Course 02402 Introduction to Statistics Lecture 13:

A course summary

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Agenda - the 12 lectures

- Ochapter 1: Simple Graphics and Summary Statistics
- Chapter 2: Discrete Distributions
- Chapter 2: Continuous Distributions
- Chapter 3: One sample confidence intervals
- 6 Chapter 3: One sample hypothesis testing
- 6 Chapter 3: Two Sample statistics
- Chapter 4: Statistics by simulation
- Chapter 5: Simple linear Regression Analysis
- Ochapter 6: Multiple linear Regression Analysis
- © Chapter 8: One-way Analysis of Variance
- Chapter 8: Two-way Analysis of Variance
- Chapter 7: Inferences for Proportions

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Chapter 1: Simple Graphics and Summary Statistics

- Look at data as it is! (descriptive statistics)
- Summary Statistics
 - Mean \bar{x}
 - Standard deviation s, variance s^2
 - Median, upper- and lower quartiles
- Simple graphics
 - Scatter plot (xy plot)
 - Histogram, cumulative distribution
 - Boxplots, Bar charts, Pie charts

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Chapter 2: Discrete Distributions

- General concepts:
 - Definition of a stochastic variable
 - Density function
 - Distribution function
 - Mean and variance
- Specific distributions:
 - The binomial distribution
 - The hypergeometric distribution
 - The Poisson distribution

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Chapter 2: Continuous Distributions

- General concepts:
 - Density function, distribution function
 - Mean, variance
 - Calculation rules for stochastic variables
- Specific distributions:
 - Normal
 - Log-Normal, Uniform, Exponential

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Chapter 3: One sample confidence intervals

General concepts

- Estimation, confidence intervals
- Population and a random sample
- Sampling distributions (t and χ^2)
- Central Limit Theorem
- Specific methods, one sample:
 - Confidence intervals for the mean
 - Confidence intervals for the variance (and standard deviation)

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Chapter 3: One sample hypothesis testing

- General concepts:
 - Hypotheses, p-value, Significance level
 - Type I and Type II error, Power
- Specific methods, One sample:
 - t-test for mean difference
 - Sample size for wanted power
 - Normal qq-plot

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Chapter 3: Two Samples

- Specific methods, two samples:
 - Test and confidence interval for the mean difference (t-test)
- Specific methods, two PAIRED samples:
 - "Take difference"⇒ "One sample"
- Planning for precision and/or power
 - One-sample Confidence interval: sample size for wanted precision
 - One-sample hypothesis test: sample size for wanted power (or other combinations)
 - Two-sample hypothesis test: sample size for wanted power (or other combinations)

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Chapter 4, Statistics by simulation

- Introduction to simulation
- Error propagation rules
- Bootstrapping
 - Parametric
 - Non-parametric
 - Confidence intervals (and hence also hypothesis testing)
- Specific situations: (4 versions of confidence intervals)
 - One-sample and Two-sample data
 - Parametric and Non-parametric

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Chapter 5: Simple linear Regression Analysis

- Two quantitative variables, x and y.
- Calculating least squares line
- Inferences for a simple linear regression model
 - Statistical model: $y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$
 - Interval estimation and test for β_0 and β_1 .
 - Confidence interval for the expected line.
 - Prediction interval.
- r and r^2
 - r describes the strength of a linear relation.
 - r^2 expresses the proportion of the y variability explained by the linear relation.

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Chapter 6: Multiple linear Regression Analysis

- Many quantitative variables, x_1 , x_2 and y.
- Calculating least squares fit
- Inferences for a the multiple linear regression model
 - Statistical model: $y_i = \beta_0 + \beta_1 x_{1,i} + \beta_2 x_{2,i} \varepsilon_i$
 - Interval estimation and test for β_0 and β_i .
 - Confidence interval for the expected fit.
 - Prediction interval.
- r^2 expresses the proportion of the y variability explained by the linear relation.

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Chapter 8: One-way Analysis of Variance

- Specific methods, k INDEPENDENT samples
- One-way analysis of variance
 - Compares the means of the groups
 - ANOVA-table: SST = SS(Tr) + SSE
 - F-test.
 - Post hoc test: pairwise t-test with/without Bonferroni correction

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Chapter 8: Two-way Analysis of Variance

- Block design two-way analysis of variance
- ANOVA-tabel: SST = SS(Tr) + SS(Bl) + SSE
 - SST, SS(Tr) and SS(Bl) calculated as one-way ANOVA
 - SSE = SST SS(Tr) SS(Bl)
- F-test.
- Post hoc test: pairwise *t*-test with/without
 Bonferroni correction

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Chapter 7: Inferences for Proportions

- Specific methods, one, two and k > 2 samples
 - Binary/categorical response
- Estimation and confidence interval of proportions
 - Large sample vs. small sample methods
- Hypotheses for one proportion
- Hypotheses for two proportions
- Analysis of contingency tables (χ^2 -test) (All expected > 5)

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