RPr-Spielman-2020

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1 Reproduction of Spielman et al's 2020 Evaluation of the Social Vulnerability Index

1.0.1 Authors

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1.0.2 Abstract

This study is a reproduction of:

Spielman, S. E., Tuccillo, J., Folch, D. C., Schweikert, A., Davies, R., Wood, N., & Tate, E. (2020). Evaluating Social Vulnerability Indicators: Criteria and their Application to the Social Vulnerability Index. Natural Hazards, 100(1), 417–436. https://doi.org/10.1007/s11069-019-03820-z

The Spielman et al (2020) paper is in turn a replication of:

Cutter, S. L., Boruff, B. J., & Shirley, W. L. (2003). Social vulnerability to environmental hazards. Social Science Quarterly, 84(2), 242–261. https://doi.org/10.1111/1540-6237.8402002

Spielman et al (2020) developed methods to evaluate the internal consistency and construct validity of the Cutter, Boruff and Shirley (2003) Social Vulnerability Index (SoVI). First, they reproduce a national SoVI model and validate it against an SPSS procedure provided by the original research group (Hazards Vulnerability Research Institute at University of South Carolina). The original SoVI uses 42 independent z-score normalized variables from the U.S. Census, reduces the data to factors using Principal Components Analysis, selects the first eleven factors, inverts factors with inverse relationships to social vulnerability, and sums the factors together to produce a SoVI score. The reproduced SoVI model was slightly different than the original model due to changes in U.S. Census data, using only 28 variables.

Spielman et al. modify the geographic extent of the SoVI calculation by calculating SoVI on a national extent, and then recalculating for each of ten Federal Emergency Management Agency (FEMA) regions, and again for a single state or cluster of states within each of the ten regions, resulting in 21 total indices. Internal consistency is assessed by calculating the spearman rank correlation coefficient of the SoVI score for counties in the state model compared to the FEMA region

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model and national model. Construct validity is assessed by summing the loadings for each input variable across the PCA factors in each model and calculating the variables sign (positive/negative) and the rank of the variable's total loading compared to the other variables. These signs and ranks are summarized across all 21 versions of the SoVI model with regard to the number of times the sign is different from the national model and the distributions of ranks.

In this reproduction study, we attempt to reproduce identical SoVI model outputs for each of the 21 models in the original study. We will compare these outputs to data files in Spielman et al.'s GitHub repository. We will also attempt to reproduce identical results of internal consistency analysis (figure 1 and table 2) and construct validity analysis (figure 2) from Spielman et al.'s paper. We succeed in reproducing identical SoVI model outputs, but find slight discrepancies in our figures and tables.

The code in this Jupyter notebook report is adapted from Spielman et al's GitHub repository. The original study states the intended open source permissions in the acknowledgements: "To facilitate advances to current practice and to allow replication of our results, all of the code and data used in this analysis is open source and available at (https://github.com/geoss/sovi-validity). Funding was provided by the US National Science Foundation (Award No. 1333271) and the U.S. Geological Survey Land Change Science Program."

1.0.3 Keywords

Social vulnerability, social indicators, Principal Component Analysis, reproducibility

1.1 Study design

We computationally reproduce Spielman et al's original work using the code provided in their Github repository (https://github.com/geoss/sovi-validity), adapting their code to run in an updated Python environment using current package versions. We make all of our work available online using the HEGSRR reproducible research compendium template.

The original paper was a replication study testing the sensitivity of SoVI to changes in geographic extent. Spielman et al addressed the following hypotheses in their work:

OR-H1: SoVI is internally inconsistent.

To address this hypothesis, Spielman et al illustrated that SoVI is not robust to changes in geographic extent by calculating SoVI scores for ten selected states or groups of states on three geographic extents: national, FEMA region, and state(s). The counties within the state(s) of interest were then selected and ranked according to their SoVI score. OR-H1 was tested by calculating Spearman's rank correlation between the state and FEMA region models and between the state and national models.

OR-H2: SoVI is theoretically inconsistent.

To address this hypothesis, Spielman et al used the same SoVI models as described under OR-H1. For each model, they summed all of the PCA factors together to determine the net influence of each variable in each model. Then they recorded the signs of each variable and calculated the number of deviations of the ten state and FEMA region models from the national model. They also ranked the variables by absolute value for each model and calculated summary statistics regarding the distribution of ranks for each variable amongst all models. Spielman et al did not use

a particular statistical method to test OR-H2, but illustrated substantial disagreements between variable rankings and signs amongst the 21 SoVI models.

For our reproduction, we address the following three hypotheses:

RPr-H1: Reproduced SoVI model scores and other reproduced output datasets are not identical to the original study SoVI model scores and provided output datasets for each of the 21 SoVI models.

RPr-H2: Reproduced figures and tables for the internal consistency analysis are not identical to the figures and tables (figure 1 and table 2) of the original study.

RPr-H3: For the theoretical consistency analysis, reproduced direction reversals and min, average, and max SoVI rank value of 28 demographic variables are not identical to the direction reversals and min, average, and max SoVI rank values shown in figure 2 of the original study.

We answer these questions by working through Spielman et al's code line by line in an updated python coding environment. To improve reproducibility, we reorganize Spielman's repository into the Template for Reproducible and Replicable Research in Human-Environment and Geographical Sciences (doi:10.17605/OSF.IO/W29MQ) and use one Jupyter notebook for the reproduction report and code. We catalogue barriers to reproducibility and make improvements wherever possible.

Disclaimer: we worked with the data and code before writing this report, so there is no preregistration of the analysis plan. We originally intended to publish only a replication of this study; we did not anticipate publishing a reproduction until we spent some time working with the code.

Spatio-temporal metadata

- Spatial Coverage: United States, excluding Puerto Rico
- Spatial Resolution: Counties and county equivalents
- Spatial Reference System: EPSG:4269
- Temporal Coverage: 2008 2012 (data is the 2012 5-year ACS)
- Temporal Resolution: One-time measurement, does not address change over time

1.2 Materials and procedure

1.2.1 Computational environment

Currently, we are using a 2020 MacBook Pro running on macOS Ventura 13.3.1. We anticipate collaborators working on the project from different computers and different operating systems, and we seek to containerize the project so that scripts can be run on many different machines.

The original study used Python for their analysis, so we reproduce their results in Python, using a containerized conda environment. This environment consists of Python 3.9.16 and the software packages listed in requirements.txt

To set up this environment on another machine, one should install the correct version of Python and run the cell below to install the correct package versions. If a user wishes to create a self-contained environment, they should explore very, conda, or pipenv virtual environments.

```
[1]: %%script echo skipping # comment this line out to run this cell

!pip install -r ../environment/requirements.txt
```

```
[2]: # Import modules, define directories
     import pygris
     import pandas as pd
     import geopandas as gpd
     from pygris.data import get_census
     from pygris import counties
     from pyhere import here
     import numpy as np
     import libpysal as lps
     import lxml
     import tabulate
     from scipy.stats import spearmanr
     from scipy.stats.mstats import zscore as ZSCORE
     from scipy.stats import rankdata
     import mdp as MDP
     from operator import itemgetter
     import copy
     from matplotlib.colors import ListedColormap
     from matplotlib import patheffects as pe
     import matplotlib.pyplot as plt
     from IPython import display
     from IPython.display import Markdown, Latex
     pd.set option("chained assignment", None)
     path = {
         "dscr": here("data", "scratch"),
         "drpub": here("data", "raw", "public", "spielman", "input"),
         "drpub2": here("data", "raw", "public"),
         "drpriv": here("data", "raw", "private"),
         "ddpub": here("data", "derived", "public", "version1"),
         "ddpriv": here("data", "derived", "private"),
         "rfig": here("results", "figures"),
         "roth": here("results", "other"),
         "rtab": here("results", "tables"),
         "og_out": here("data", "raw", "public", "spielman", "output"),
         "dmet": here("data", "metadata")
     }
[3]: | %%script echo skipping # Save computational environment
     # Note that this approach is not perfect -- it may miss some packages
```

skipping # Save computational environment

!pip install pigar

!python -m pigar generate

1.2.2 Data and variables

For Spielman et al's original study, the data sources were the 2008-2012 5-year American Community Survey and the 2010 decennial census. Spielman et al downloaded their data from Social Explorer; in our reproduction, we pull our data directly from the census into Python via a census API package known as pygris. These variables are based on the original work by Cutter et al to create SoVI, and cover a wide range of social and demographic information, the particulars of which are described below.

In order to confirm that our data and Spielman et al's data perfectly match each other, we import the names of relevant variables from both datasets here.

(1) 2008-2012 American Community Survey (5-year) Used in both original study and reproduction.

Planned deviation: to enhance reproducibility, we draw the data directly from the census into python using the pygris package.

```
[5]: \%script echo skipping # Comment this first line out if you wish to acquire
      ⇔data directly from census
     # Acquire attribute data for reproduction
     counties_detailed = get_census(dataset = "acs/acs5", # dataset name on the_
      Gensus API you are connecting to; find datasets at https://api.census.gov/
      \hookrightarrow data.html
                              variables = acs_variables, # string (or list of_
      ⇔strings) of desired vars. For the 2021 5-year ACS Data Profile, those⊔
      -variable IDs are found at https://api.census.gov/data/2021/acs/acs5/profile/
      \hookrightarrow variables.html
                              year = 2012, # year of your data (or end-year for all
      ⇔5-year ACS sample)
                              params = { # dict of query parameters to send to the
      \hookrightarrow API.
                                "for": "county:*"},
                              guess_dtypes = True,
                              return_geoid = True)
     # Drop Puerto Rico
     counties_detailed = counties_detailed.loc[~counties_detailed['GEOID'].str.
      ⇔startswith('72')]
```

```
# Download and save raw data
counties_detailed.to_csv( here(path["drpub2"], "counties_attributes_raw.csv"))
```

skipping # Comment this first line out if you wish to acquire data directly from census

```
[6]: # Optionally, load data directly from the repository
counties_detailed = pd.read_csv( here(path["drpub2"], "counties_attributes_raw.

→csv"), dtype = {'GEOID': object} )
counties_detailed = counties_detailed.drop(counties_detailed.columns[0],axis=1)
```

```
[8]: Markdown(here(path["dmet"], "ACS_2012_geographic_metadata.md"))
```

- [8]:
- Title: American Community Survey 2012 5-year Estimate Demographic Variables
- Abstract: The 5-year ACS provides estimates surrounding demographic information in the USA. These estimates are more reliable than 1-year and 3-year estimates but less reliable than decennial census data. On the other hand, 5-year estimates are less current than 1-year and 3-year estimates because they represent measurements taken over 60 months. See the census website for more details.
- Spatial Coverage: United States, excluding Puerto Rico
- Spatial Resolution: County and county-equivalents
- Spatial Reference System: None, just attribute data
- Temporal Coverage: 2008-2012
- Temporal Resolution: Data averaged over five years
- Lineage: Original data downloaded from Social Explorer and then placed in the original study's GitHub repository: https://github.com/geoss/sovi-validity. Reproduction data obtained directly from the census via API.
- Distribution: The reproduction data is distributed via a census API. See the detailed tables on the census website and instructions for drawing census data directly into python on the pygris website. Spielman et al originally accessed the ACS data with Social Explorer from

the following two tables.

