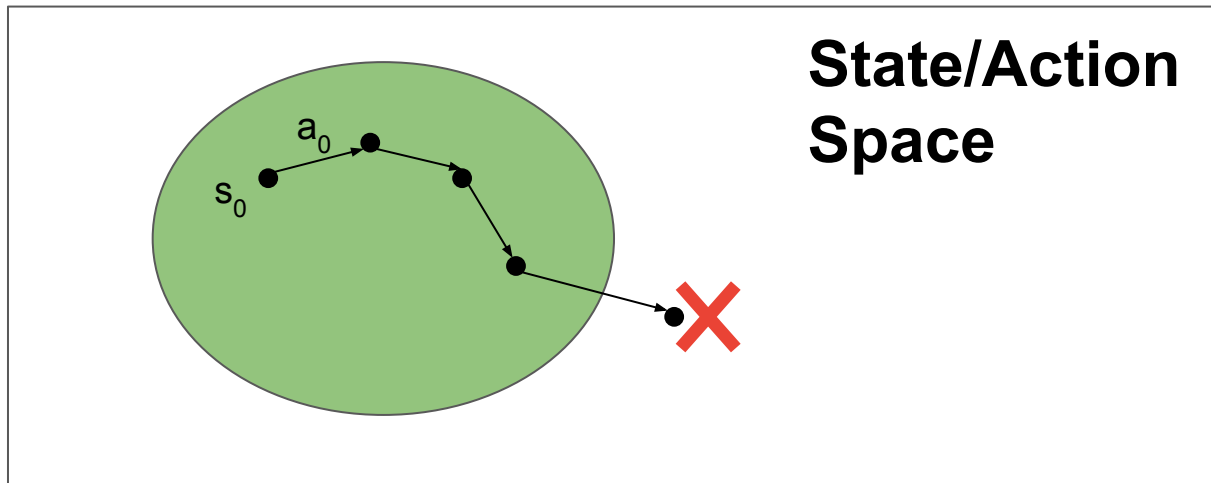
$$f_s(\mathbf{s}_t, \mathbf{a}_t) \geq 0$$

# Constrained Markov Decision Process (CMDP)



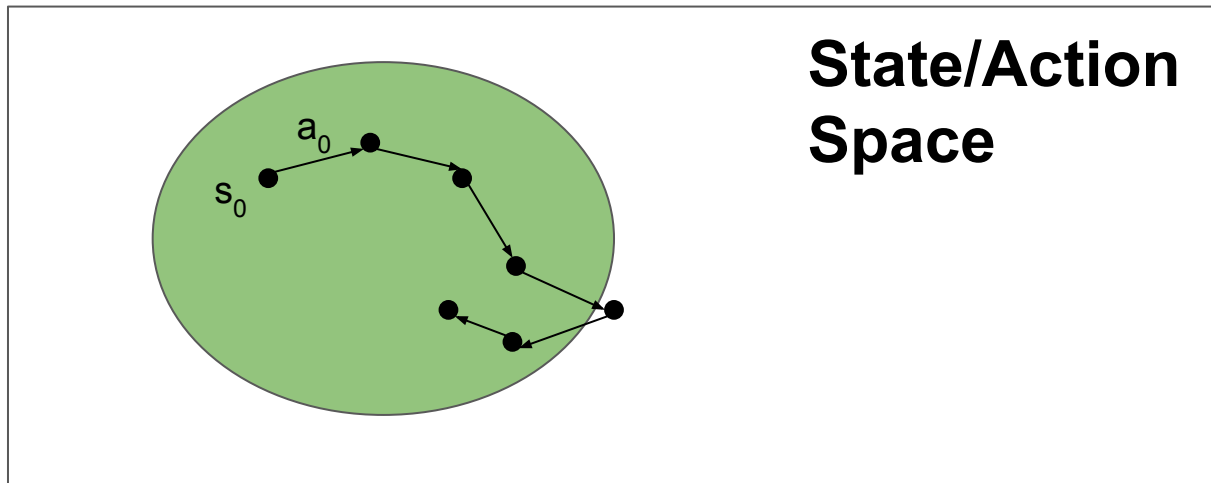
$$f_s(\mathbf{s}_t, \mathbf{a}_t) \geq 0$$

# CMDP Problem Definition



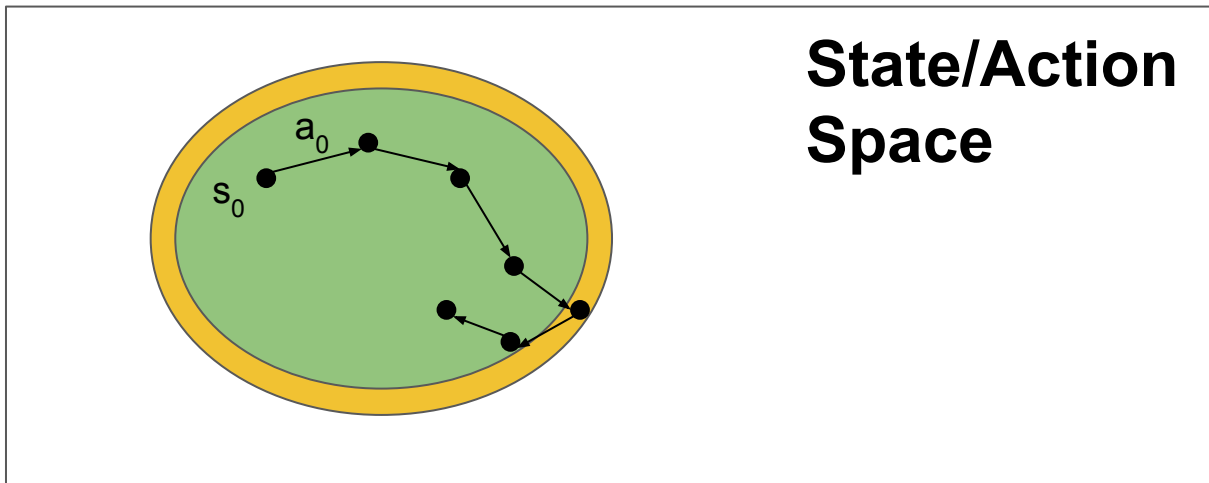
$$\max_{\pi \in \Pi} \mathbb{E}_{\tau \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(\mathbf{s}_t, \mathbf{a}_t) \right]$$

# CMDP Problem Definition



$$\begin{aligned} \max_{\pi \in \Pi} \mathbb{E}_{\tau \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(\mathbf{s}_t, \mathbf{a}_t) \right] \\ \text{s.t. } \mathbb{E}_{(\mathbf{s}_t, \mathbf{a}_t) \sim \rho_{\pi}} \left[ \sum f_s(\mathbf{s}_t, \mathbf{a}_t) \right] \geq 0 \end{aligned}$$

# CMDP Problem Definition



$$\begin{aligned} \max_{\pi \in \Pi} \mathbb{E}_{\tau \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(\mathbf{s}_t, \mathbf{a}_t) \right] \\ \text{s.t. } \mathbb{E}_{(\mathbf{s}_t, \mathbf{a}_t) \sim \rho_{\pi}} \left[ \sum f_s(\mathbf{s}_t, \mathbf{a}_t) \right] \geq 0 \end{aligned}$$

# Solving CMDP: Lagrangian Method

$$\begin{aligned}
 & \max_{\pi \in \Pi} \mathbb{E}_{\tau \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(s_t, \mathbf{a}_t) \right] \\
 & \text{s.t. } \mathbb{E}_{(s_t, \mathbf{a}_t) \sim \rho_{\pi}} \left[ \sum f_s(s_t, \mathbf{a}_t) \right] \geq 0
 \end{aligned}
 =
 \max_{\pi} \min_{\lambda \geq 0} \mathbb{E}_{\pi \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(s_t, a_t) + \lambda f_s(s_t, a_t) \right]$$

Lagrangian

$$\mathcal{L}(\pi, \lambda) = \mathbb{E}_{\tau \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(s_t, \mathbf{a}_t) + \lambda f_s(s_t, \mathbf{a}_t) \right]$$

$$\max_{\pi} \min_{\lambda \geq 0} \mathcal{L}(\pi, \lambda)$$

$$\max_{\pi} \min_{\lambda \geq 0} \mathbb{E}_{\pi \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(s_t, a_t) + \lambda f_s(s_t, a_t) \right]$$

= 0    ≥ 0

$$\max_{\pi} \min_{\lambda \geq 0} \mathbb{E}_{\pi \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(s_t, a_t) + \lambda f_s(s_t, a_t) \right]$$

→ ∞    ≤ 0

$$\max_{\pi} \min_{\lambda \geq 0} \mathbb{E}_{\pi \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(s_t, a_t) + \lambda f_s(s_t, a_t) \right]$$

