

1.
  - False.  $2^{\{c * \sqrt{n}\}} = (2^c)^{\sqrt{n}}$ . For example, let  $c = 2$ , then we have  $4^{\sqrt{n}}$ , which is not bounded by  $2^{\sqrt{n}}$
  - True.
  - True. big-O is an upper bound, but not a tight upper bound.
  - False. The worst case running time is  $O(kn)$ . (Note, this isn't the best worded question.)
  - False. Let  $f = 2n$ .  $f$  is  $O(n)$ , but  $2^{\{2n\}} = 4^n$  is not  $O(2^n)$

2.
  - a.  $\Theta(n \log n + k) = \Theta(n \log n)$  -- note  $k$  is always less than  $n$  so we can drop it.
  - b.  $\Theta(kn)$
  - c. Unfortunately, selection is  $O(n^2)$  in the worst case. If you ignore this (technically, not correct),  $O(n + k \log k)$ . Alternative answers would be to put in a heap:  $O(n + k \log n)$

3.
 

call `findShift(1, A.length, A)`

```
findShift(s, e, A)
- mid = (e-s)/2
- if A[mid-1] > A[mid] -> return mid-1
- if A[s] > A[mid] -> return findShift(s, mid, A)
- else -> return findShift(mid, e, A)
```

4.
  - a. Master method
 

$a = 3$   
 $b = 3$   
 $f(n) = \log n$

$f(n) = O(n^{0.9})$  so  $T(n) = \Theta(n)$

- b. Recursion tree method
 

$T(n) = \sum_{i=1}^n n^d \log n = n * n^d \log n = n^{\{d+1\}} \log n$