- $-\ http://www.socialexplorer.com/pub/reportdata/HtmlResults.aspx?reportid=R10728365$
- $-\ http://www.socialexplorer.com/pub/reportdata/HtmlResults.aspx?reportid=R10775556$
- Constraints: Census data is available in the public domain
- Data Quality: Margin of error provided by the Census Bureau for relevant variables
- Variables: See ACS_2012_data_dictionary.csv

[9]: acs_vars

[9]:		Reproduction Label	Spielman Label	\
	0	GEOID	Geo_FIPS	
	1	B01002_001E	ACS12_5yr_B01002001	
	2	B03002_001E	ACS12_5yr_B03002001	
	3	B03002_004E	ACS12_5yr_B03002004	
	4	B03002_005E	ACS12_5yr_B03002005	
	5	B03002_006E	ACS12_5yr_B03002006	
	6	B03002_012E	ACS12_5yr_B03002012	
	7	B06001_002E	ACS12_5yr_B06001002	
	8	B09020_001E	ACS12_5yr_B09020001	
	9	B01003_001E	ACS12_5yr_B01003001	
	10	B25008_001E	ACS12_5yr_B25008001	
	11	B25002_002E	ACS12_5yr_B25002002	
	12	B25003_003E	ACS12_5yr_B25003003	
	13	B25002_001E	ACS12_5yr_B25002001	
	14	B09020_021E	ACS12_5yr_B09020021	
	15	B01001_026E	ACS12_5yr_B01001026	
	16	B11001_006E	ACS12_5yr_B11001006	
	17	B11001_001E	ACS12_5yr_B11001001	
	18	B25002_003E	ACS12_5yr_B25002003	
	19	B19025_001E	ACS12_5yr_B19025001	
	20	B23022_025E	ACS12_5yr_B23022025	
	21	B23022_049E	ACS12_5yr_B23022049	
	22	B23022_001E	ACS12_5yr_B23022001	
	23	B17021_002E	ACS12_5yr_B17021002	
	24	B17021_001E	ACS12_5yr_B17021001	
	25	B25024_010E	ACS12_5yr_B25024010	
	26	B25024_001E	ACS12_5yr_B25024001	
	27	C24010_038E	ACS12_5yr_C24010038	
	28	C24010_001E	ACS12_5yr_C24010001	
	29	B19055_002E	ACS12_5yr_B19055002	
	30	B19055_001E	ACS12_5yr_B19055001	
	31	B09002_002E	ACS12_5yr_B09002002	
	32	B09002_001E	ACS12_5yr_B09002001	
	33	B19001_017E	ACS12_5yr_B19001017	
	34	B06007_005E	ACS12_5yr_B06007005	
	35	B06007_008E	ACS12_5yr_B06007008	
	36	B06007_001E	ACS12_5yr_B06007001	

37 38 39 40 41 42 43 44	B16010_002E
0	Alias FIDS code unique identifier
0 1	FIPS code unique identifier median age
2	total population of respondents to race/ethnicity
3	total Black population
4	total Native American population
5	total Asian population
6	total Latinx population
7	total population under 5 years of age
8	total population over 65 years of age
9	total population
10	total population in occupied housing units
11	total occupied housing units
12	total renter occupied housing units
13 14	total housing units for which occupancy status total 65+ living in group quarters
15	total of living in gloup quarters total female population
16	total female-headed family households
17	total households for which household type is k
18	total vacant housing units
19	aggregate household income
20	total males unemployed for last 12 months
21	total females unemployed for last 12 months
22	total population for which unemployment and se
23	total population below poverty level
24	total population for which poverty information
25 26	number of mobile home housing units in structure total housing units in structure
27	total housing units in structure total female employed
28	total population for which sex and occupation
29	total households with social security income
30	total households for which social security inc
31	total children in married couple families
32	total children for which family type and age a
33	total households with over 200k income
34	total Spanish-speakers who speak english less
35	total people who speak another language and sp

```
36
    total population with known language spoken at...
37
    total population with less than a high school ...
38
    total for which education, employment, languag...
39
            total population in extractive industries
40
            total population for which industry known
41
                  total people in service occupations
42
           total households with no available vehicle
    total households for which vehicle status and ...
43
44
                                     median gross rent
45
                                     median home value
                                             Definition
                                                             Type \
0
    Unique code for every county and county-equiva...
                                                         string
1
       MEDIAN AGE BY SEX: Estimate!!Median age!!Total
                                                         float64
2
    HISPANIC OR LATINO ORIGIN BY RACE: Estimate!!T...
                                                          int64
3
    HISPANIC OR LATINO ORIGIN BY RACE: Estimate!!T...
                                                          int64
    HISPANIC OR LATINO ORIGIN BY RACE: Estimate!!T...
4
                                                          int64
5
    HISPANIC OR LATINO ORIGIN BY RACE: Estimate!!T...
                                                          int64
    HISPANIC OR LATINO ORIGIN BY RACE: Estimate!!T...
                                                          int64
7
    PLACE OF BIRTH BY AGE IN THE UNITED STATES: Es...
                                                       float64
    RELATIONSHIP BY HOUSEHOLD TYPE (INCLUDING LIVI...
8
                                                          int64
9
                     TOTAL POPULATION: Estimate!!Total
                                                            int64
    TOTAL POPULATION IN OCCUPIED HOUSING UNITS BY ...
                                                          int64
10
          OCCUPANCY STATUS: Estimate!!Total!!Occupied
11
                                                            int64
12
             TENURE: Estimate!!Total!!Renter occupied
                                                            int64
13
                     OCCUPANCY STATUS: Estimate!!Total
                                                            int64
    RELATIONSHIP BY HOUSEHOLD TYPE (INCLUDING LIVI...
14
                                                          int64
15
                  SEX BY AGE: Estimate!!Total!!Female
                                                            int64
16
    HOUSEHOLD TYPE (INCLUDING LIVING ALONE): Estim ...
                                                          int64
    HOUSEHOLD TYPE (INCLUDING LIVING ALONE): Estim ...
17
                                                          int64
18
            OCCUPANCY STATUS: Estimate!!Total!!Vacant
                                                            int64
    AGGREGATE HOUSEHOLD INCOME IN THE PAST 12 MONT...
19
                                                          int64
    SEX BY WORK STATUS IN THE PAST 12 MONTHS BY US...
20
                                                          int64
    SEX BY WORK STATUS IN THE PAST 12 MONTHS BY US...
21
                                                          int64
    SEX BY WORK STATUS IN THE PAST 12 MONTHS BY US...
                                                          int64
23
    POVERTY STATUS OF INDIVIDUALS IN THE PAST 12 M...
                                                          int64
24
    POVERTY STATUS OF INDIVIDUALS IN THE PAST 12 M...
                                                          int64
25
     UNITS IN STRUCTURE: Estimate!!Total!!Mobile home
                                                            int64
26
                  UNITS IN STRUCTURE: Estimate!!Total
                                                            int64
27
    SEX BY OCCUPATION FOR THE CIVILIAN EMPLOYED PO ...
                                                          int64
    SEX BY OCCUPATION FOR THE CIVILIAN EMPLOYED PO ...
28
                                                          int64
29
    SOCIAL SECURITY INCOME IN THE PAST 12 MONTHS F ...
                                                          int64
    SOCIAL SECURITY INCOME IN THE PAST 12 MONTHS F...
                                                          int64
31
    OWN CHILDREN UNDER 18 YEARS BY FAMILY TYPE AND ...
                                                          int64
    OWN CHILDREN UNDER 18 YEARS BY FAMILY TYPE AND ...
32
                                                          int64
   HOUSEHOLD INCOME IN THE PAST 12 MONTHS (IN 201...
33
                                                          int64
   PLACE OF BIRTH BY LANGUAGE SPOKEN AT HOME AND ...
                                                       float64
```

35	PLACE OF BIRTH BY LANGUAGE SPOKEN AT HOME AND	float64
36	PLACE OF BIRTH BY LANGUAGE SPOKEN AT HOME AND	float64
37	EDUCATIONAL ATTAINMENT AND EMPLOYMENT STATUS B	int64
38	EDUCATIONAL ATTAINMENT AND EMPLOYMENT STATUS B	int64
39	INDUSTRY BY OCCUPATION FOR THE CIVILIAN EMPLOY	int64
40	INDUSTRY BY OCCUPATION FOR THE CIVILIAN EMPLOY	int64
41	INDUSTRY BY OCCUPATION FOR THE CIVILIAN EMPLOY	int64
42	HOUSEHOLD SIZE BY VEHICLES AVAILABLE: Estimate	int64
43	HOUSEHOLD SIZE BY VEHICLES AVAILABLE: Estimate	int64
44	MEDIAN GROSS RENT (DOLLARS): Estimate!!Median	int64
45	MEDIAN VALUE (DOLLARS): Estimate!!Median value	float64

	Domain	Missing Data Value(s)	Missing Data Frequency
0	01001 - 56045	None	0.0
1	21.7 - 63	NaN	0.0
2	66 - 9840024	NaN	0.0
3	0 - 1267825	NaN	0.0
4	0 - 59060	NaN	0.0
5	0 - 1343920	NaN	0.0
6	0 - 4694846	NaN	0.0
7	0 - 651662	NaN	78.0
8	5 - 1078555	NaN	0.0
9	66 - 9840024	NaN	0.0
10	62 - 9664175	NaN	0.0
11	35 - 3218511	NaN	0.0
12	14 - 1695180	NaN	0.0
13	70 - 3441416	NaN	0.0
14	0 - 37611	NaN	0.0
15	20 - 4987765	NaN	0.0
16	0 - 498851	NaN	0.0
17	35 - 3218511	NaN	0.0
18	35 - 245069	NaN	0.0
19	1785600 - 263044380000	NaN	0.0
20	1 - 726803	NaN	0.0
21	0 - 1131737	NaN	0.0
22	45 - 6658456	NaN	0.0
23	0 - 1658231	NaN	0.0
24	64 - 9684503	NaN	0.0
25	0 - 85377	NaN	0.0
26	70 - 3441416	NaN	0.0
27	12 - 2056023	NaN	0.0
28	54 - 4495118	NaN	0.0
29	9 - 726298	NaN	0.0
30	35 - 3218511	NaN	0.0
31	0 - 1380977	NaN	0.0
32	0 - 2032147	NaN	0.0
33	0 - 208954	NaN	0.0

34	0 - 1695391	NaN	78.0
35	0 - 743418	NaN	78.0
36	66 - 9188362	NaN	78.0
37	5 - 1508273	NaN	0.0
38	65 - 6380366	NaN	0.0
39	0 - 54942	NaN	0.0
40	54 - 4495118	NaN	0.0
41	4 - 837607	NaN	0.0
42	0 - 577967	NaN	0.0
43	35 - 3218511	NaN	0.0
44	275 - 1678	NaN	0.0
45	19400 - 944100	NaN	1.0

The above are the metadata files that we wrote for our pygris-acquired version of this data, stored as ACS_2012_data_dictionary.csv and ACS_2012_geographic_metadata.md. The metadata files provided by Spielman et al are also in our repository, named sovi_acs.txt and sovi_acs_kids.txt.

(2) 2010 Decennial Census Used in Spielman et al's original study.

[11]: Markdown(here(path["dmet"], "dec_2010_metadata.md"))

[11]:

- Title: 2010 Decennial Census
- Abstract: Collected once every ten years, the decennial census documents demographic and population data in the United States.
- Spatial Coverage: United States, excluding Puerto Rico
- Spatial Resolution: County and county-equivalents
- Spatial Reference System: None, just attribute data
- Temporal Coverage: 2010
- Temporal Resolution: One-time observations
- Lineage: Original data downloaded from Social Explorer and then placed in the original study's GitHub repository: https://github.com/geoss/sovi-validity.
- Distribution: Visit this URL for access
- Constraints: Census data is available in the public domain
- Data Quality: Margin of error provided by the Census Bureau for relevant variables
- Variables:

						Missing	Missing
						Data	Data Fre-
Label	Alias	Definition	Type	Accuracy	Domain	Value(s)	quency
SE_T02A_	_01022nd area	Area	float64	•••	1.998779	nan	0
		(Land) in			-		
		square			145504.8		
		miles					

Label	Alias	Definition	Type	Accuracy	Domain	Missing Data Value(s)	Missing Data Frequency
Geo_FIPS	FIPS code unique identifier	Unique code for every county and county- equivalent in USA	string		g01001 - g56045	None	0

Original metadata file provided by Spielman et al as sovi_decennial_sup1.txt.

(3) USA Counties Shapefile Used in Spielman et al's original study

```
[12]: spielman_geom = gpd.read_file( here(path["drpub"], "USA_Counties_500k.shp") )
[13]: Markdown( here(path["dmet"], 'USA_counties_metadata.md') )
```

- [13]:
- Title: USA Counties Geographic Shapefile
- Abstract: No metadata provided, so it is unclear exactly where Spielman et al acquired this file but they likely downloaded it directly or indirectly from the census. The shapefile provides the geometries of counties and county-equivalents in the United States, with limited attribute information including county name and a unique identifier.
- Spatial Coverage: United States, excluding Puerto Rico
- Spatial Resolution: County and county-equivalents
- Spatial Reference System: EPSG:4269
- Temporal Coverage: Unknown
- Temporal Resolution: One-time observations
- Lineage: Unknown
- Distribution: Unknown. Presumably downloaded from census.
- Constraints: Census data is available in the public domain
- Data Quality: 1:500,000 scale
- Variables: For each variable, enter the following information. If you have two or more variables per data source, you may want to present this information in table form (shown below)

Label	Alias	Definition	Type	Accuracy	Domain	Missing Data Value(s)	Missing Data Frequency
geoFIPS	FIPS code unique identifer	Unique code for every county and county-equivalent in USA	string		g01001 - g56045	None	0

No original metadata file provided.