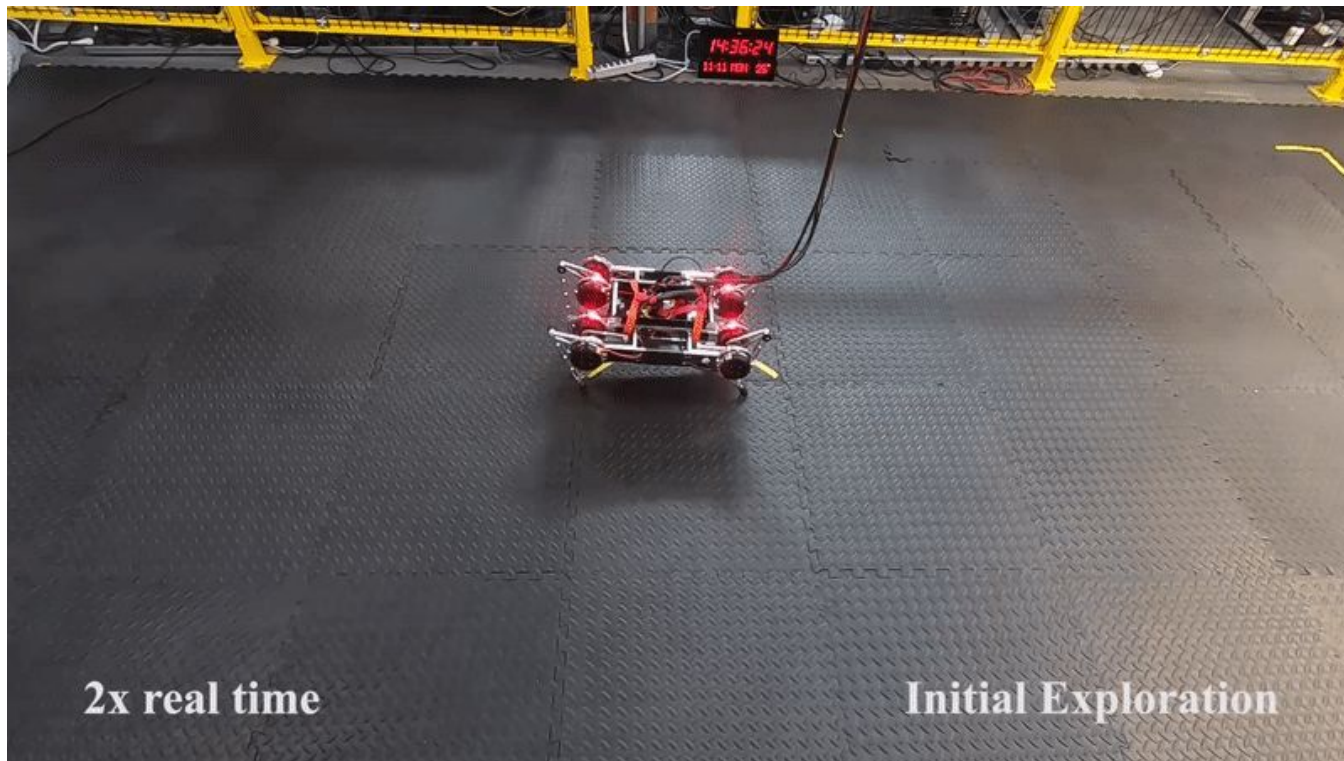


$$\max_{\pi} \min_{\lambda \geq 0} \mathbb{E}_{\pi \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(s_t, a_t) + \lambda f_s(s_t, a_t) \right]$$

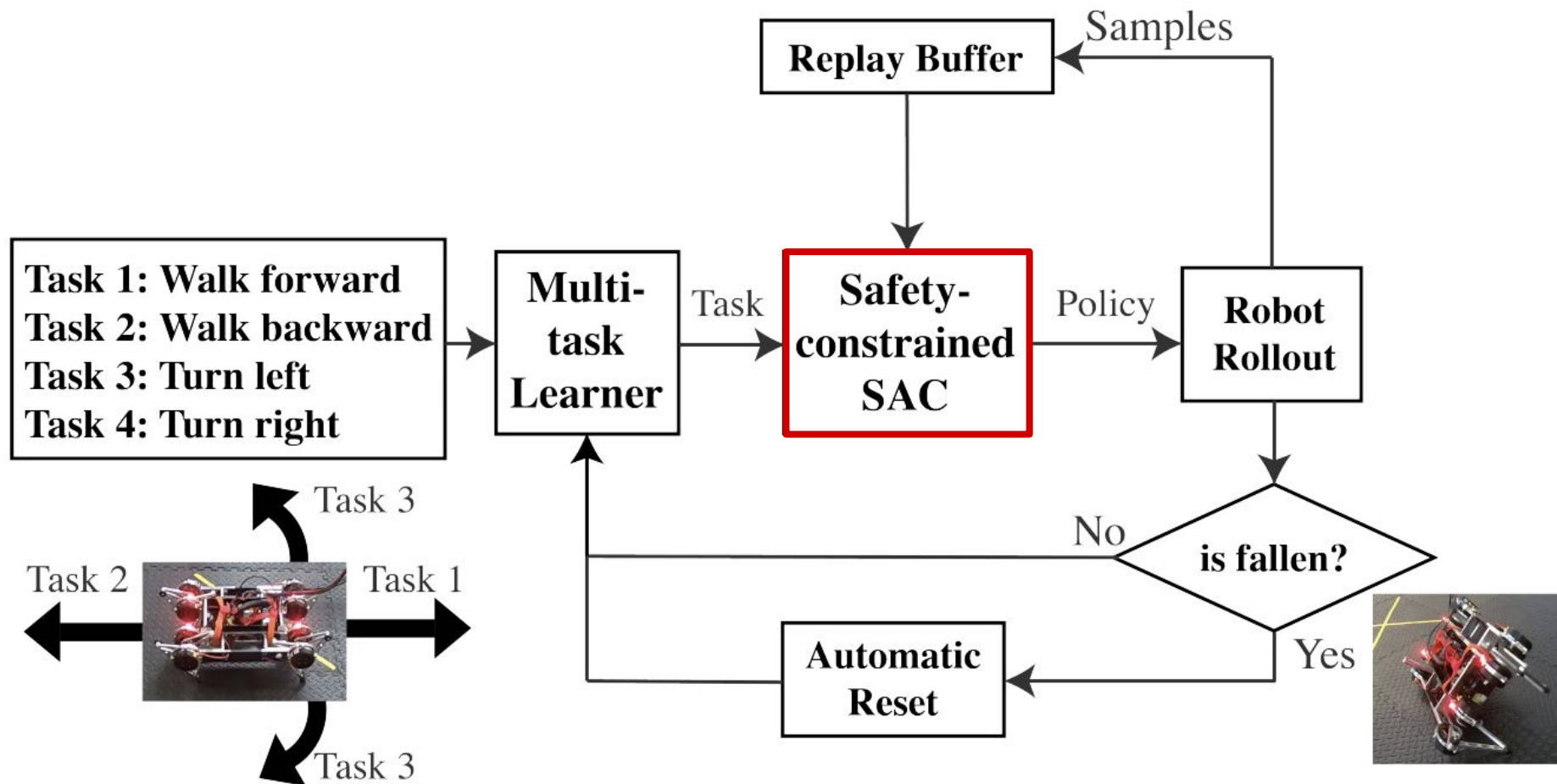
## Pseudocode

1. Randomly initialize  $\pi$ , set  $\lambda = 0$
2. Roll out policy  $\pi$
3. Calculate policy gradient  $\frac{\partial \mathcal{L}}{\partial \pi}$
4.  $\pi = \pi + \alpha \frac{\partial \mathcal{L}}{\partial \pi}$
5. Calculate gradient  $\frac{\partial \mathcal{L}}{\partial \lambda}$
6.  $\lambda = \max(0, \lambda - \beta \frac{\partial \mathcal{L}}{\partial \lambda})$
7. Go to 2

# Case Study: Learning Locomotion in Real World



[\[Learning to Walk in the Real World with Minimal Human Effort, Ha et al. CoRL 2020\]](#)



# Safety-Constrained SAC: Formulation

$$\begin{aligned} \max_{\pi \in \Pi} \mathbb{E}_{\tau \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(\mathbf{s}_t, \mathbf{a}_t) \right] \\ \text{s.t. } \mathbb{E}_{(\mathbf{s}_t, \mathbf{a}_t) \sim \rho_{\pi}} [f_s(\mathbf{s}_t, \mathbf{a}_t)] \geq 0, \quad \forall t. \\ \boxed{\mathbb{E}_{\rho_{\pi}} [-\log(\pi_t(\cdot | \mathbf{s}_t))] \geq \mathcal{H}} \end{aligned}$$

