

Group 3

● Graded

Group

kambenh liban karshe

Collins Munene Kariuki

Blessing Adomakoh

...and 3 more

 [View or edit group](#)

Total Points

1 / 1 pts

Question 1

[Attended and participated](#)

1 / 1 pt

✓ - 0 pts Correct

No questions assigned to the following page.

CS140 - Group Assignment 3

Due: Friday, Feb. 9 at 10pm

Note: you only need to submit one assignment *per group*.

1. Induction on trees

Use a proof by strong induction to show that a binary tree of height h has at most 2^h leaf nodes.

2. Recreating binary search trees

- (a) Suppose that we have numbers between 1 and 1000 in a binary search tree, and we want to search for the number 363. Which (and there might be more than one) of the following sequences could *not* be the sequence of nodes examined?

- i. 2, 252, 401, 398, 330, 344, 397, 363
- ii. 924, 220, 911, 244, 898, 258, 362, 363
- iii. 925, 202, 911, 240, 912, 245, 363
- iv. 2, 399, 387, 219, 266, 382, 381, 278, 363
- v. 935, 278, 347, 621, 299, 392, 358, 363

- (b) Given any sequence of numbers and any number for which you're searching, how could you determine whether the sequence could be the sequence of nodes examined?

3. Group experience

What was each person's favorite class in high school? Least favorite? (Don't forget your TA!)

No questions assigned to the following page.

1. Induction on trees

Use a proof by strong induction to show that a binary tree of height h has at most 2^h leaf nodes.

Base case: Only the leaf node.
 $2^h = 2^0 = 1$ (True).

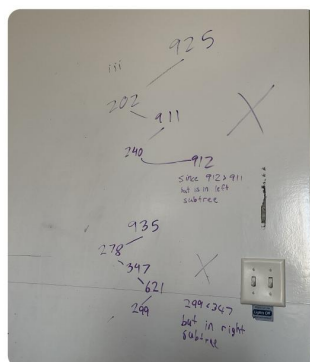
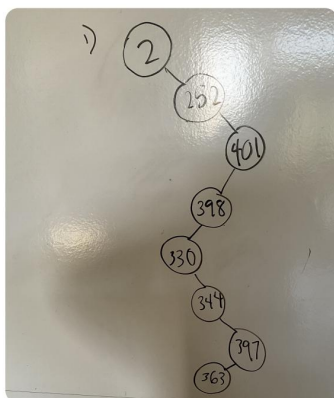
Inductive hypothesis: Assume all subtrees of x have $\leq 2^j$ leaf nodes for $0 \leq j \leq k$.

leaf = # leaf left + # leaf right
 $\leq 2^{j-1} + 2^{j-1} = 2 \cdot 2^{j-1} = 2^j$

2. Recreating binary search trees

(a) Suppose that we have numbers between 1 and 1000 in a binary search tree, and we want to search for the number 363. Which (and there might be more than one) of the following sequences could *not* be the sequence of nodes examined?

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- 2, 399, 387, 219, 266, 382, 381, 278, 363
- 935, 278, 347, 621, 299, 392, 358, 363



(b) Given any sequence of numbers and any number for which you're searching, how could you determine whether the sequence could be the sequence of nodes examined?

Given sequence

When we go left the number preceding the new number on the left side is the new-max

When we go right the number preceding the new number on the right side is the new-min

No questions assigned to the following page.

3. Group experience

What was each person's favorite class in high school? Least favorite? (Don't forget your TA!)

REDiet: Fav: IB History least Fav: Bio

SOPhia: Favorite: math least fav: Chem

COLlin: Fav: physics least fav: bio

nizl: Fav: gov least fav: Chem

BLESSing: Fav: IB psychology HL, least fav: AP Euro

Kambel: Fav: Art, least Fav: English