(4) USA Counties Cartographic Boundaries Used in reproduction study.

Planned deviation: to enhance reproducibility, we draw the data directly from the census into python using the pygris package.

```
[14]: \[ \frac{\psi_script}{\psi_script} \text{ echo skipping # Comment this first line out if you wish to acquire_\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\tex{
```

skipping # Comment this first line out if you wish to acquire data directly from census

- [16]: Markdown(here(path["dmet"], "county_geom_2010_metadata.md"))
- Title: USA Counties Cartographic Boundaries
 - Abstract: The cartographic boundary files provided by the US census are simplified representations of the MAF/TIGER files. We use the 2010 boundary file because the census has not made such a file available for 2012 or 2011 and the original paper also used land area from 2010. This shapefile provides the geometries of counties and county-equivalents in the United States, with limited attribute information including land area.
 - Spatial Coverage: United States, excluding Puerto Rico
 - Spatial Resolution: County and county-equivalents
 - Spatial Reference System: EPSG:4269
 - Temporal Coverage: 2010
 - Temporal Resolution: One-time observations

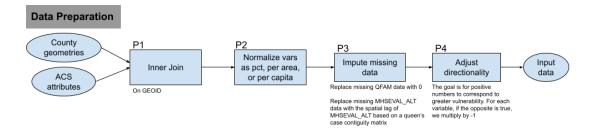
- Lineage: We use pygris to pull the data directly from the census into python.
- Distribution: This file is distributed via a census API. See more information on the census website and instructions for drawing census data directly into python on the pygris website.
- Constraints: Census data is available in the public domain
- Data Quality: 1:500,000 scale
- Variables: For each variable, enter the following information. If you have two or more variables per data source, you may want to present this information in table form (shown below)

Label	Alias	Definition	Type	Accuracy	Domain	Missing Data Value(s)	Missing Data Frequency
STATE	State- level FIPS code	State- level FIPS code	string		01 - 56	None	0
COUNTY	County- level FIPS code	County- level FIPS code	string		001 - 840	None	0
CENSUSAF	R.F.A.d area	land area in square miles	float64		1.999 - 145504.789	nan	0

The metadata file for this data is stored as county_geom_2010_metadata.md.

1.2.3 Data transformations

A workflow diagram for this section is displayed below.



We begin with step P1: joining the geometry and attribute data

```
[17]: # Step P1
# Join geometry and attribute data for reproduction
counties_shp['GEOID'] = counties_shp.STATE + counties_shp.COUNTY
counties = counties_shp.merge(counties_detailed, how = "inner", on = "GEOID")
# Also join Spielman's land area information to the rest of Spielman's data
```

```
# (to check that all data is accurate, not for purposes of analysis)
acs = acs.merge(dec_sup1, how = "inner", on='Geo_FIPS')
```

Planned deviation: Because we decided to acquire our data independently from Spielman et al, we need to check that our data is indeed the same as theirs.

To begin, we define a function that can check that the entries of two pandas DataFrames are equal.

```
[18]: # Define a function that can determine whether every entry in specified columns
       ⇔of two tables match
      def equiv(table1, sort1, column1, table2, sort2, column2):
          Tests two tables to see whether corresponding columns have equivalent_{\sqcup}
       \ominusentries.
          Parameters:
          table1 - the first table
          sort1 - the column in the first table to join by (str)
          column1 - the column(s) in the first table to test the values of (list of \Box
       \hookrightarrow str) (should list analogous columns for columns2)
          table2 - the second table
          sort2 - the column in the second table to join by (str)
          column2 - the column(s) in the second table to test the values of (list of \Box
       \hookrightarrow str)
          111
          # Sort tables
          table1 = table1.sort_values(by = sort1).reset_index()
          table2 = table2.sort_values(by = sort2).reset_index()
          # Rename column name in table2 to match that in table1
          for i in range(len(column1)):
               table2 = table2.rename(columns={column2[i]: column1[i]})
          # Select the columns to test equivalency of
          table1 = table1[column1]
          table2 = table2[column1]
          # Perform equivalency test
          test = table1.eq(table2)
          return test
```

Next, we round our area columns to the nearest integer, just for the purposes of comparing the two columns. These columns came from different sources and we know that they do not match up exactly.

```
[19]: # # Round area column
# acs['SE_TO2A_002_check'] = acs.SE_TO2A_002.round(0)
# counties['CENSUSAREA_check'] = counties.CENSUSAREA.round(0)
```

```
# Add the area variables to the lists of variables
acs_variables.append('CENSUSAREA')
spielman_acs_variables.append('SE_TO2A_002')
```

```
[20]: # Perform equivalency test
test = equiv(counties, "GEOID", acs_variables, acs, "Geo_FIPS",
spielman_acs_variables)
matching_cols = pd.DataFrame({"test": test.sum().eq(3143)}) # 3143 matches the
summber of rows
matching_cols.loc[~matching_cols.test] # Identify the columns that have some
size data discrepencies
```

[20]: test
B25077_001E False
CENSUSAREA False

The following variables have some discrepancy between the original and reproduction data: - $B25077\ 001E$ - CENSUSAREA

```
[21]: GEOID B25077_001E Geo_FIPS ACS12_5yr_B25077001
0 15005 NaN 15005 NaN
```

By inspection, we see that the one disagreement between B25077_001E and ACS12_5yr_B25077001 occurs because of a NaN value in an analogous location in each of the two datasets. Rather than revealing an issue in matching our data, this shows us that we will need to impute a missing value for one NaN in B25077_001E – median home value (see P3).

```
[22]:
            GEOID
                   CENSUSAREA Geo_FIPS
                                         SE_T02A_002
            01001
                       594.436
                                  01001
                                             594.4361
      1
            01005
                       884.876
                                  01005
                                             884.8763
      2
            01007
                       622.582
                                  01007
                                             622.5823
      3
                      644.776
                                             644.7759
            01009
                                  01009
      4
                                             622.8047
            01011
                      622.805
                                  01011
      2285 55137
                      626.153
                                  55137
                                             626.1533
      2286 55141
                      793.116
                                  55141
                                            793.1165
      2287 56013
                                  56013
                                           9183.8130
                     9183.814
      2288 56023
                     4076.129
                                  56023
                                           4076.1300
      2289 56037
                    10426.649
                                  56037
                                          10426.6500
      [2290 rows x 4 columns]
```

There are many disagreements between CENSUSAREA and SE_T02A_002, but they appear to be relatively minor differences. Let us evaluate how large those differences are.

Maximum difference: 0.010999999998603016 Average difference: 0.00031027379912322995

The largest discrepency between the two different sources of land area data is just over 0.01 square miles and the average difference (amongst those with a difference) is tiny. With such a minor difference between our data and theirs, for our purposes we will consider our data roughly the same as Spielman et al's.

```
[24]: # Step P2
      # Calculating the variables used in SoVI
      counties['MEDAGE_ACS'] = counties.B01002_001E
      counties['BLACK_ACS'] = counties.B03002_004E / (counties.B03002_001E)
      counties['QNATAM_ACS'] = counties.B03002_005E / (counties.B03002_001E)
      counties['QASIAN_ACS'] = counties.B03002_006E / (counties.B03002_001E)
      counties['QHISP ACS'] = counties.B03002 012E / (counties.B03002 001E)
      counties['QAGEDEP_ACS'] = (counties.B06001_002E + counties.B09020_001E) /
       ⇔(counties.B01003 001E)
      counties['QPUNIT_ACS'] = counties.B25008_001E / (counties.B25002_002E)
      counties['PRENTER_ACS'] = counties.B25003_003E / (counties.B25002_001E)
      counties['QNRRES_ACS'] = counties.B09020_021E / (counties.B01003_001E)
      counties['QFEMALE_ACS'] = counties.B01001_026E / (counties.B01003_001E)
      counties['QFHH_ACS'] = counties.B11001_006E / (counties.B11001_001E)
      counties['QUNOCCHU_ACS'] = counties.B25002_003E / (counties.B25002_001E)
      counties['QCVLUN'] = (counties.B23022_025E + counties.B23022_049E) / \
                      counties.B23022 001E
      counties['QPOVTY'] = (counties.B17021_002E) / counties.B17021_001E
      counties['QMOHO'] = (counties.B25024_010E) / counties.B25024_001E
      counties['QFEMLBR'] = (counties.C24010_038E) / counties.C24010_001E
      counties['QSSBEN'] = (counties.B19055_002E) / counties.B19055_001E
      counties['QFAM'] = (counties.B09002_002E) / counties.B09002_001E
      counties['QRICH200K'] = (counties.B19001_017E) / counties.B11001_001E
      counties['PERCAP ALT'] = counties.B19025 001E / (counties.B25008 001E)
      counties['QESL_ALT'] = (counties.B06007_005E + counties.B06007_008E) / \
                        counties.B06007 001E
      counties['QED12LES_ALT'] = (counties.B16010_002E) / counties.B16010_001E
      counties['QEXTRCT_ALT'] = (counties.C24050_002E) / counties.C24050_001E
      counties['QSERV_ALT'] = (counties.C24050_029E) / counties.C24050_001E
      counties['QNOAUTO_ALT'] = (counties.B08201_002E) / counties.B08201_001E
      counties['MDGRENT_ALT'] = counties.B25064_001E
      counties['MHSEVAL ALT'] = counties.B25077 001E
      counties['POPDENS'] = counties.B01003_001E / (counties.CENSUSAREA)
```

As noted before, B25077_001E is missing a data value. We now perform one final check to see if we need to impute anything else.

```
[25]: # Check for missing data
for i in counties.columns:
    x = counties[i].isnull().sum()
    if x > 0:
        print(i, "contains", x, "missing value(s).")

# Check for infinities
counties_num = counties.select_dtypes(include=['int64','float64'])
for i in counties_num.columns:
    xmin = counties_num[i].min()
```

```
xmax = counties_num[i].max()
if xmin == -np.inf:
    print(i, "contains a negative infinity")
elif xmax == np.inf:
    print(i, "contains a positive infinity")
```

```
LSAD contains 2 missing value(s).
B25077_001E contains 1 missing value(s).
QFAM contains 2 missing value(s).
MHSEVAL_ALT contains 1 missing value(s).
```

There are four variables with missing data. LSAD is not used in our analysis, so we may ignore this. B25077_001E and MHSEVAL_ALT are literally identical, so we will ignore B25077_001E and simply impute for MHSEVAL_ALT's one missing value. We also need to impute for QFAM's 2 missing values. We use the same imputation decisions that Spielman et al employ in their analysis.