Entropy  
Constraints

# Safety-Constrained SAC: Formulation

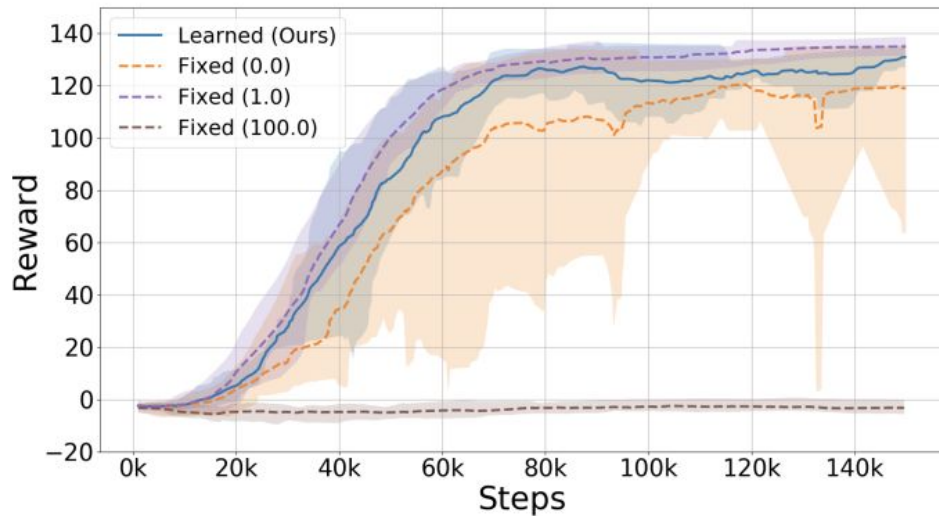
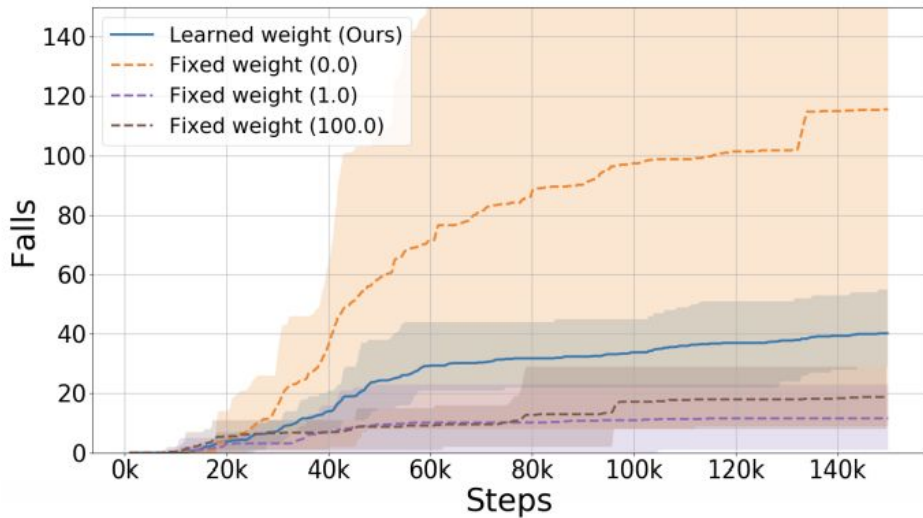
$$\begin{aligned} \max_{\pi \in \Pi} \mathbb{E}_{\tau \sim \rho_{\pi}} \left[ \sum_{t=0}^T r(\mathbf{s}_t, \mathbf{a}_t) \right] \\ \text{s.t. } \mathbb{E}_{(\mathbf{s}_t, \mathbf{a}_t) \sim \rho_{\pi}} [f_s(\mathbf{s}_t, \mathbf{a}_t)] \geq 0, \quad \forall t \\ \mathbb{E}_{\rho_{\pi}} [-\log(\pi_t(\cdot | \mathbf{s}_t))] \geq \mathcal{H} \end{aligned}$$

