

$$\frac{25}{30}$$
Exercise 7.4.6:

Determine the quotient set X / \sim for each of the following equivalence relations.

2. Let $X = \mathbb{Z}$ and define $a \sim b$ if and only if $b - a \in 4\mathbb{Z}$.

$$X / \sim = \{ [0], [1], [2], [3] \}$$

Describe equiv classes

4. Let $X = \mathbb{R}^2$ and define $(x,y) \sim (a,b)$ if and only if one of the following holds:

$$x \geq 0, y \geq 0, a \geq 0, b \geq 0$$

$$x < 0, y < 0, a < 0, b < 0$$

$$xy < 0 \text{ and } ab < 0.$$

$$x = 0 \text{ and } y < 0 \text{ and } a = 0 \text{ and } b < 0.$$

$$y = 0 \text{ and } x < 0 \text{ and } b = 0 \text{ and } a < 0.$$

$$X / \sim = \{ [(1,1)], [(-1,-1)], [(1,-1)], [(0,-1)], [(-1,0)] \}$$

picture helps,
but needs more
description