Unplanned deviation: When imputing for MHSEVAL_ALT's missing data, we removed a fair amount of extraneous code that was filling in missing spatial lag data with original data for the county. This was unnecessary because we only needed to impute data for one county and that county had spatial lag data. Also note that Spielman et al's method for imputing data for MHSEVAL_ALT is a deviation from Cutter's original methodology, in which she imputed a 0 for any missing value. While this is a deviation from the original SoVI methodology, 0 is an unrealistic median home value, so Spielman et al's method for imputation seems like a reasonable improvement.

```
# Step P3
# Replace missing QFAM data with 0
counties.QFAM = counties.QFAM.replace([np.inf, -np.inf, np.nan], 0)

# Replace missing MHSEVAL_ALT data with its spatial lag

# Calculate spatial weights matrix
w = lps.weights.Queen.from_dataframe(counties)
w.transform = 'R'
# Calculate spatial lag
counties['MHSEVAL_ALT_LAG'] = lps.weights.lag_spatial(w, counties.MHSEVAL_ALT)
# Impute for the missing value
counties.MHSEVAL_ALT[np.isnan(counties['MHSEVAL_ALT'])] = ____
counties[["MHSEVAL_ALT_LAG"]] [pd.isna(counties['MHSEVAL_ALT'])]
```

```
('WARNING: ', 68, ' is an island (no neighbors)')
('WARNING: ', 546, ' is an island (no neighbors)')
('WARNING: ', 547, ' is an island (no neighbors)')
('WARNING: ', 549, ' is an island (no neighbors)')
('WARNING: ', 1226, ' is an island (no neighbors)')
('WARNING: ', 1876, ' is an island (no neighbors)')
('WARNING: ', 2976, ' is an island (no neighbors)')
```

/Users/liamsmith/opt/anaconda3/envs/RP1-Spielman-2020/lib/python3.9/site-packages/libpysal/weights/weights.py:172: UserWarning: The weights matrix is not fully connected:

```
There are 10 disconnected components.

There are 7 islands with ids: 68, 546, 547, 549, 1226, 1876, 2976.

warnings.warn(message)
```

Before adjusting directionality, let us check that all of our derived variables match all of Spielman et al's derived variables.

```
[28]: # Select only the relevant columns
      # Attribute name and expected influence on vulnerability
      input_names = [['MEDAGE_ACS', 'pos', 'person', 'Median Age'],
                     ['BLACK_ACS', 'pos', 'person', 'Pop African-American (%)'],
                     ['QNATAM_ACS', 'pos', 'person', 'Pop Native American (%)'],
                     ['QASIAN_ACS', 'pos', 'person', 'Pop Asian (%)'],
                     ['QHISP_ACS', 'pos', 'person', 'Pop Hispanic (%)'],
                     ['QAGEDEP_ACS', 'pos', 'person', 'Age Dependency (%)'],
                     ['QPUNIT_ACS', 'pos', 'person', 'Persons Per Housing Unit'],
                     ['PRENTER_ACS', 'pos', 'hu', 'Rental Housing (%)'],
                     ['QNRRES_ACS', 'pos', 'person', 'Nursing Home Residents (%)'],
                     ['QFEMALE_ACS', 'pos', 'person', 'Pop Female (%)'],
                     ['QFHH_ACS', 'pos', 'hu', 'Female-Headed Households (%)'],
                     ['QUNOCCHU_ACS', 'pos', 'hu', 'Vacant Housing (%)'],
                     ['PERCAP_ALT', 'neg', 'person', 'Per-Capita Income'],
                     ['QESL_ALT', 'pos', 'person', 'English as Second Language (%)'],
                     ['QCVLUN', 'pos', 'person', 'Unemployment (%)'],
                     ['QPOVTY', 'pos', 'person', 'Poverty (%)'],
                     ['QMOHO', 'pos', 'hu', 'Mobile Homes (%)'],
                     ['QED12LES_ALT', 'pos', 'person',
                         'Adults Completed <Grade 12 (%)'],
                     ['QFEMLBR', 'pos', 'person', 'Female Employment (%)'],
                     ['QEXTRCT_ALT', 'pos', 'person',
                         'Extractive Sector Employment (%)'],
                     ['QSERV_ALT', 'pos', 'person', 'Service Sector Employment (%)'],
                     ['QSSBEN', 'pos', 'hu', 'Social Security Income (%)'],
                     ['QNOAUTO_ALT', 'pos', 'hu', 'No Automobile (%)'],
                     ['QFAM', 'neg', 'person', 'Children in Married Families (%)'],
                     ['QRICH200K', 'neg', 'hu', 'Annual Income >$200K (%)'],
                     ['MDGRENT_ALT', 'neg', 'hu', 'Median Rent'],
                     ['MHSEVAL_ALT', 'neg', 'hu', 'Median Home Value'],
                     ['POPDENS', 'pos', 'person', 'Population Density']]
```

```
# Get attribute names
      attr_names1 = [j[0] for j in input_names] + ['GEOID']
      attr_names2 = [j[0] for j in input_names] + ['Geo_FIPS']
      # Select only the columns needed to compute SoVI
      counties = counties[attr_names1]
      US_All = US_All[attr_names2]
      counties["GEOID"] = "g" + counties["GEOID"]
      counties['stateID'] = counties.GEOID.str.slice(0, 3, 1)
      attr_names1.remove('GEOID')
      counties = counties.set_index(counties["GEOID"]).sort_index()
      US_All['stateID'] = US_All.Geo_FIPS.str.slice(0, 3, 1)
      attr_names2.remove('Geo_FIPS')
      US_All = US_All.set_index(US_All["Geo_FIPS"]).sort_index()
[29]: counties.eq(US_All).sum()
[29]: BLACK_ACS
                      3143
                         0
      GEOID
      Geo_FIPS
                         0
      MDGRENT_ALT
                      3143
      MEDAGE_ACS
                      3143
                      3143
      MHSEVAL_ALT
      PERCAP_ALT
                      3143
      POPDENS
                       853
                      3143
      PRENTER_ACS
      QAGEDEP_ACS
                      3143
      QASIAN ACS
                      3143
      QCVLUN
                      3143
      QED12LES_ALT
                      3143
      QESL_ALT
                      3143
      QEXTRCT_ALT
                      3143
      QFAM
                      3143
                      3143
      QFEMALE_ACS
      QFEMLBR
                      3143
      QFHH_ACS
                      3143
      QHISP_ACS
                      3143
      QMOHO
                      3143
      QNATAM_ACS
                      3143
      QNOAUTO_ALT
                      3143
      QNRRES_ACS
                      3143
```

QPOVTY

QPUNIT ACS

QRICH200K

3143

3143

3143

```
QSERV_ALT 3143
QSSBEN 3143
QUNOCCHU_ACS 3143
stateID 3143
dtype: int64
```

Therre are 3143 observations in the dataset, so it appears that all variables match up perfectly except POPDENS. POPDENS is the one variable that was derived from the land area, so this was to be expected. Let us confirm that the differences between the two datasets are minor.

```
[30]: diff = (abs(counties[["POPDENS"]] - US_All[["POPDENS"]]))
print("Maximum difference:", diff.max()[0], "\nAverage difference:", diff.

mean()[0])
```

Maximum difference: 0.949787960271351 Average difference: 0.0015009727346509663

With a maximum difference less than 1 and an average difference less than 0.01, our data is sufficiently close to Spielman et al's for our purposes.

Now we proceed to step P4, switching the directionality of variables as needed in order to ensure that higher values of a variable are associated with higher levels of vulnerability.

```
[31]: # Step P4

# Flip signs as needed to ensure that each variable contributes as expected to

the final Sovi

for name, sign, sample, hrname in input_names:
    if sign == 'neg':
        counties[name] = -counties[name].values
        print("Inverting variable:", name)

elif sign == 'pos':
    pass
else:
    print("problem in flipping signs")
    raise
```

Inverting variable: PERCAP_ALT Inverting variable: QFAM Inverting variable: QRICH200K Inverting variable: MDGRENT_ALT Inverting variable: MHSEVAL_ALT

A final step of data transformation will be performed at the beginning of the SoVI model analysis. Each demographic variable will be normalized by calculating its z-score.

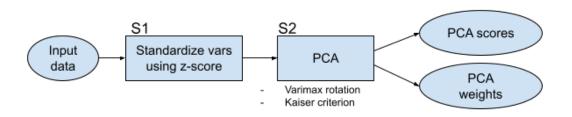
1.2.4 Analysis

Principal Component Analysis Spielman et al constructed a class to conduct SPSS-style PCA with varimax rotation in python and validated their procedure against Cutter et al's SPSS workflow used to calculate SoVI. Below I include a workflow diagram that shows, without too much detail,

the main operations and important outputs of their SPSS PCA class. After that, I have included their relevant code.

PCA Workflow

We will later refer to this workflow as one function, SPSS PCA.



[32]: class SPSS_PCA:

A class that integrates most (all?) of the assumptions SPSS imbeds in_{\sqcup} $\hookrightarrow their$

implimnetation of principal components analysis (PCA), which can be found in thier GUI under Analyze > Dimension Reduction > Factor. This class is not intended to be a full blown recreation of the SPSS Factor Analysis GUI, □

 $\hookrightarrow but$

it does replicate (possibly) the most common use cases. Note that this, \Box $\hookrightarrow class$

will not produce exactly the same results as SPSS, probably due to,, \hookrightarrow differences

in how eigenvectors/eigenvalues and/or singular values are computed. ⊔ *→However*.

this class does seem to get all the signs to match, which is not really $_{\!\sqcup}$ $\neg necessary$

but kinda nice. Most of the approach came from the official $SPSS_{\sqcup}$ \hookrightarrow documentation.

References

ftp://public.dhe.ibm.com/software/analytics/spss/documentation/ -statistics/20.0/en/client/Manuals/IBM_SPSS_Statistics_Algorithms.pdf

http://spssx-discussion.1045642.n5.nabble.com/

 \rightarrow Interpretation-of-PCA-td1074350.html

http://mdp-toolkit.sourceforge.net/api/mdp.nodes.WhiteningNode-class.