Safety Constraints

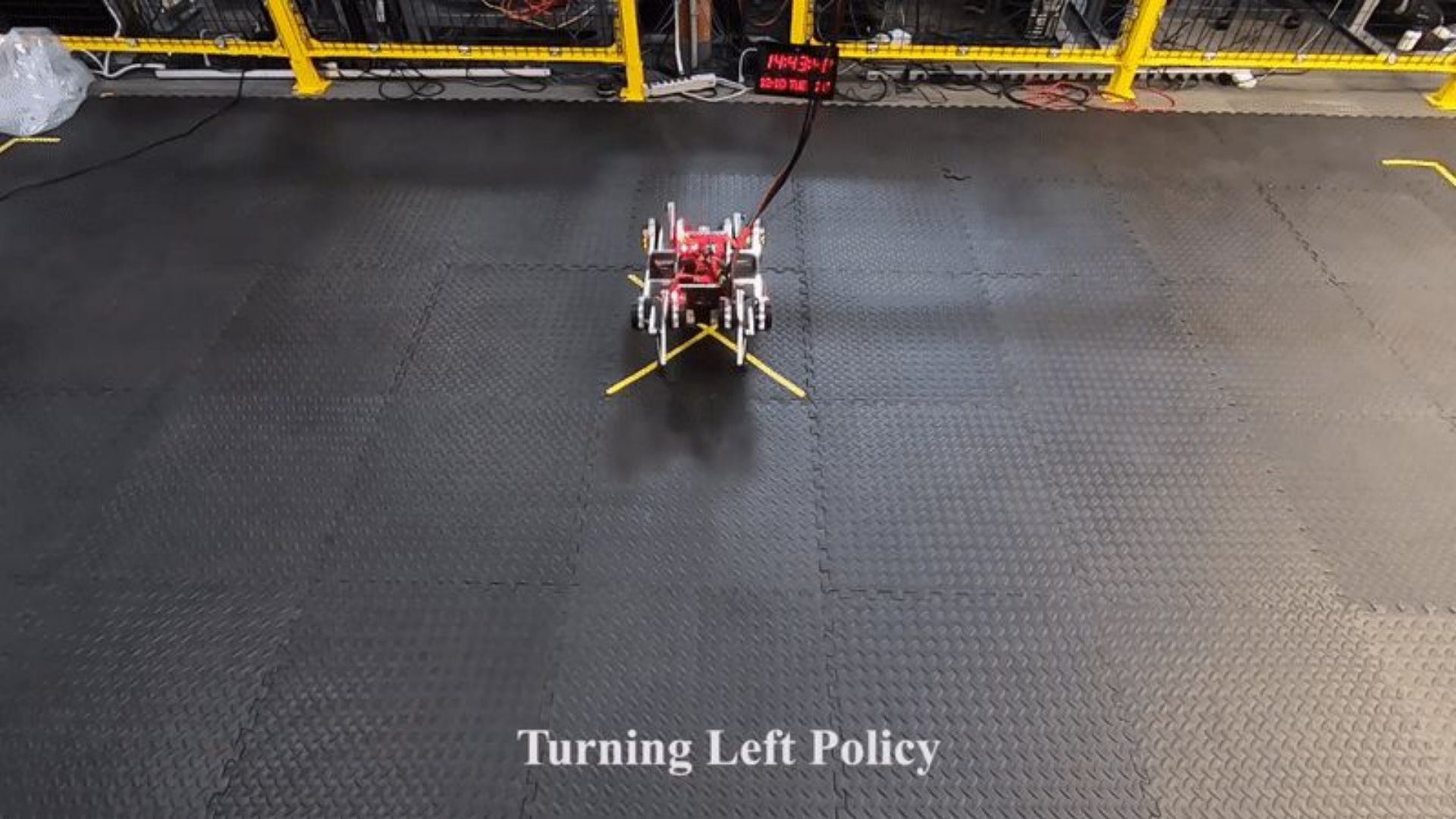
where

$$f_s(\mathbf{s}_t, \mathbf{a}_t) = \min(\hat{p} - |p_t|, \hat{r} - |r_t|)$$

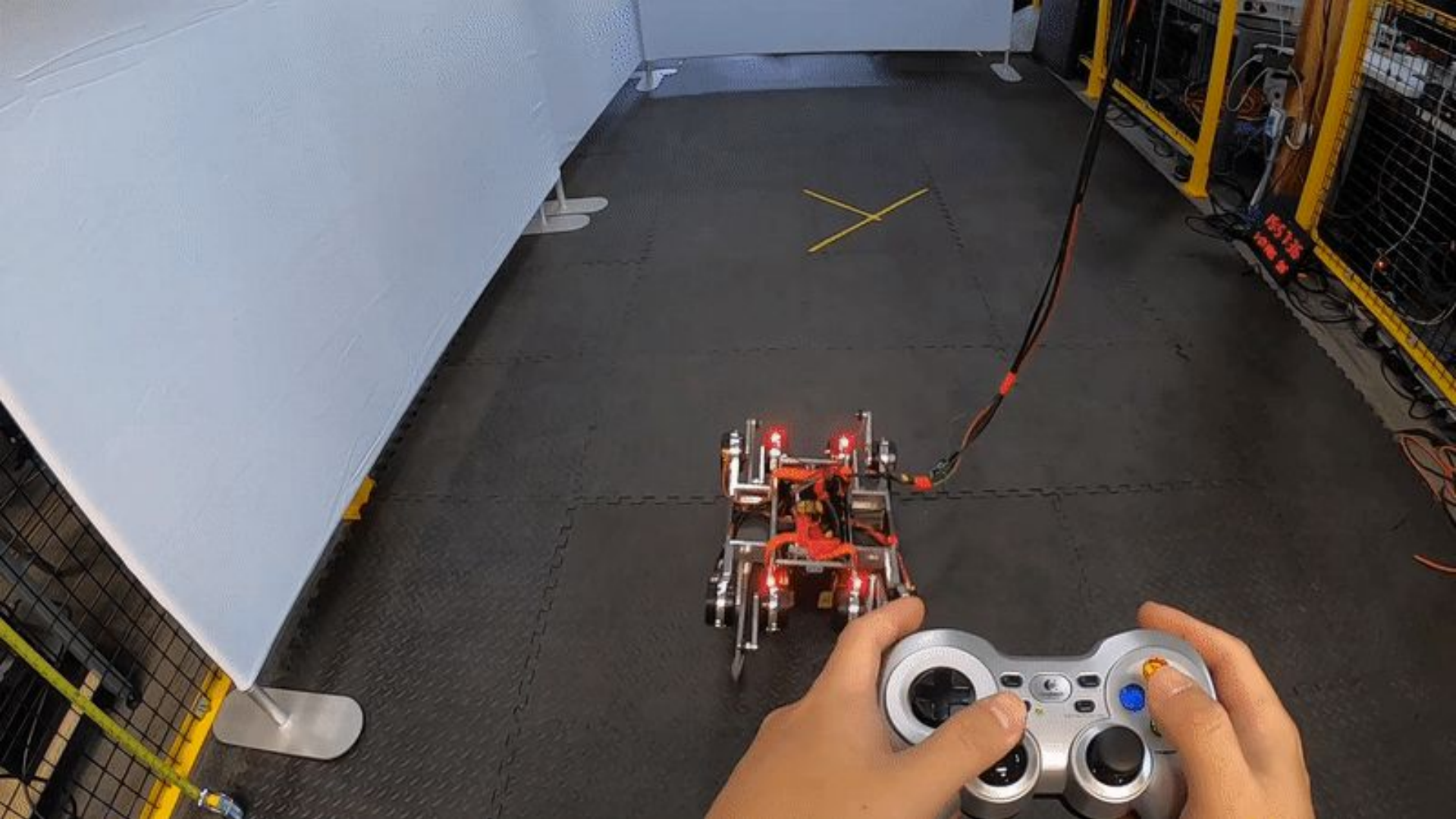
# Safety-Constrained SAC: Evaluation





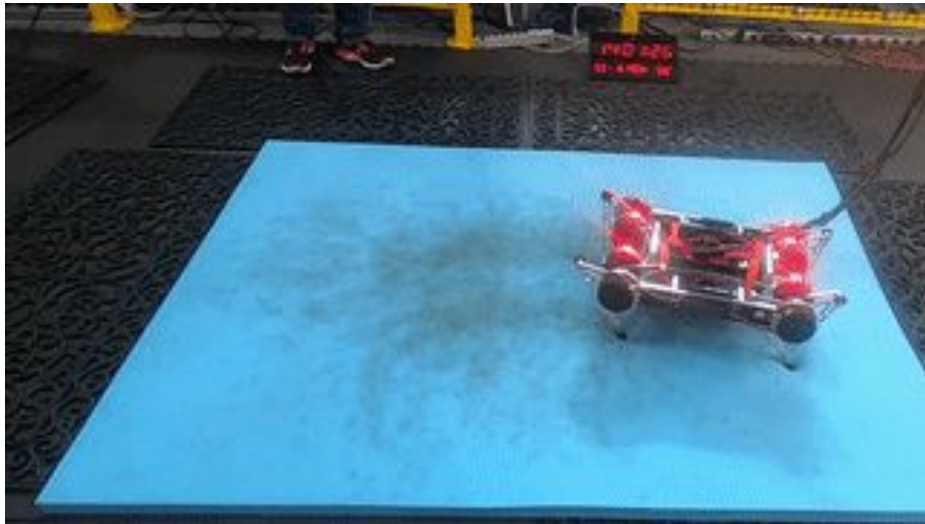


Turning Left Policy

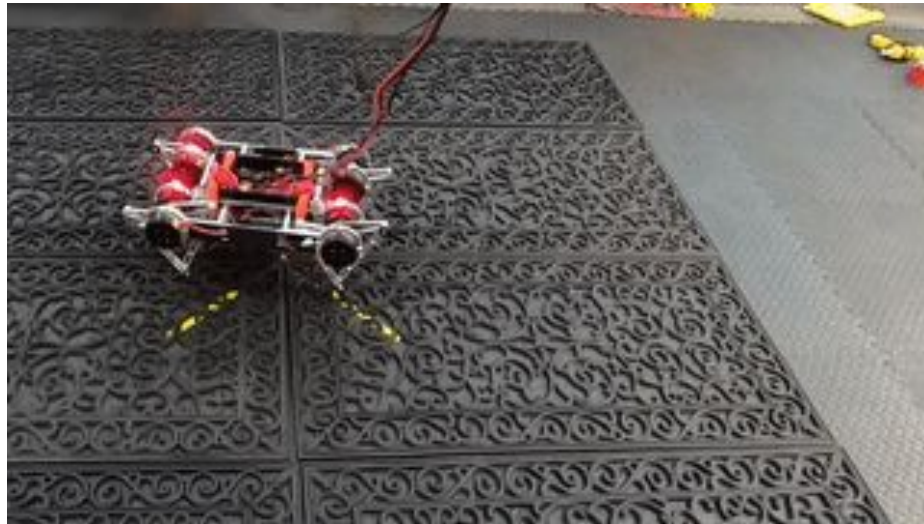




# Learning on challenging terrains



Memory foam

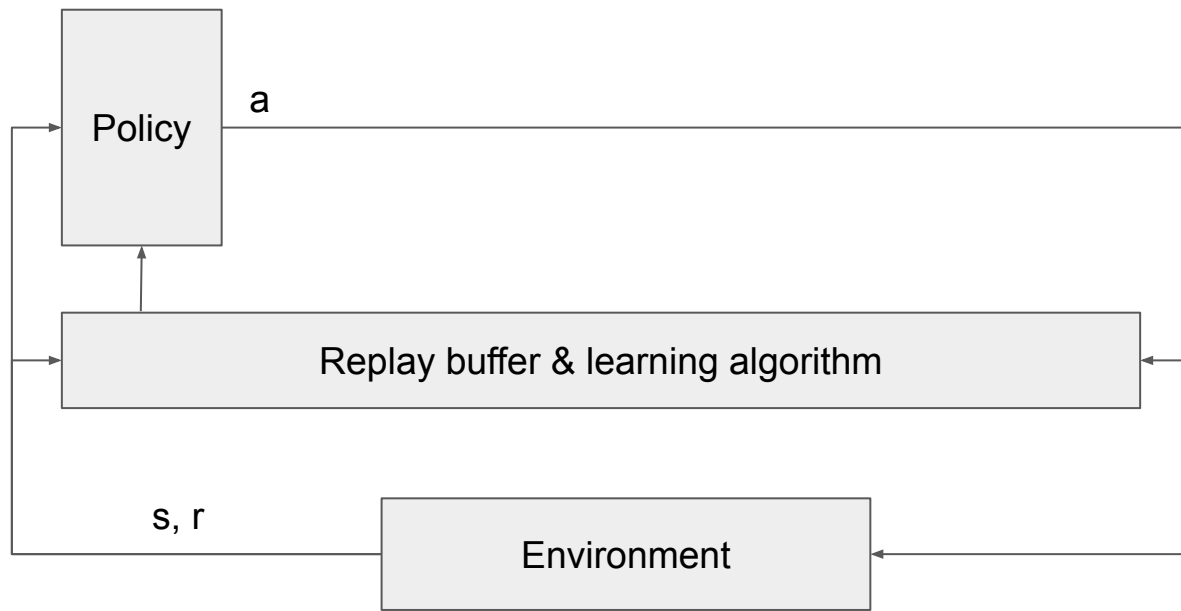


Rubber mat with crevices

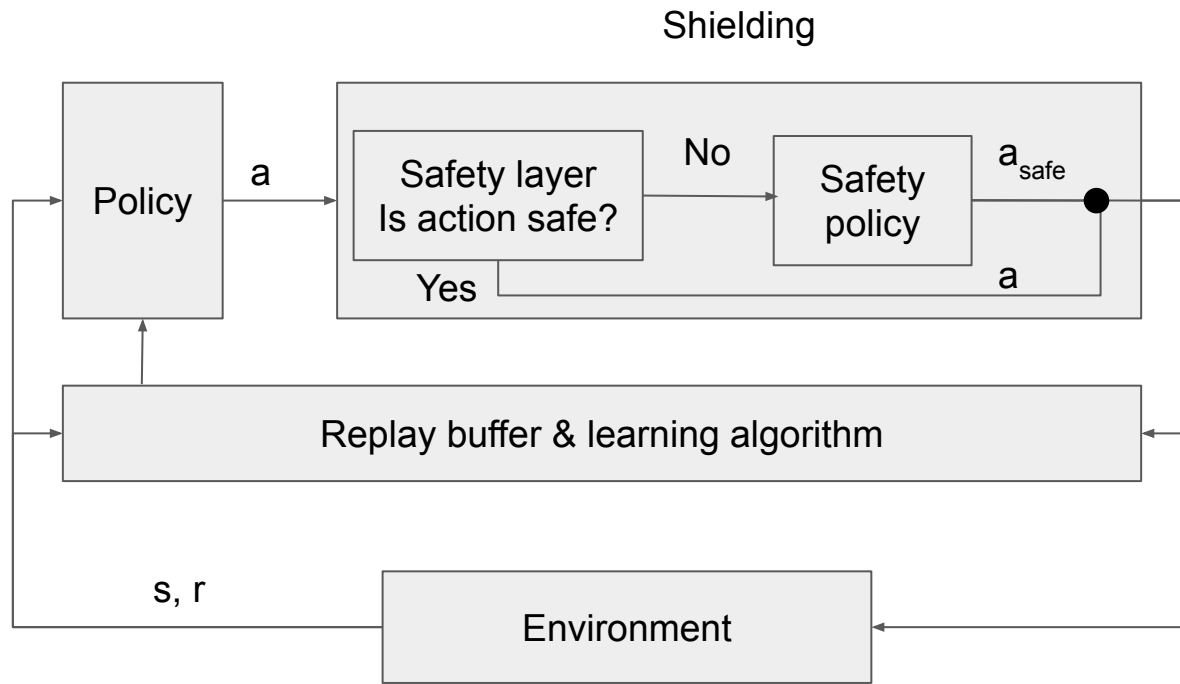
# Limitations

- Unsafe events can still happen, though less frequently
- Hard to specify safety constraints in many applications
  - Can we learn safety constraints? [\[Recovery RL: Safe Reinforcement Learning with Learned Recovery Zones, Thananjeyan et al. RA-L, 2021\]](#)