 $\hookrightarrow html$

https://qithub.com/mdp-toolkit/mdp-toolkit/blob/master/mdp/nodes/ $\neg pca_nodes.py$

```
Parameters
       inputs: numpy array
                         n \times k numpy array; n observations and k variables on
\ominus each observation
       reduce: boolean (default=False)
                         If True, then use eigenvalues to determine which
⇒ factors to keep; all
                         results will be based on just these factors. If False
\hookrightarrowuse all factors.
       min_eig: float (default=1.0)
                         If reduce=True, then keep all factors with anu
⇔eigenvalue greater than
                         min_eiq. SPSS default is 1.0. If reduce=False, then__
\negmin_eig is ignored.
       varimax: boolean (default=False)
                         If True, then apply a varimax rotation to the results.
\hookrightarrow If False, then
                        return the unrotated results only.
       Attributes
       z_inputs:
                        numpy array
                                 z-scores of the input array.
       comp_mat:
                         numpy array
                                 Component matrix (a.k.a, "loadings").
       scores:
                                numpy array
                                 New uncorrelated vectors associated with each
\ominus observation.
       eigenvals_all:
                               numpy array
                                 Eigenvalues associated with each factor.
                          numpy array
       eigenvals:
                                 Subset of eigenvalues_all reflecting only those_
⇔that meet the
                                 criterion defined by parameters reduce and \Box
\hookrightarrow min_eiq.
       weights:
                   numpy array
                                 Values applied to the input data (after_
\hookrightarrow z-scores) to get the PCA
                                 scores. "Component score coefficient matrix" in
\hookrightarrow SPSS or
                                 "projection matrix" in the MDP library.
                                numpy array
       comms:
                                 Communalities
       sum sq load: numpy array
                                  Sum of squared loadings.
```

```
comp_mat_rot: numpy array or None
                                  Component matrix after rotation. Ordered from ____
\hookrightarrow highest to lowest
                                  variance explained based on sum_sq_load_rot.__
→None if varimax=False.
       scores_rot:
                        numpy array or None
                                Uncorrelated vectors associated with each\sqcup
\hookrightarrow observation, after
                                rotation. None if varimax=False.
       weights_rot: numpy array or None
                                Rotated values applied to the input data (after_
\ominus z-scores) to get
                                               scores. None if varimax=False.
       sum_sq_load_rot: numpy array or None
                                 Sum of squared loadings for rotated results.
\hookrightarrow None if
                                 varimax=False.
       111
       def __init__(self, inputs, reduce=False, min_eig=1.0, varimax=False):
       # Step S1
               z_inputs = ZSCORE(inputs) # seems necessary for SPSS__
→"correlation matrix" setting (their default)
       # The rest is step S2
               # run base SPSS-style PCA to get all eigenvalues
               pca node = MDP.nodes.WhiteningNode() # settings for the PCA
               scores = pca_node.execute(z_inputs) # base run PCA
               eigenvalues_all = pca_node.d # rename PCA results
               # run SPSS-style PCA based on user settings
               pca_node = MDP.nodes.WhiteningNode(reduce=reduce,__
→var_abs=min_eig) # settings for the PCA
               scores = pca_node.execute(z_inputs) # run PCA (these have_
\hookrightarrow mean=0, std dev=1)
               weights = pca_node.v # rename PCA results (these might be a_
→ transformation of the eigenvectors)
               eigenvalues = pca_node.d # rename PCA results
               component_matrix = weights * eigenvalues # compute the loadings
               component_matrix = self._reflect(component_matrix)
⇔signs to match SPSS
               communalities = (component_matrix**2).sum(1) # compute the__
\hookrightarrow communalities
               sum_sq_loadings = (component_matrix**2).sum(0) # note that this_
⇔is the same as eigenvalues
```

```
weights reflected = component matrix/eigenvalues # qet signs_
→to match SPSS
              scores_reflected = np.dot(z_inputs, weights_reflected) # note_
⇒that abs(scores)=abs(scores reflected)
              if varimax:
                       # SPSS-style varimax rotation prep
                      c_normalizer = 1. / MDP.numx.sqrt(communalities) #__
→used to normalize inputs to varimax
                       c_normalizer.shape = (component_matrix.shape[0],1) #__
⇔reshape to vectorize normalization
                      cm_normalized = c_normalizer * component_matrix #__
\rightarrownormalize component matrix for varimax
                       # varimax rotation
                       cm_normalized_varimax = self._varimax(cm_normalized) #__
⇔run varimax
                      c_normalizer2 = MDP.numx.sqrt(communalities) # used to_
→denormalize varimax output
                      c_normalizer2.shape = (component_matrix.shape[0],1) #__
⇔reshape to vectorize denormalization
                      cm_varimax = c_normalizer2 * cm_normalized_varimax #__
\rightarrow denormalize varimax output
                       # reorder varimax component matrix
                      sorter = (cm_varimax**2).sum(0) # base the ordering on_
⇒sum of squared loadings
                      sorter = zip(sorter.tolist(), range(sorter.shape[0])) __
→# add index to denote current order
                      sorter = sorted(sorter, key=itemgetter(0),___
→reverse=True) # sort from largest to smallest
                       sum_sq_loadings_varimax, reorderer = zip(*sorter) #__
→unzip the sorted list
                      sum_sq_loadings_varimax = np.
→array(sum_sq_loadings_varimax) # convert to array
                       cm_varimax = cm_varimax[:,reorderer] # reorder__
\hookrightarrow component matrix
                       # varimax scores
                      cm_varimax_reflected = self._reflect(cm_varimax) # get_
⇔signs to match SPSS
                      varimax_weights = np.dot(cm_varimax_reflected,
                                                        np.linalg.inv(np.

dot(cm_varimax_reflected.T,
```

```
scores_varimax = np.dot(z_inputs, varimax_weights)
               else:
                       comp_mat_rot = None
                       scores_rot = None
                       weights_rot = None
               # assign output variables
               self.z_inputs = z_inputs
               self.scores = scores reflected
               self.comp_mat = component_matrix
               self.eigenvals_all = eigenvalues_all
               self.eigenvals = eigenvalues
               self.weights = weights_reflected
               self.comms = communalities
               self.sum_sq_load = sum_sq_loadings
               self.comp_mat_rot = cm_varimax_reflected
               self.scores_rot = scores_varimax # PCA scores output
               self.weights_rot = varimax_weights # PCA weights output
               self.sum_sq_load_rot = sum_sq_loadings_varimax
       def _reflect(self, cm):
               # reflect factors with negative sums; SPSS default
               cm = copy.deepcopy(cm)
               reflector = cm.sum(0)
               for column, measure in enumerate(reflector):
                       if measure < 0:</pre>
                                cm[:,column] = -cm[:,column]
               return cm
       def _varimax(self, Phi, gamma = 1.0, q = 100, tol = 1e-6):
               # downloaded from http://en.wikipedia.org/wiki/
→ Talk%3aVarimax_rotation
               # also here http://stackoverflow.com/questions/17628589/
\hookrightarrow perform-varimax-rotation-in-python-using-numpy
               p,k = Phi.shape
               R = np.eye(k)
               d=0
               for i in range(q):
                       d_old = d
                       Lambda = np.dot(Phi, R)
                       u,s,vh = np.linalg.svd(np.dot(Phi.T,np.
→asarray(Lambda)**3 - (gamma/p) *
                                                        np.dot(Lambda, np.
→diag(np.diag(np.dot(Lambda.T,Lambda))))))
                       R = np.dot(u,vh)
                       d = np.sum(s)
                       if d_old!=0 and d/d_old < 1 + tol:
```

```
break
return np.dot(Phi, R)
```

Basic set-up for storing results

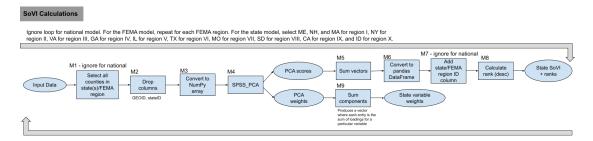
```
[33]: # Build FEMA subRegions Dict values= state ID's
      FEMA subs = dict()
      FEMA\_subs['FEMA\_1'] = ['g23g33g25', 'g50', 'g09', 'g44']
      FEMA_subs['FEMA_2'] = ['g36', 'g34']
      FEMA_subs['FEMA_3'] = ['g42', 'g10', 'g11', 'g24', 'g51', 'g54']
      FEMA_subs['FEMA_4'] = ['g21', 'g47', 'g37', 'g28', 'g01', 'g13', 'g45', 'g12']
      FEMA_subs['FEMA_5'] = ['g27', 'g55', 'g26', 'g17', 'g18', 'g39']
      FEMA_subs['FEMA_6'] = ['g35', 'g48', 'g40', 'g05', 'g22']
      FEMA_subs['FEMA_7'] = ['g31', 'g19', 'g20', 'g29']
      FEMA_subs['FEMA_8'] = ['g30', 'g38', 'g56', 'g46', 'g49', 'g08']
      FEMA_subs['FEMA_9'] = ['g06', 'g32', 'g04']
      FEMA_subs['FEMA_10'] = ['g53', 'g41', 'g16']
      # DataFrames to hold US, FEMA region, and state level results
      # Dict to hold variable loadings
      # key will be [USA, Fema_region, stateid] depending on level of analysis
      varContrib = {}
      # National Score
      US_Sovi_Score = pd.DataFrame(index=counties.GEOID,
                                   columns=['sovi', 'rank'])
      # In the FEMA_Region_Sovi_Score data frame ranks are BY FEMA REGION.
      # The data frame holds both the SOVI score and the county rank
      # This means that there should be 10 counties with rank 1 (one for each
      # FEMA Region)
      FEMA_Region_Sovi_Score = pd.DataFrame(index=counties.GEOID,
                                            columns=['sovi', 'rank', 'fema region'])
      # Create New England conglomerate of states
      # These are the FIPS codes for the states with the letter "q" appended
      counties.loc[counties.stateID.isin(['g23', 'g33', 'g25']), 'stateID'] = counties.loc[counties.stateID.isin(['g23', 'g33', 'g25']), 'stateID']

→ 'g23g33g25'

      # These are the states in the state level analysis
      stateList = ['g23g33g25', 'g36', 'g51', 'g13',
                   'g17', 'g48', 'g29', 'g46', 'g06', 'g16']
      # In the State_Sovi_Score data frame ranks are BY STATE.
      # The data frame holds both the SOVI score and the county rank
```

```
# This means that there should be 10 counties with rank 1 (one for each
# state in stateList)
State_Sovi_Score = pd.DataFrame(
   index=counties.index[counties.stateID.isin(stateList)],
   columns=['sovi', 'rank', 'state_id'])
```

Calculating SoVI At this stage, we seek to calculate the SoVI ranks and variable weightings on the national, FEMA region, and state-level spatial extents. Below is a workflow for calculating SoVI, followed by the code for each spatial extent.



```
# Compute National SoVI
     ######################
     # compute SoVI
     # Step M2
     inputData = counties.drop(['GEOID', 'stateID'], axis=1, inplace=False)
     # Step M3
     inputData array = inputData.values  # Convert DataFrame to NumPy array
     # Step M4
     pca = SPSS_PCA(inputData_array, reduce=True, varimax=True)
     # Step M5
     sovi_actual_us = pca.scores_rot.sum(1)
     # Step M6
     sovi_actual_us = pd.DataFrame(
         sovi actual us, index=counties.GEOID, columns=['sovi'])
     # Step M8
     sovi_actual_us['rank'] = sovi_actual_us.rank(
         method='average', ascending=False)
     US_Sovi_Score.update(sovi_actual_us)
     # Step M9
     attrib_contribution_us = pca.weights_rot.sum(1)
```

```
varContrib['USA'] = zip(attr_names1, attrib_contribution_us.tolist()) #__
Generate dictionary for all net loadings by variable for US

# Quick check of ranks: max should equal number of counties in US

try:
    US_Sovi_Score['rank'].max() == len(counties)

except:
    print("error in ranking check")
    raise

# cleanup
del inputData
# del inputData_norm
del sovi_actual_us
del attrib_contribution_us
```

```
# Compute FEMA Region SoVI
     #############################
     for i in FEMA_subs:
         # Step M1: Subset FEMA subregion
         FEMARegionData = counties[counties['stateID'].isin(FEMA_subs[i])]
         # Step M2
         inputData = FEMARegionData.drop(
             ['GEOID', 'stateID'], axis=1, inplace=False)
         # Step M3
         inputData_array = inputData.values # Convert DataFrame to NumPy array
         pca = SPSS_PCA(inputData_array, reduce=True, varimax=True)
         # Step M5
         sovi_actual_fema = pca.scores_rot.sum(1)
         # Step M6
         sovi_actual_fema = pd.DataFrame(
             sovi_actual_fema, index=FEMARegionData.index, columns=['sovi'])
         # Step M7
         sovi_actual_fema['fema_region'] = i
         # Step M8
         sovi_actual_fema['rank'] = sovi_actual_fema['sovi'].rank(
             method='average', ascending=False)
```

```
FEMA_Region_Sovi_Score.update(sovi_actual_fema)

# Step M9
attrib_contribution_fema = pca.weights_rot.sum(1)
varContrib[i] = zip(attr_names1, attrib_contribution_fema.tolist())

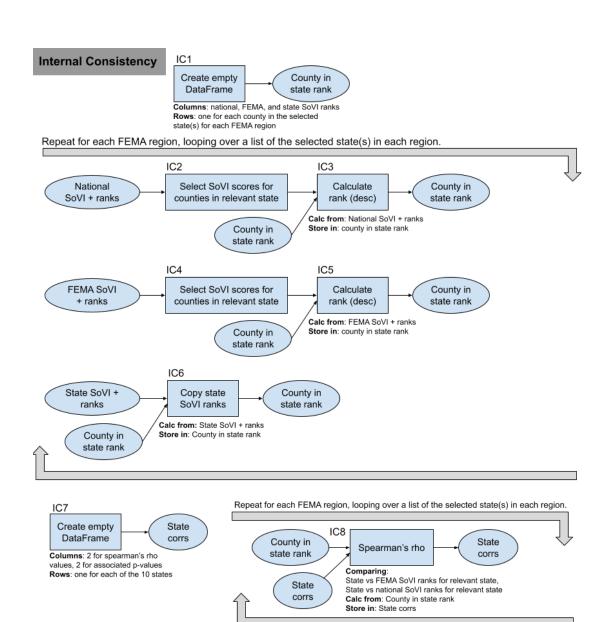
# cleanup
del FEMARegionData
del inputData
del sovi_actual_fema
del attrib_contribution_fema
```

```
# Compute State Level SoVI
     #############################
     for st in stateList:
         # Step M1: Subset FEMA subregion
         stateData = counties[counties.stateID == st]
         # Step M2
         inputData = stateData.drop(['GEOID', 'stateID'], axis=1, inplace=False)
         # Step M3
         inputData_array = inputData.values # Convert DataFrame to NumPy array
         # Step M4
         pca = SPSS_PCA(inputData_array, reduce=True, varimax=True)
         # Step M5
         sovi_actual = pca.scores_rot.sum(1)
         # Step M6
         sovi_actual = pd.DataFrame(
             sovi_actual, index=stateData.index, columns=['sovi'])
         # Step M7
         sovi_actual['state_id'] = st
         # Step M8
         sovi_actual['rank'] = sovi_actual['sovi'].rank(
             method='average', ascending=False)
         State_Sovi_Score.update(sovi_actual)
         # Step M9
         attrib_contribution = pca.weights_rot.sum(1)
         varContrib[st] = zip(attr_names1, attrib_contribution.tolist())
```

```
# cleanup
del stateData
del inputData
del sovi_actual
del attrib_contribution
```

Internal consistency analysis Now that we have generated the SoVI scores for the 21 different models, we turn to our analysis of internal consistency.