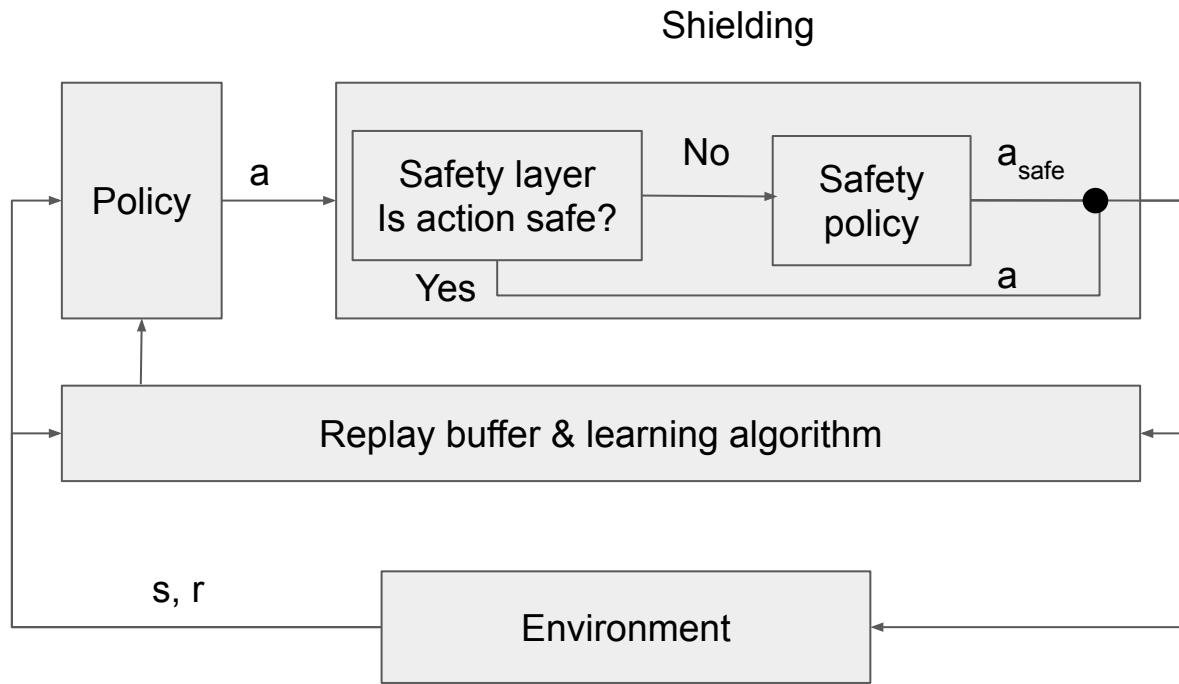
# Safe Learning via Shielding



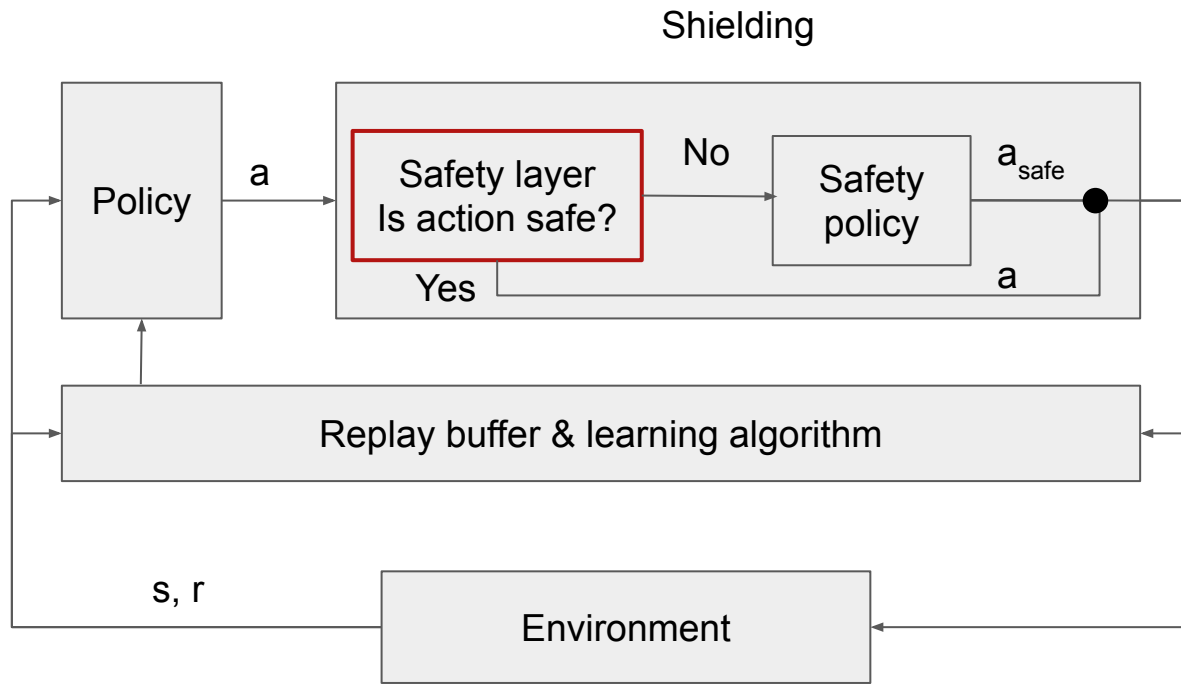
# Safe Learning via Shielding



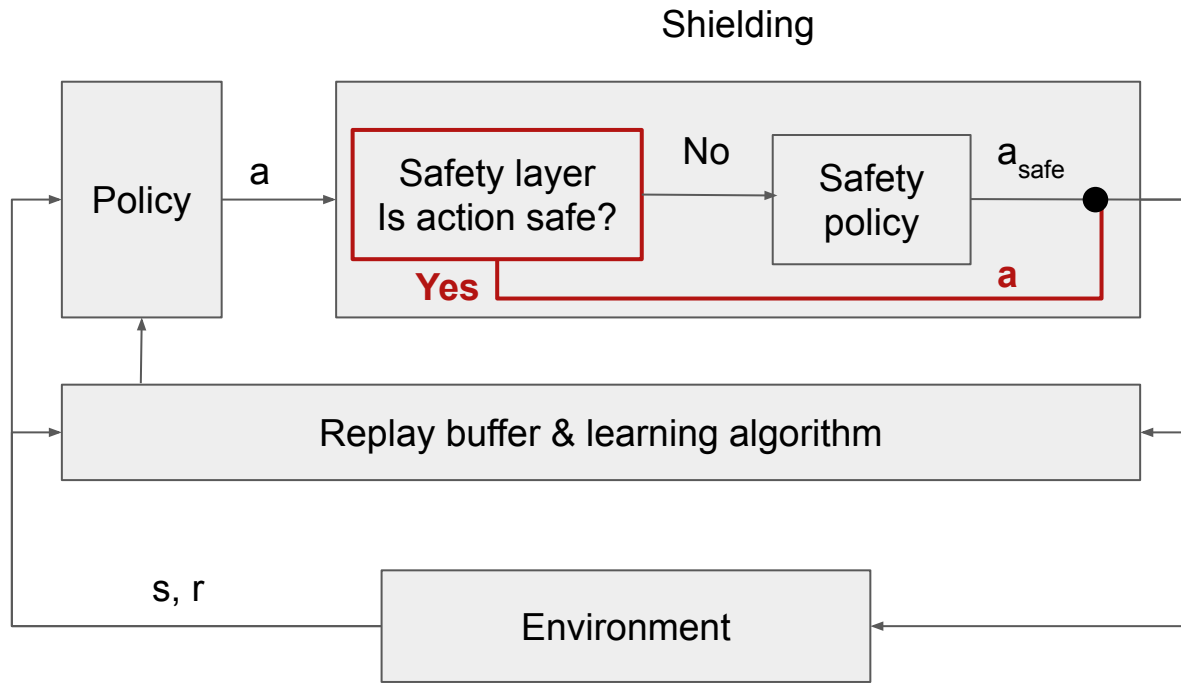
# Safe Learning via Shielding



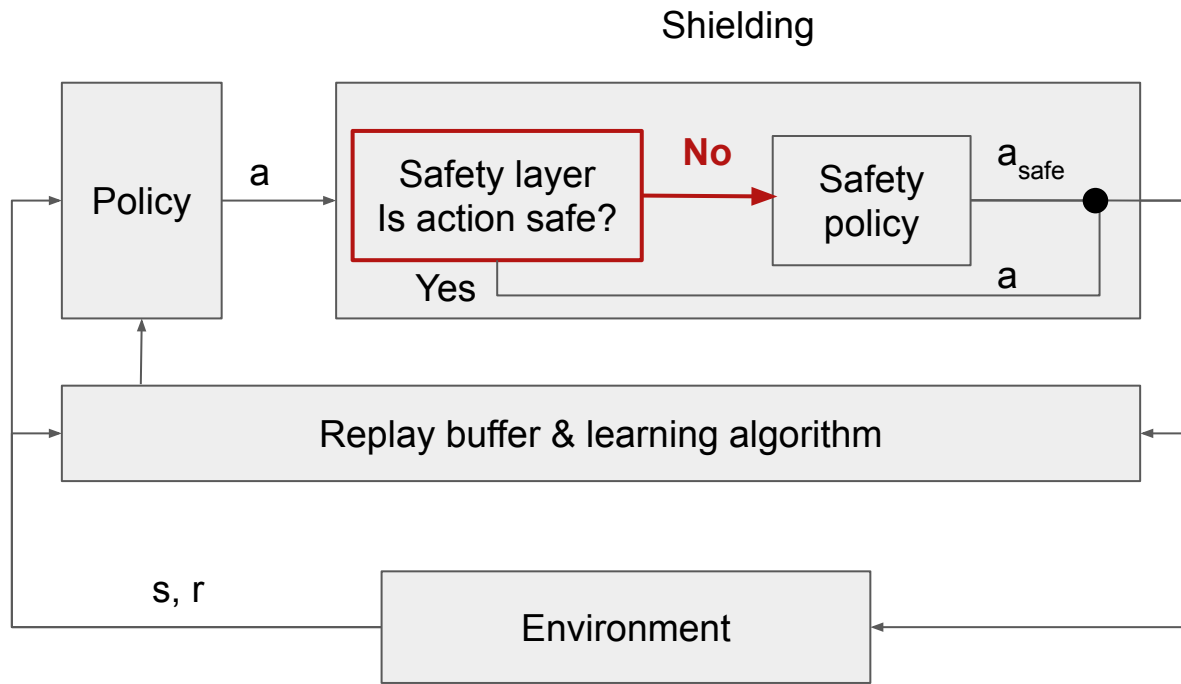
# Safe Learning via Shielding



# Safe Learning via Shielding

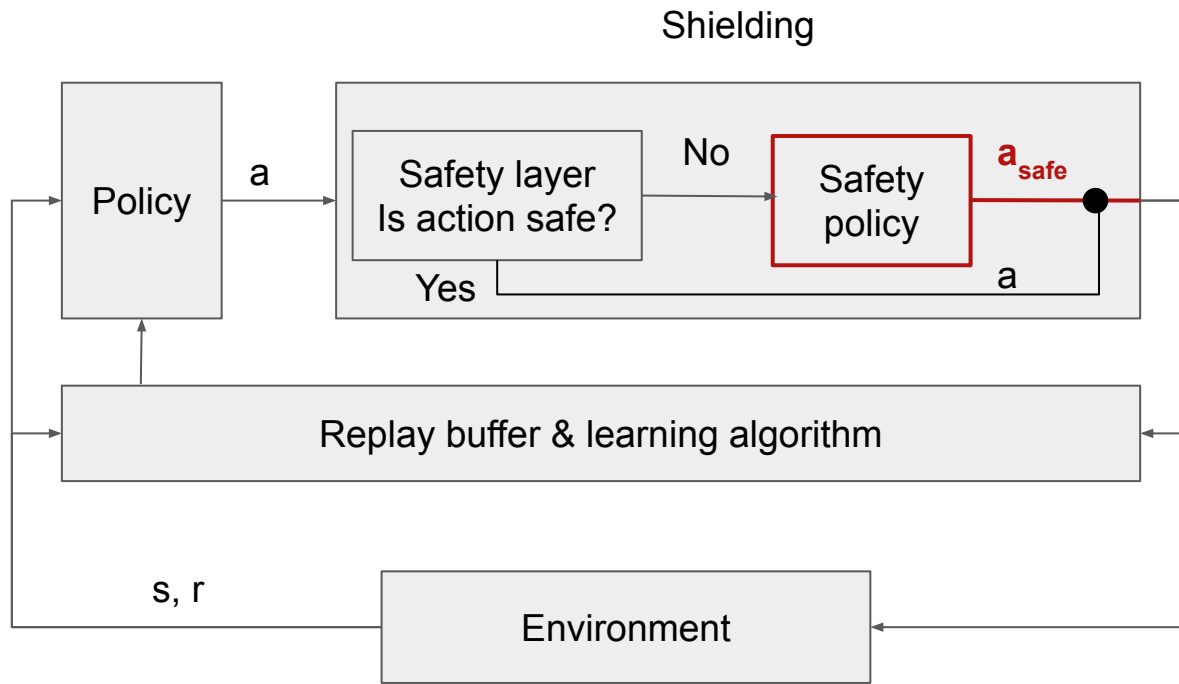


# Safe Learning via Shielding



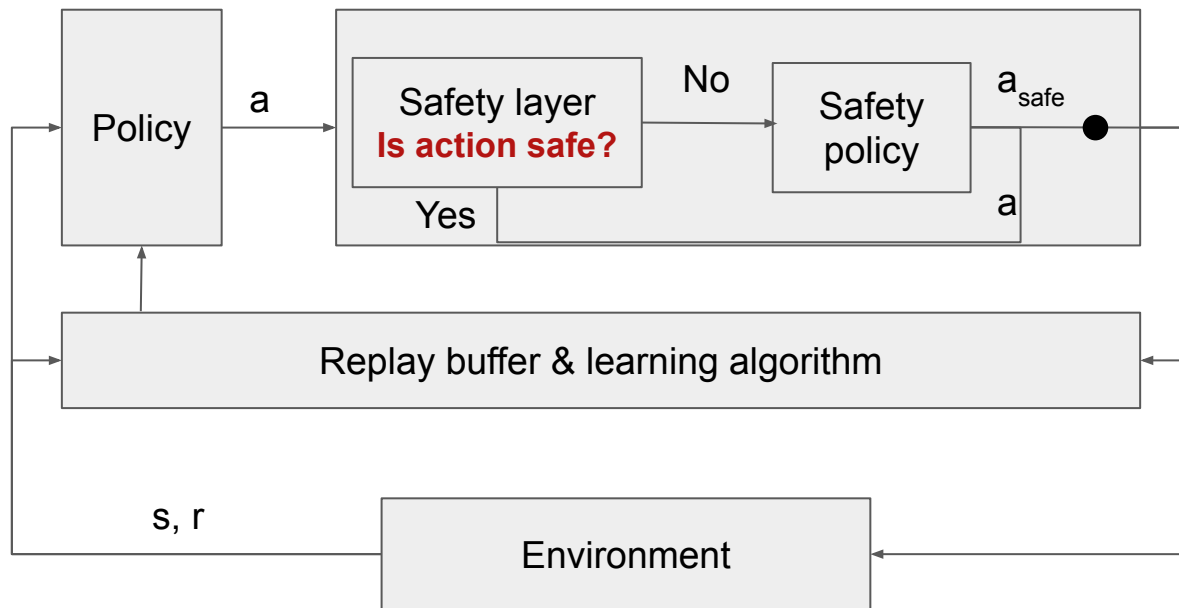


# Safe Learning via Shielding



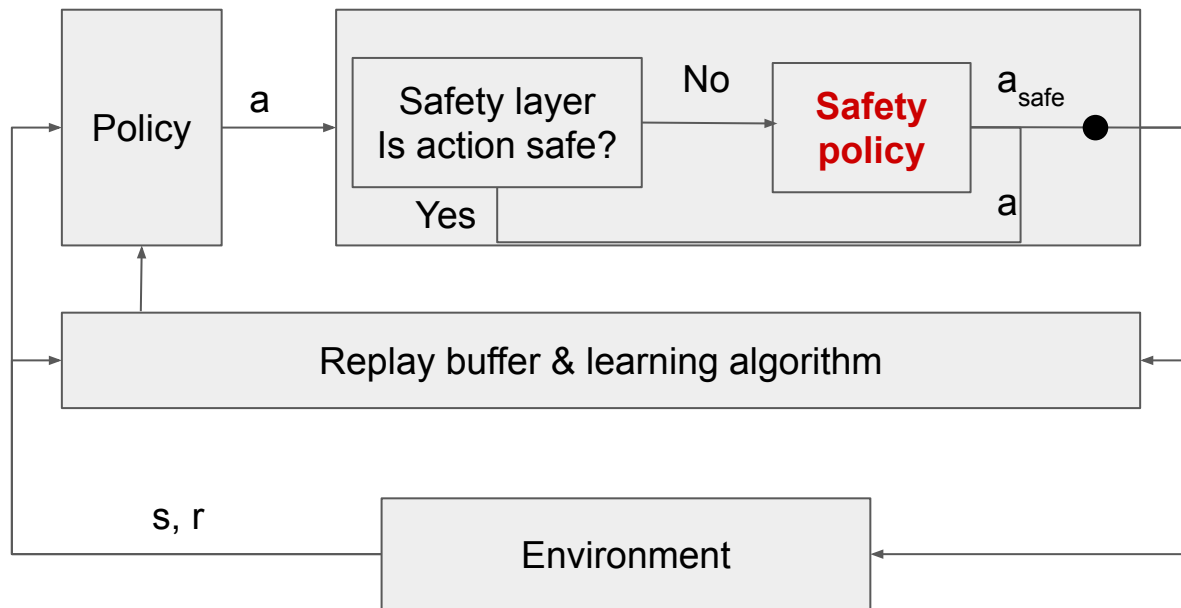
# Two Questions

- How to decide whether an action is safe?



# Two Questions

- How to decide whether an action is safe?
- Where does the safety policy come from?