This analysis checks for consistent SoVI rankings of counties in a region of interest (a state or group of small states) through three versions of a SoVI model, each using a different geographic extent for input data. Those extents are: 1) all counties in the country, 2) all the counties in a FEMA region, and 3) all counties in a single state or group of small states. The SoVI scores for the counties in the region of interest are selected and ranked. The agreement between the three sets of rankings is calculated using the Spearman's Rho rank correlation coefficient. If the model is internally consistent, one could expect a nearly perfect positive rank correlation close to 1, implying that counties have similar levels of social vulnerability vis a vis one another in the region of interest, regardless of how much extraneous information from other counties in the FEMA region or from the whole United States has been included in the SoVI model.



```
for st in stateList:
    if st == 'g23g33g25':
       # Step IC2: Select the index and SoVI scores from national model for
 →Maine, New Hampshire, and Massachusetts
        st_cty_scores1 = US_Sovi_Score.loc[['g23' in s for s in US_Sovi_Score.

index], 'sovi']

        st_cty_scores2 = US_Sovi_Score.loc[['g33' in s for s in US_Sovi_Score.
 →index], 'sovi']
        st_cty_scores3 = US_Sovi_Score.loc[['g25' in s for s in US_Sovi_Score.

index], 'sovi']

        st_cty_scores = pd.concat([st_cty_scores1, st_cty_scores2,__

st_cty_scores3])
        # Step IC3: Re-rank the national SoVI scores but just for the counties \Box
 → in the relevant states
        county_in_state_rank.loc[st_cty_scores.index, 'us_sovi_rank'] =__

st_cty_scores.rank(method='average', ascending=False)
        # Step IC4: Select the index and SoVI scores from FEMA model for Maine, ...
 →New Hampshire, and Massachusetts
        st_cty_scores1 = FEMA_Region_Sovi_Score.loc[['g23' in s for s in_
 →FEMA_Region_Sovi_Score.index], 'sovi']
        st_cty_scores2 = FEMA_Region_Sovi_Score.loc[['g33' in s for s in_
 →FEMA_Region_Sovi_Score.index], 'sovi']
        st_cty_scores3 = FEMA_Region_Sovi_Score.loc[['g25' in s for s in_
 →FEMA_Region_Sovi_Score.index], 'sovi']
        st_cty_scores = pd.concat([st_cty_scores1, st_cty_scores2,__

st_cty_scores3])
        # Step IC5: Re-rank the FEMA SoVI scores but just for the counties in
 \hookrightarrow the relevant states
        county_in_state rank.loc[st_cty_scores.index, 'fema_region_sovi_rank']__

    st_cty_scores.rank(method='average', ascending=False)

        # Step IC6: Pull the state-only SoVI ranks into the same dataframe as_{f \sqcup}
 ⇒the other data
        county_in_state_rank.loc[st_cty_scores.index, 'state_sovi_rank'] = ___
 State_Sovi_Score.loc[State_Sovi_Score['state_id'] == 'g23g33g25', 'rank']
    else:
        # Step\ IC2: select\ the\ index\ and\ SoVI\ scores\ from\ national\ model\ for_{f l}
 → the relevant state
        st_cty_scores = US_Sovi_Score.loc[[st in s for s in US_Sovi_Score.

index], 'sovi']
```

```
# Step IC3: Re-rank the national SoVI scores but just for the counties \Box
       → in the relevant state
             county_in_state_rank.loc[st_cty_scores.index, 'us_sovi_rank'] =_
       ⇔st_cty_scores.rank(method='average', ascending=False)
             # Step IC4: Select the index and SoVI scores from FEMA model for the
       ⇔relevant state
             st_cty_scores = FEMA_Region_Sovi_Score.loc[[st in s for s in_
       →FEMA_Region_Sovi_Score.index], 'sovi']
             # Step IC5: Re-rank the FEMA SoVI scores but just for the counties in
       → the relevant state
             county_in_state_rank.loc[st_cty_scores.index, 'fema_region_sovi_rank']_u
       st_cty_scores.rank(method='average', ascending=False)
             # Step IC6: Pull the state-only SoVI ranks into the same dataframe as_{\sqcup}
       ⇔the other data
             county_in_state_rank.loc[st_cty_scores.index, 'state_sovi_rank'] = __
       State Sovi Score.loc[State Sovi Score['state id'] == st, 'rank']
# CORRELATIONS
     #######################
     # Step IC 7: Create an empty DataFrame to hold Spearman test results
     state_corrs = pd.DataFrame(index = stateList, columns = ['spearman_r_st_fema',_
      for st in stateList:
       if st == 'g23g33g25':
         # Step IC8: Calculate spearman correlation between state and FEMA, state
      \rightarrow and national
         multi_state_data_tmp1 = county_in_state_rank.loc[['g23' in s for s in_
       →county_in_state_rank.index], ]
         multi_state_data_tmp2 = county_in_state_rank.loc[['g25' in s for s in_u
      ⇒county_in_state_rank.index], ]
```

state_corrs.loc['g23g33g25',] = [st_fema_spearman[0], st_fema_spearman[1],_

multi_state_data_tmp3 = county_in_state_rank.loc[['g33' in s for s in_

st_fema_spearman = spearmanr(multi_state_data_tmp[['state_sovi_rank',_

st_us_spearman = spearmanr(multi_state_data_tmp[['state_sovi_rank',_

multi_state_data_tmp = pd.concat([multi_state_data_tmp1,__

multi_state_data_tmp2, multi_state_data_tmp3])

¬st_us_spearman[0], st_us_spearman[1]]

→county_in_state_rank.index],]

'us_sovi_rank']])

```
else:

# Step IC8: Calculate spearman correlation between state and FEMA, state_
and national

st_fema_spearman = spearmanr(county_in_state_rank.loc[[st in s for s in_
county_in_state_rank.index], ['state_sovi_rank', 'fema_region_sovi_rank']])

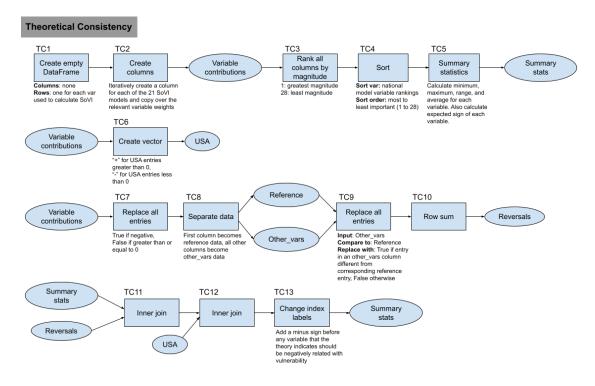
st_us_spearman = spearmanr(county_in_state_rank.loc[[st in s for s in_
county_in_state_rank.index], ['state_sovi_rank', 'us_sovi_rank']])

state_corrs.loc[st,] = [st_fema_spearman[0], st_fema_spearman[1],__
st_us_spearman[0], st_us_spearman[1]]
```

Theoretical consistency analysis Finally, we investigate the questions surrounding theoretical consistency.

This analysis checks for consistent signs and ranks of variables across the same 21 models that were used in the internal consistency analysis. To evaluate the signs and ranks of variables, we sum all components together, producing one vector for each model containing the net effect of each variable on the SoVI score. Theoretical consistency is indicated by little variation amongst all models in the signs and magnitudes of variable weights. Theoretical inconsistency is indicated by substantial variation in the signs and weights of variables and by disagreement between a variable's theoretical influence and modeled influence on vulnerability.

Unplanned deviation: we were unable to find all of the code for this part the analysis, so we wrote much of this code ourselves.



[39]: # Step TC1: Create a DataFrame to hold variable contributions values variable_contributions = pd.DataFrame(index=attr_names1)

```
# Step TC2: Add variable contributions values to DataFrame
for area in varContrib.keys():
    variable_contributions[area] = [x for i, x in varContrib[area]]
# Step TC3: For all SoVI models, rank variables from the greatest to the least \Box
 \hookrightarrow magnitudes
rankContrib = abs(variable_contributions).apply(rankdata, axis=0,__
 →method='average')
rankContrib = (28-rankContrib) + 1
# Step TC4: Sort variable rankings according to national model's most to least
 \hookrightarrow important
rankContrib = rankContrib.sort_values("USA", ascending = True).reset_index()
rankContrib.index = rankContrib["index"]
rankContrib = rankContrib.drop(columns = ["index"])
# Step TC5: Calculate summary statistics for each variable
summary_stats = pd.DataFrame( {"Min": rankContrib.min(axis = 1).round(),
                                "Max": rankContrib.max(axis = 1).round(),
                                "Range": rankContrib.max(axis = 1) - rankContrib.
 \rightarrowmin(axis = 1).round(),
                                "Average": rankContrib.mean(axis = 1).round(2)
                               } )
# Step TC6: determine signs of USA model
def pos_neg(x):
    if x > 0:
        return "+"
    else:
        return "-"
usa = variable_contributions["USA"].apply(pos_neg)
# Step TC7: Determine all positive/negatives
reversals_adj = variable_contributions < 0</pre>
# Step TC8: Separate data
reference = reversals_adj[["USA"]]
other_vars = reversals_adj.drop(columns = ["USA"])
# Step TC9: Determine all reversals from expected sign
for i in range(len(other_vars.columns)):
    other_vars.iloc[:, i] = reversals_adj["USA"].eq(other_vars.iloc[:, i]).
 ⇔eq(False)
# Step TC10: calculate reversals
reversal_sum = pd.DataFrame( {"Reversals": other_vars.sum(axis = 1)} )
```

```
# Step TC11: Join data
summary_stats = summary_stats.merge(reversal_sum, left_index = True,__
 →right_index = True)
# Step TC12: Join data
summary stats = summary stats.merge(usa, left index = True, right index = True)
# Step TC13: Change index labels to reflect any changes prior to SoVI
 \hookrightarrow calculation
for name, sign, sample, hrname in input_names:
    if sign == 'neg':
        summary stats = summary stats.rename(index={name: '- '+ name})
    else:
        pass
# Table aesthetics edits
summary_stats = summary_stats.rename(columns={"USA": "National Model"})
summary_stats = summary_stats.loc[:,['National Model', 'Reversals', 'Min',_
 →'Average', 'Max', 'Range']]
```

We made a different choice than Spielman et al in this table. Since we adjusted all variables such that larger values are theoretically associated with a higher degree of vulnerability before calculating SoVI, we would expect all outputs to be positive. In Spielman et al's "expected contribution" column, some signs were negative – they recorded the directionality we would expect of the variables if they had made no adjustments before calculating SoVI. This leads to a misleading table because their "original contribution" column displays the signs of the model output including prior adjustments to directionality, but the "expected contribution" column displays the signs if the model had not adjusted directionality. To make their "expected contribution" column consistent with their "original contribution" column, they would need all of the signs to be positive in the "expected contribution" column. We choose to simply not include an "expected contribution" column since there would be no variation within it anyway. Additionally, we add a negative sign in front of any variables that we changed the directionality of for the sake of clarity.

Save analysis results

```
# The data frame holds both the SOVI score and the county rank
# This means that there should be 10 counties with rank 1 (one for each
# state in stateList)
State_Sovi_Score.to_csv( here(path["ddpub"], 'State_Sovi_Score.csv') )

# County rank within state for US, state, and fema_region sovis
county_in_state_rank.to_csv( here(path["ddpub"], 'County_in_State_Rank.csv') )

# Variable contributions for sovis at all geographic extents
variable_contributions.to_csv( here(path["ddpub"], 'variable_contributions.

-csv') )

# Correlation of ranks
state_corrs.to_csv( here(path["ddpub"], 'state_fema_us_rank_correlations.csv') )
```

1.3 Results

1.3.1 Rpr-H1

First, we tested RPr-H1, that reproduced SoVI model scores for each county are not identical to the original study SoVI model scores for each county for each of the 21 SoVI models.

We define a function, check_it to check equivalency of the original output files to our reproduced output files.

```
[41]: def check it(file, rounder = False):
          Given a file name, this function finds the corresponding file provided by \Box
       \hookrightarrowSpielman et al and the file produced
          by our code and returns the number of matches for each column.
          111
          global rpl
          global og
          global test
          rpl = pd.read_csv( here(path["ddpub"], file) )
          og = pd.read_csv( here(path["og_out"], file) )
          og = og.rename(columns = {"Geo_FIPS": "GEOID"})
          if "sovi" in rpl.columns:
              rpl["sovi"] = rpl["sovi"].round(2)
              og["sovi"] = og["sovi"].round(2)
          if "Unnamed: 0" in rpl.columns:
              rpl.index = rpl["Unnamed: 0"]
              rpl = rpl.drop(columns = ["Unnamed: 0"])
          if "Unnamed: 0" in og.columns:
```

```
og.index = og["Unnamed: 0"]
  og = og.drop(columns = ["Unnamed: 0"])

if rounder != False:
    og = og.round(rounder)
    rpl = rpl.round(rounder)

test = rpl.eq(og)

if test.sum().eq(len(rpl)).sum() == len(test.sum()):
    return print("All values match!")
else:
    return test.sum()
```

```
US SoVI Scores & Rankings
[42]: check_it('US_Sovi_Score.csv')
[42]: GEOID
              3143
      sovi
              3143
     rank
              3141
      dtype: int64
[43]: merged = og.merge(rpl, how = "inner", on = "GEOID")
      merged.loc[~test["rank"]]
[43]:
            GEOID sovi_x rank_x sovi_y rank_y
                    -4.53 2984.0
      1150
           g22075
                                    -4.53
                                           2983.0
     3120 g56001
                    -4.53 2983.0
                                    -4.53 2984.0
```

We have identically reproduced national SoVI scores (rounded to 2 decimal points) for all 3143 counties compared to the original study, but two county ranks are different, probably due to the small differences between our area column and theirs.

FEMA Region SoVI Scores & Rankings

Our check it function found potential differences in 34 counties. The following table shows the SoVI scores and ranks for those counties.

```
[45]: merged = og.merge(rpl, how = "inner", on = "GEOID")
merged.loc[~test["rank"] | ~test["sovi"] | ~test["fema_region"]]#.head()
```

[45]:	GEOID	sovi_x	rank x	fema_region_x	sovi_y	rank y	fema_region_y
67	g02013	- NaN	NaN	- C - NaN	NaN	NaN	- C -V NaN
68	g02016	NaN	NaN	NaN	NaN	NaN	NaN
69	g02020	NaN	NaN	NaN	NaN	NaN	NaN
70	g02050	NaN	NaN	NaN	NaN	NaN	NaN
71	g02060	NaN	NaN	NaN	NaN	NaN	NaN
72	g02068	NaN	NaN	NaN	NaN	NaN	NaN
73	g02070	NaN	NaN	NaN	NaN	NaN	NaN
74	g02090	NaN	NaN	NaN	NaN	NaN	NaN
75	g02100	NaN	NaN	NaN	NaN	NaN	NaN
76	g02105	NaN	NaN	NaN	NaN	NaN	NaN
77	g02110	NaN	NaN	NaN	NaN	NaN	NaN
78	g02122	NaN	NaN	NaN	NaN	NaN	NaN
79	g02130	NaN	NaN	NaN	NaN	NaN	NaN
80	g02150	NaN	NaN	NaN	NaN	NaN	NaN
81	g02164	NaN	NaN	NaN	NaN	NaN	NaN
82	g02170	NaN	NaN	NaN	NaN	NaN	NaN
83	g02180	NaN	NaN	NaN	NaN	NaN	NaN
84	g02185	NaN	NaN	NaN	NaN	NaN	NaN
85	g02188	NaN	NaN	NaN	NaN	NaN	NaN
86	g02195	NaN	NaN	NaN	NaN	NaN	NaN
87	g02198	NaN	NaN	NaN	NaN	NaN	NaN
88	g02220	NaN	NaN	NaN	NaN	NaN	NaN
89	g02230	NaN	NaN	NaN	NaN	NaN	NaN
90	g02240	NaN	NaN	NaN	NaN	NaN	NaN
91	g02261	NaN	NaN	NaN	NaN	NaN	NaN
92	g02270	NaN	NaN	NaN	NaN	NaN	NaN
93	g02275	NaN	NaN	NaN	NaN	NaN	NaN
94	g02282	NaN	NaN	NaN	NaN	NaN	NaN
95	g02290	NaN	NaN	NaN	NaN	NaN	NaN
546	g15001	NaN	NaN	NaN	NaN	NaN	NaN
547	g15003	NaN	NaN	NaN	NaN	NaN	NaN
548	g15005	NaN	NaN	NaN	NaN	NaN	NaN
549	g15007	NaN	NaN	NaN	NaN	NaN	NaN
550	g15009	NaN	NaN	NaN	NaN	NaN	NaN

These 34 counties are missing data in both the original study and our reproduction study. The counties and county equivalents are all located in Hawaii (FIPS code 15) and Alaska (FIPS code 02). In Spielman et al.'s code, when they define the states in FEMA region IX, they do not include HI, and when they define the states in FEMA region X, they do not include AK. All differences here arise from missing data in analogous places in both my output and theirs. This result was successfully reproduced.

State SoVI Scores & Rankings

```
[46]: check_it('State_Sovi_Score.csv')
```

All values match!

We have identically reproduced SoVI scores for all state models.

County in State Rank

```
[47]: check_it("County_in_State_Rank.csv")
```

All values match!

We have identically reproduced the SoVI rankings in the state(s) of interest for all 21 models.

Variable Contributions

```
[48]: check_it("variable_contributions.csv", rounder = 3)
```

All values match!

When rounded to 3 decimal places, we have successfully reproduced all variable contributions for all models.

State FEMA US Rank Correlations

```
[49]: check_it("state_fema_us_rank_correlations.csv", rounder = 14)
```

All values match!

When rounded to 14 decimal places, we have succesfully reproduced all Spearman's rank correlations.

1.3.2 RPr-H2

Next, we tested RPr-H2, that reproduced figures and tables for the internal consistency analysis are not identical to the figures and tables of the original study.

Figure 1

```
[51]: # Edit counties GEOID to match other datasets
    counties["GEOID"] = "g" + counties["GEOID"]

# Select just the rows and columns needed
    counties_CA = counties.loc[counties["STATE"] == "06"]
    counties_CA = counties_CA[["GEOID", "geometry"]]

# Join all datasets
    counties_CA = counties_CA.merge(USA, on = "GEOID")
    counties_CA = counties_CA.merge(FEMA, on = "GEOID")
    counties_CA = counties_CA.merge(CA, on = "GEOID")
```

```
[52]: # Create overarching plot
      fig, ax = plt.subplots(1, 4, figsize=(20, 8))
      fig.tight_layout()
      ax[0].axis('off')
      ax[1].axis('off')
      ax[2].axis('off')
      ax[3].axis('off');
      # Create CA rank map
      top5 CA = counties CA.loc[counties CA["rank CA"] < 6]</pre>
      bottom5_CA = counties_CA.loc[counties_CA["rank_CA"] > 53]
      ax[0].set title("(a) California Analysis")
      counties_CA.plot(ax = ax[0], cmap = mycolor, edgecolor = 'black', linewidth = .
       →1)
      top5_CA.plot(ax = ax[0], column = "rank_CA", cmap = "Reds_r")
      top5_CA.apply(lambda x: ax[0].text(s=round(x['rank_CA']), color = 'black', x=x.
       ogeometry.centroid.coords[0][0], y=x.geometry.centroid.coords[0][1],⊔
       ⇔ha='center', path_effects=[pe.withStroke(linewidth=1.5,_

→foreground="white")]), axis=1, );
      bottom5_CA.plot(ax = ax[0], column = "rank_CA", cmap = "Blues");
      bottom5_CA.apply(lambda x: ax[0].text(s=round(x['rank_CA']), color = 'black',__
       →x=x.geometry.centroid.coords[0][0], y=x.geometry.centroid.coords[0][1],
       ⇔ha='center', path_effects=[pe.withStroke(linewidth=1.5,_

→foreground="white")]), axis=1, );
      # Create FEMA rank map
      top5 CA = counties CA.loc[counties CA["rank FEMA"] < 6]</pre>
      bottom5_CA = counties_CA.loc[counties_CA["rank_FEMA"] > 53]
      ax[1].set title("(b) FEMA Region IX Analysis")
      counties_CA.plot(ax = ax[1], cmap = mycolor, edgecolor = 'black', linewidth = .
      top5_CA.plot(ax = ax[1], column = "rank_FEMA", cmap = "Reds_r")
      top5_CA.apply(lambda x: ax[1].text(s=round(x['rank_FEMA']), color = 'black', __
       →x=x.geometry.centroid.coords[0][0], y=x.geometry.centroid.coords[0][1], __
       ⇔ha='center', path_effects=[pe.withStroke(linewidth=1.5,_

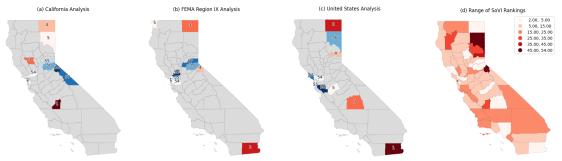
¬foreground="white")]), axis=1, );
```

```
bottom5 CA.plot(ax = ax[1], column = "rank FEMA", cmap = "Blues");
bottom5_CA.apply(lambda x: ax[1].text(s=round(x['rank FEMA']), color = 'black',__
 →x=x.geometry.centroid.coords[0][0], y=x.geometry.centroid.coords[0][1],
 ⇔ha='center', path_effects=[pe.withStroke(linewidth=1.5,_

→foreground="white")]), axis=1, );
# Create USA rank map
top5 CA = counties CA.loc[counties CA["rank USA"] < 6]
bottom5_CA = counties_CA.loc[counties_CA["rank_USA"] > 53]
ax[2].set_title("(c) United States Analysis")
counties_CA.plot(ax = ax[2], cmap = mycolor, edgecolor = 'black', linewidth = .
 ⇒1)
top5 CA.plot(ax = ax[2], column = "rank USA", cmap = "Reds r")
top5_CA.apply(lambda x: ax[2].text(s=round(x['rank_USA']), color = 'black', x=x.
 ⇒geometry.centroid.coords[0][0], y=x.geometry.centroid.coords[0][1],
 ⇔ha='center', path_effects=[pe.withStroke(linewidth=1.5,_

¬foreground="white")]), axis=1, );
bottom5_CA.plot(ax = ax[2], column = "rank_USA", cmap = "Blues");
bottom5_CA.apply(lambda x: ax[2].text(s=round(x['rank_USA']), color = 'black', __
 →x=x.geometry.centroid.coords[0][0], y=x.geometry.centroid.coords[0][1],
 ⇔ha='center', path_effects=[pe.withStroke(linewidth=1.5,_

¬foreground="white")]), axis=1, );
# Create range rank map
ax[3].set title("(d) Range of SoVI Rankings")
counties_CA["min_rank"] = counties_CA[["rank_USA", "rank_FEMA", "rank_CA"]].
 \rightarrowmin(axis = 1)
counties_CA["max_rank"] = counties_CA[["rank_USA", "rank_FEMA", "rank_CA"]].
counties_CA["range_rank"] = counties_CA["max_rank"] - counties_CA["min_rank"]
counties_CA.plot(ax = ax[3], column = "range_rank", cmap = "Reds", edgecolor = counties_can be considered.
 legend=True, classification_kwds=dict(bins=[5,15,25,35,45]));
plt.savefig( here(path["rfig"], 'fig1.png') ) # Save image
```