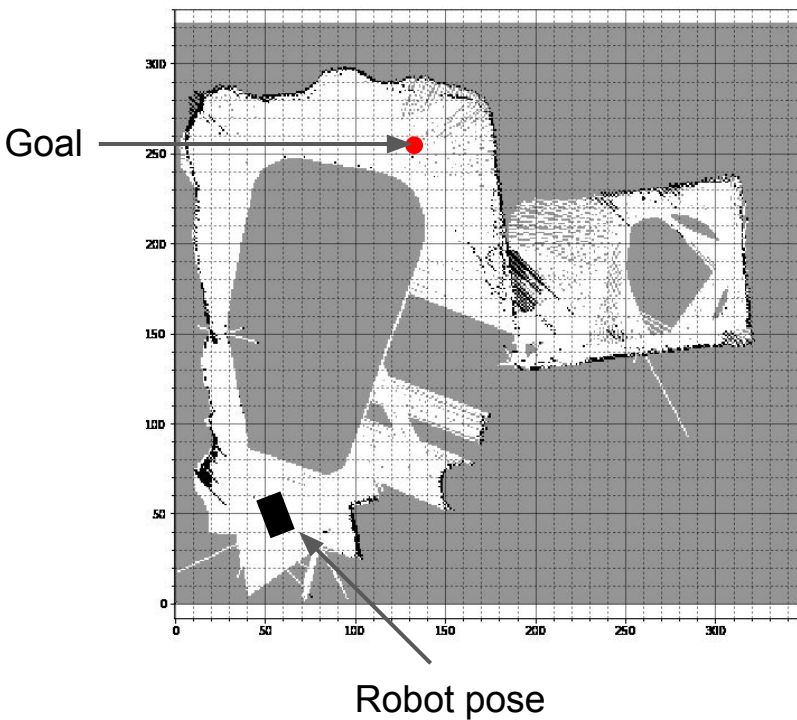


# Two Questions

- How to decide whether an action is safe?
  - Manually specified threshold on actions (e.g. torque limit, joint limit)
  - Future state in safe set by model rollout
  - Query pretrained safety critic: [\[Learning to be Safe: Deep RL with a Safety Critic, Srinivasan et al. 2020\]](#)
- Where does the safety policy come from?
  - Simple engineered solution (e.g. stop)
  - Traditional model-based control (e.g. model-predictive control)
  - Learned safety policy in simulation
    - domain randomization
    - adversarial training: [\[Robust Adversarial Reinforcement Learning, Pinto et al. ICML, 2017\]](#)