This figure looks almost the same as Spielman et al's. In (a), rank 3 is in a different place; in (b), rank 4 and rank 5 have switched places, but otherwise everything looks good. Our FEMA and

state SoVI score data perfectly matched Spielman et al's output, so we are not sure what caused these differences.

```
Table 2
[53]: # Read in data
      table2 = pd.read csv(here(path["ddpub"], "state fema us rank correlations.
      # Formatting table
      table2.index = table2["Unnamed: 0"]
      table2 = table2.drop(columns = ["Unnamed: 0"])
      table2["FEMA Region"] = ["I", "II", "III", "IV", "V", "VI", "VII", "VIII",
       table2["All US counties input file versus all counties in a state input file"] [
       ⇔= table2["spearman_r_st_us"].round(2)
      table2["All counties in a FEMA region versus counties in a state within the
       ⇒FEMA region input file"] = table2["spearman_r_st_fema"].round(2)
      table2["State used for comparison"] = ["Composite of ME, NH, MA", "NY", "VA",
       →"GA", "IL", "TX", "MO", "SD", "CA", "ID"]
      table2 = table2.transpose().rename_axis('FEMA Region', axis='columns')
      table2 = table2.rename(columns=table2.iloc[4])
      table2 = table2.drop(labels = ["FEMA Region", "spearman_r_st_fema", __

¬"spearman_r_st_us"], axis = 0)
[54]: if (table2.loc["pvalue_st_fema"] < 0.01).sum() == 10 and (table2.
       →loc["pvalue_st_us"] < 0.01).sum() == 10:</pre>
          table2 = table2.drop(["pvalue_st_fema", "pvalue_st_us"])
          print("p < 0.01 for all values")</pre>
          print("Different result than in paper")
     p < 0.01 for all values
[55]: table2
                                                                                 I \
[55]: FEMA Region
                                                                           0.75
     All US counties input file versus all counties ...
      All counties in a FEMA region versus counties i...
                                                                           0.94
      State used for comparison
                                                          Composite of ME, NH, MA
     FEMA Region
                                                            ΤT
                                                                              V \
                                                                 III
                                                                       ΙV
     All US counties input file versus all counties ... 0.79 0.68 0.5
                                                                          0.5
     All counties in a FEMA region versus counties i... 0.61
                                                               0.9 0.8 0.34
     State used for comparison
                                                                  VA
                                                                       GA
                                                                             IL
                                                            NY
     FEMA Region
                                                            VI
                                                                 VII VIII
     All US counties input file versus all counties ... 0.62 0.9 0.61 0.53
```

```
All counties in a FEMA region versus counties i... 0.68 0.82 0.87 0.69 State used for comparison TX MO SD CA
```

```
FEMA Region X
All US counties input file versus all counties ... 0.66
All counties in a FEMA region versus counties i... 0.88
State used for comparison ID
```

All of these numbers match up with those in Spielman et al's paper except for one, which is reported as 0.65 in their paper rather as opposed to a 0.68 in our work. Since we checked that our data matches their provided output data, they likely made a simple typo when typing up their work for publication.

```
[56]: # Save file
table2.to_csv( here(path["rtab"],"table2.csv") )
```

1.3.3 RPr-H3

Finally, we tested RPr-H3, that reproduced direction reversals and min, average, and max SoVI rank value of 28 demographic variables are not identical to the direction reversals and min, average, and max SoVI rank values shown in figure 2 of the original study.

Figure 2

	[]:	summary_stats
--	-----	---------------

[]:	National Model	Reversals	Min	Average	Max	Range
QAGEDEP_ACS	+	0	1.0	10.90	24.0	23.0
QFEMALE_ACS	+	9	1.0	8.33	28.0	27.0
QSERV_ALT	+	3	1.0	12.48	26.0	25.0
QHISP_ACS	+	3	2.0	11.00	28.0	26.0
QFEMLBR	+	4	1.0	11.62	25.0	24.0
QNATAM_ACS	+	9	1.0	9.62	28.0	27.0
QESL_ALT	+	4	1.0	11.29	27.0	26.0
QSSBEN	+	0	3.0	11.76	21.0	18.0
QNOAUTO_ALT	+	0	1.0	14.05	28.0	27.0
ОМОНО	-	12	2.0	15.29	27.0	25.0
QPOVTY	+	0	3.0	11.71	27.0	24.0
QNRRES_ACS	+	4	1.0	10.19	22.0	21.0
- QFAM	+	2	1.0	13.67	28.0	27.0
QUNOCCHU_ACS	+	6	1.0	10.71	20.0	19.0
- PERCAP_ALT	+	3	9.0	18.48	28.0	19.0
BLACK_ACS	_	12	3.0	17.29	28.0	25.0
- MDGRENT_ALT	+	1	8.0	18.29	27.0	19.0
- QRICH200K	+	6	3.0	19.19	27.0	24.0
MEDAGE_ACS	+	1	8.0	18.19	28.0	20.0
QFHH_ACS	+	6	2.0	17.38	28.0	26.0
PRENTER_ACS	+	7	3.0	18.57	27.0	24.0
POPDENS	+	3	4.0	15.86	26.0	22.0

```
QCVLUN
                                          15
                                              1.0
                                                      13.38
                                                              23.0
                                                                      22.0
                                              5.0
- MHSEVAL ALT
                                           4
                                                      19.29
                                                              28.0
                                                                      23.0
QED12LES ALT
                                           2
                                              4.0
                                                      15.00
                                                              28.0
                                                                      24.0
QEXTRCT_ALT
                                           6
                                              1.0
                                                      17.71
                                                              28.0
                                                                      27.0
QASIAN_ACS
                                              4.0
                                          14
                                                      18.71
                                                              28.0
                                                                      24.0
QPUNIT_ACS
                                          14
                                              2.0
                                                      16.05
                                                              28.0
                                                                      26.0
```

```
[]: # Save file summary_stats.to_csv( here(path["rtab"],"fig2.csv") )
```

As mentioned in the analysis, we eliminated the "expected" column and added minus signs to the variable labels where needed to make the figure more interpretable. The "original" column matches Spielman et al's exactly, but the "reversals" column has 2 minor differences: specifically, in Spielman et al's paper, QNOAUTO_ALT has 1 reversal instead of 0 and QEXTRCT_ALT has 7 reversals instead of 6. These are pretty minor differences. Because our variable_contributions dataset matches Spielman et al's data perfectly, our best guess is that the differences are due to transciption errors when they constructed their figure.

Spielman et al do not provide exact values for our last 4 columns, but everything looks accurate when we compare our numbers to their figure.

1.4 Discussion

The goal of this study was to computationally reproduce Spielman et al's "Evaluating social vulnerability indicators: criteria and their application to the Social Vulnerability Index" (Spielman et al, 2020). To their credit, Spielman et al provided their code, data, and metadata in their sovi-validity GitHub repository, making their analysis transparent, accessible, and reproducible in a manner that is rare in the field of geography.

We have rejected RPr-H1, finding that our reproductions of each of 21 SoVI models were identical to the original results, with the possible exception of a few minor changes in county rank caused by very slightly different calculations of land area and population density. The implication of this finding is that the codified procedures used in this reproduction study can reliably reproduce and replicate the SoVI model. Given our rejection of RPr-H1, we were surprised to have difficulty exactly reproducing RPr-H2 and RPr-H3. Although our results were very similar to figure 1 and figure 2, we did find a few discrepancies in each figure which we can only assume are related to the data visualization process in the original study, which was not automated in code.

In addition to checking the original study results, a major aim of this reproduction study was to improve its computational reproducibility. With all the necessary data and code in one GitHub repository, we did not anticipate conducting a reproduction study. We assumed that we would be able to run their work relatively easily before continuing on to a replication study. However, even with all of the resources they provided, we still spent a month of full-time work on this project before successfully reproducing their results. Our experiences working with this data motivated us to publish this report, so that we can share the obstacles that made the reproduction process so time-intensive and point out methods that researchers can employ to enhance the reproducibility of their work.

The main obstacles that stood in the way of reproducing Spielman et al's results were: 1. Outdated packages 2. Extraneous data and code 3. A confusing file system 4. Incomplete code 5. Our own

edits

Outdated packages The first obstacle, and one that we anticipated because much of Spielman et al's code was written 6 or 7 years ago, was the presence of outdated packages. When working with code developed on outdated packages, one has the option of adjusting their package versions or adapting your code to run on current package versions. We opted for the latter because we found no documentation regarding the package versions used by Spielman et al, and we hope to use our code in the future for a replication study, preferably operating on an up-to-date software environment.

One notable package issue occurred because Spielman et al wrote their code before the refactoring of PySAL into several submodules that occured with the release of PySAL 2.0.0 in 2019. In Spielman et al's work, functions for calculating contiguity-based spatial weights were included in the PySAL package, but after the refactoring, this feature is included in the libpysal package. Without prior familiarity with the intricacies of PySAL's updates over the years, it took us some time to locate equivalent functions in the updated package. Changes to PySAL were perhaps the most time-consuming package update issue, but there were other smaller issues along the way, such as Pandas's deprecation of the .ix indexer in favor of .iloc and .loc. Most edits due to package updates were small, but they all took some time to figure out, time that adds up.

Researchers can eliminate this obstacle to reproducibility by containerizing their work. For this study in particular, we found that providing a list of required packages and their versions in a text file was sufficient to reconstruct the environment on another machine.

Extraneous data and code Another issue that required a substantial amount of effort to overcome was the presence of extraneous data and code. For example, although Spielman et al's paper only mentions 5-year ACS data from 2012, in their data_prep.py file, they also import and manipulate decennial census variables. Unfortunately, they do not comment their code well-enough for other researchers to understand why they do this without combing through every line of code. After some close inspection, we found that all of the decennial variables except for land area are not used to generate their results, allowing us to discard unused data and a substantial amount of code. In their data_prep.py code, Spielman et al also include some analysis of standard errors that we eventually discovered to be unnecessary.

Several other files in Spielman et al's code folder also include extraneous code. In particular, the entire contents of the drop1_place.py, spearman.py, and visualization.py, as well as portions of compute_sovis.py implementing a drop1 analysis turned out to be unnecessary to generate the results they describe in their paper. It seems that Spielman et al were considering several possible directions of research, and they left their dead ends in their code. We omit all of the unnecessary steps in our report, reducing the computational intensity of the analysis and making our work easier to follow.

While the presence of unnecessary code may not have bothered the original authors of the paper, in the absence of comments explaining their purpose, extra code makes it far more difficult for an independent party to understand their work. If one does not quickly realize which parts of the code are actually necessary, they may spend time debugging code just to discard it later on, as we did. Researchers can make it much easier for others to reproduce their work by publishing a clean version of their code with informative comments and no extraneous work.

Confusing file system From our experience working with Spielman et al's repository, we find that an index or some metadata regarding the structure of code and data would be beneficial.

The code for Spielman et al's analysis was originally divided into 6 different python scripts:
- data_prep.py - spss_pca.py - drop1_place.py - compute_sovis.py - spearman.py - visualization.py

While one could infer the order of the scripts from the file names, file contents, and whether a file called any other files, that process took a fair amount of work and left room for error. When one script calls another script which calls another script, it can become difficult to locate the source of an error. Had the researchers provided an index explaining the purpose of each script and how they work together, like our procedure_metadata.csv, that would have reduced the confusion of working with multiple scripts and prevented us from even attempting to debug unnecessary scripts. Similarly, had the authors provided a quick summary of each of their data files, like our data_metadata.csv, then we would have quickly understood the purpose of each data source, instead of guessing at each's purpose based on its name and the code that manipulates it. Generally, the more information a researcher can provide about their data and code upfront, the less time other researchers will need to spend deciphering their files during a reproduction.

Incomplete code While Spielman et al provide all of the code required to reproduce their data files, they do not provide any code for reproducing their figures. By providing their code, data, and metadata in a GitHub repository, they are on the leading edge of reproducibility in geography. However, they could further improve reproducibility by including code to generate their figures. As noted in the results section, the output data files produced by our analysis and provided by Spielman et al were identical, yet our figures exhibited slight differences. Had Spielman et al provided code to produce their figures, it would be absolutely clear whether the differences between our figures were due to typos or a difference in code; and if the differences were typos, then producing their figures with code working directly from their data may have eliminated that issue altogether.

Our own edits The other major time sink occurred because of our own edits. Spielman et al provided data and metadata for reproducing their results; assuming that they acquired their data appropriately, this should be sufficient for a reproduction. However, our end-goal with this project is to produce a replication study that will potentially involve census data from multiple years. To facilitate the acquisition of analogous data in several different time periods, it is helpful to automate the process rather than manually downloading a large number of files. For this reason, we used the python package, pygris, to acquire our data directly from the census via an API. Learning to use pygris and checking that our data sufficiently matches Spielman et al's data was a lengthy but worthy process, as it improves reproducibility and will be useful for our future work.

1.5 Conclusions

While there are ways that Spielman et al could make it easier to reproduce their work, we were able to sufficiently reproduce every relevant output dataset. We find that their results to be legitimate, highlighting issues of internal and theoretical consistency with SoVI.

Our main takeaway from reproducing Spielman et al's work is that merely providing one's code, data, and metadata is insufficient for allowing other researchers to quickly reproduce one's results. In particular, containerizing their software environment, cleaning their code and omitting extraneous information, providing some metadata regarding the structure of their code and data files,

and including code for every step of the analysis from data acquisition to figure production would all enhance the reproducibility of their work. Spielman et al produced a well-designed study in a reproducible repository, but a more carefully designed and fully executable research compendium would reduce the risk of transcription errors and allow researchers to reproduce their results in a more reasonable time frame.

1.6 References

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