# Case Study: Navigation

Observations



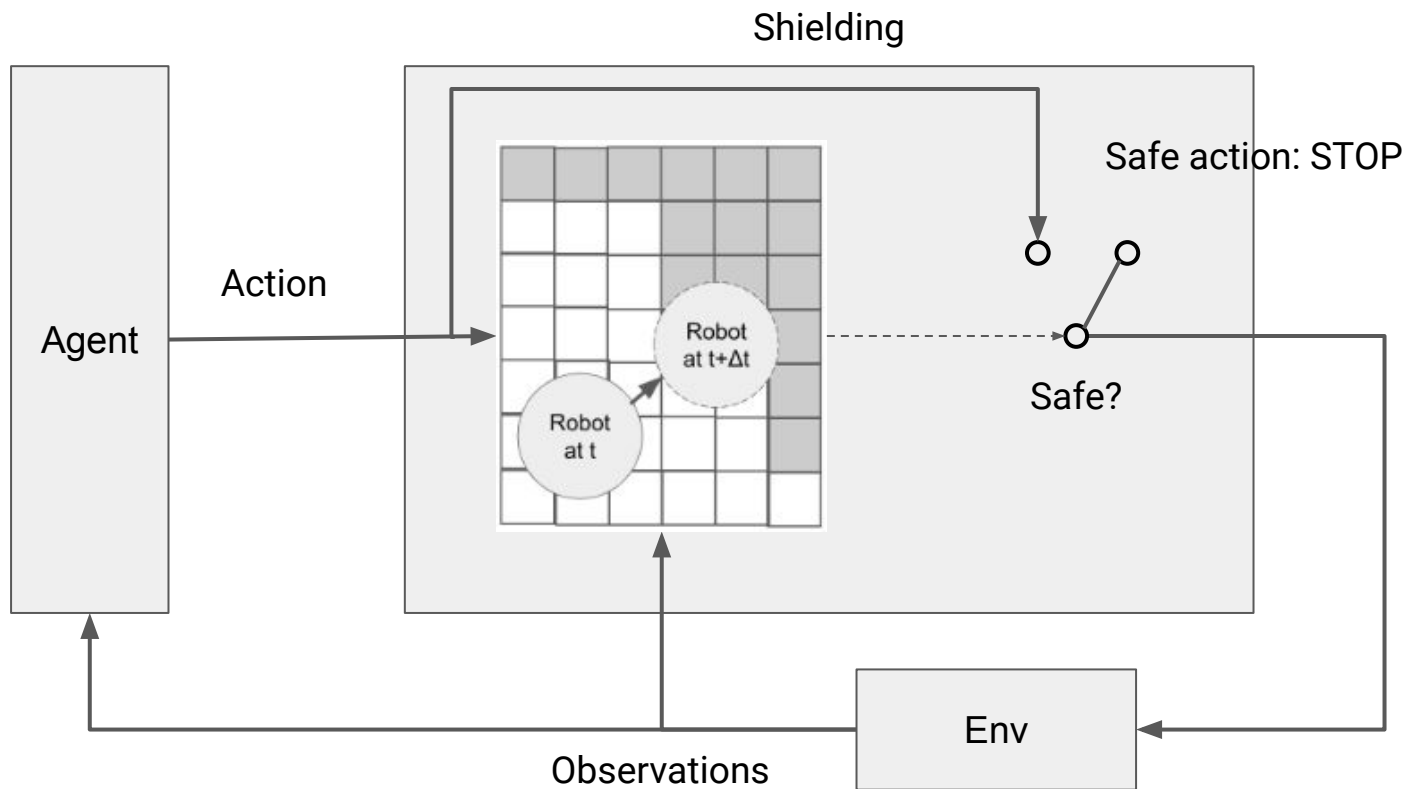
Agent



Actions

Desired turning rate  
Desired speed

# System Overview



# Result of Shielding

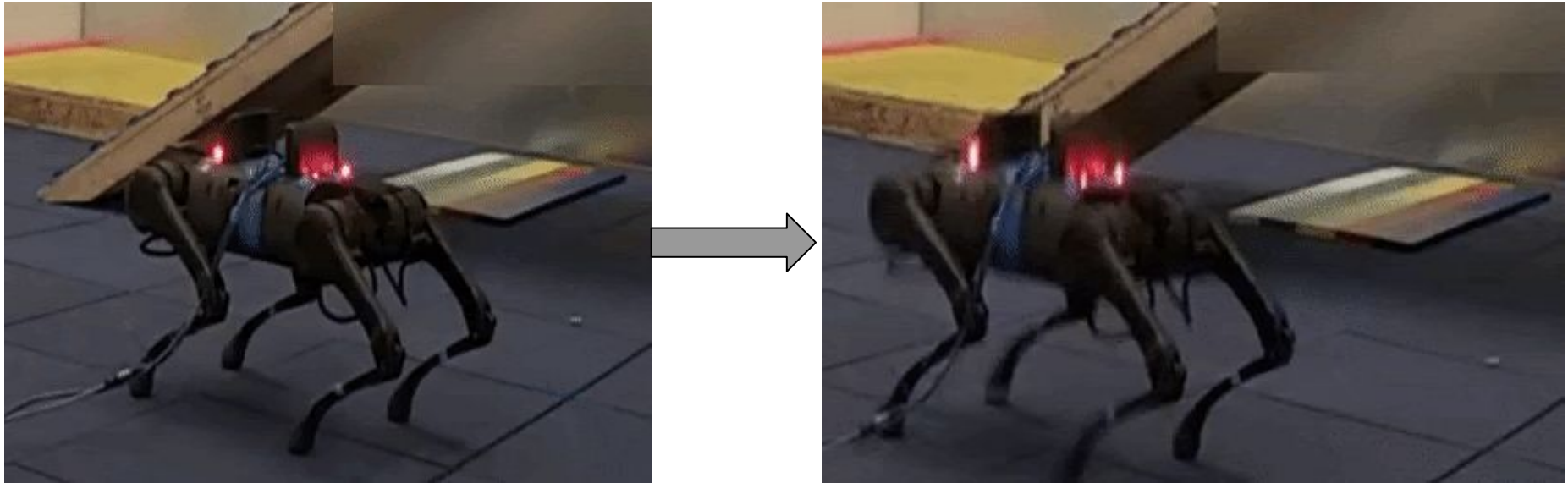


Without shielding



With shielding

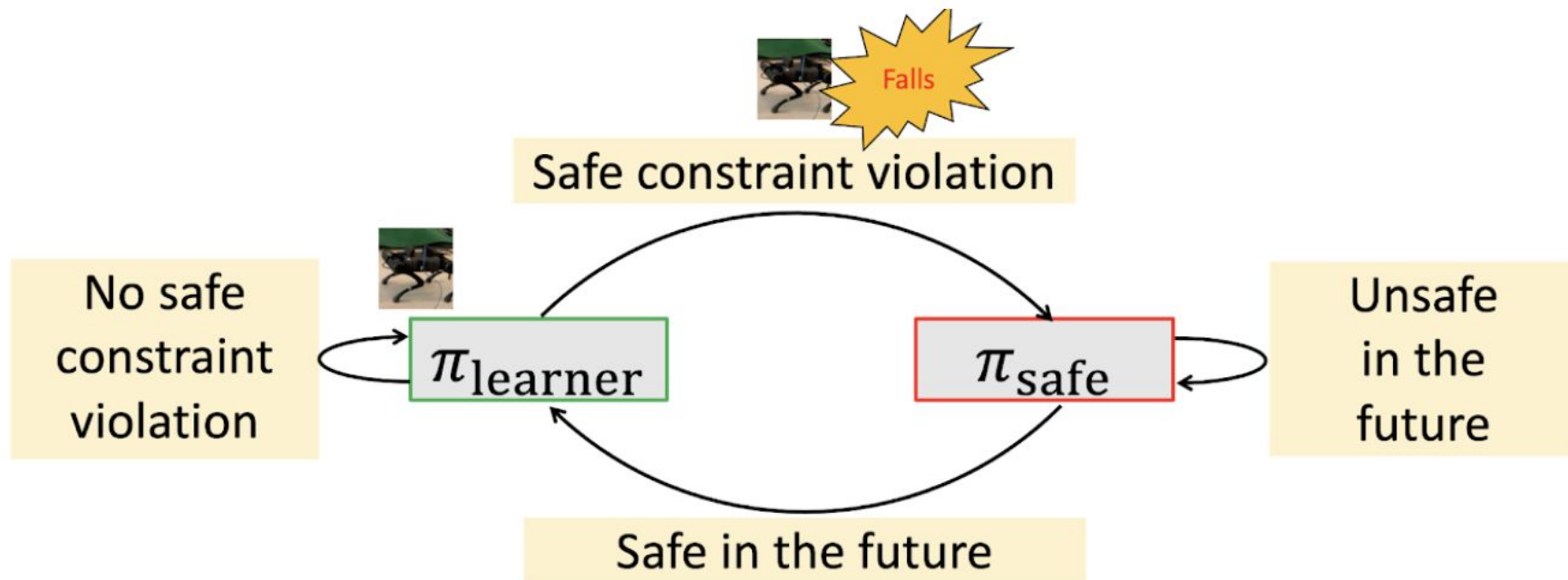
# Case Study: Locomotion



[\[Safe Reinforcement Learning for Legged Locomotion, Yang et al. 2022, Under Review\]](#)



# System Overview



[\[Safe Reinforcement Learning for Legged Locomotion, Yang et al. 2022, Under Review\]](#)

# System Details

- Safe constraint
  - Thresholds on roll and pitch of the base
- Safe policy
  - Model-predictive control based on simplified dynamics
  - RL to modulate MPC parameters (stepping frequency, swing location, etc.)
  - Trained in simulation with domain randomization

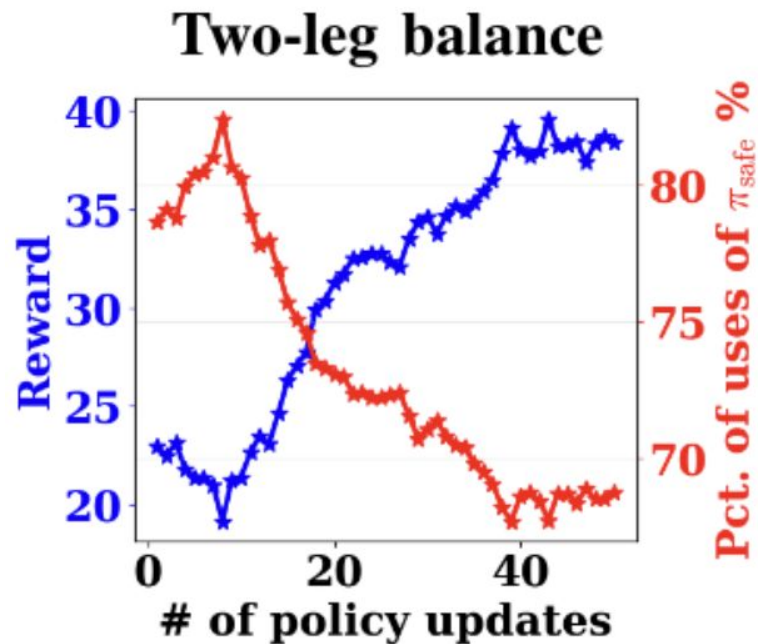
[\[Safe Reinforcement Learning for Legged Locomotion, Yang et al. 2022, Under Review\]](#)

# Training Process (Timelapse)



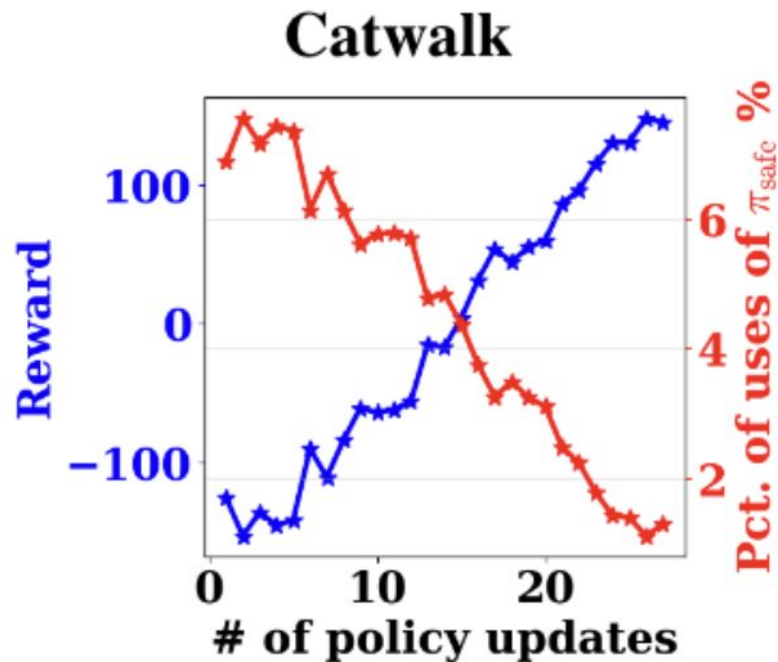
[\[Safe Reinforcement Learning for Legged Locomotion, Yang et al. 2022, Under Review\]](#)

# Results: Two-Leg Balance



[\[Safe Reinforcement Learning for Legged Locomotion, Yang et al. 2022, Under Review\]](#)

# Results: Catwalk



[\[Safe Reinforcement Learning for Legged Locomotion, Yang et al. 2022, Under Review\]](#)

# Limitations

- Switching between two policies can lead to unsafe jerky motions
- Hard to balance between safety and learning efficiency
- Difficult to design or learn safety policies for complex tasks

# Summary

- Formulate safety as constraints
- Two ways to improve safety during learning
  - Constrained Markov Decision Process
  - Safe learning via shielding