



to use neural network to learn flexible nonlinear relationship among features. The powerful



Embedded feature selection methods can combine feature selection with training process into a whole part. The most widely used embedded methods are regularization models that introduce additional constraints into the optimization of a predictive algorithm that bias the

model toward lower complexity. One of famous regularization algorithms is the Lasso pro-



usually in the form of least square or cross entropy loss. In this paper, we just use the least square loss as the fitting error:  $\mathcal{J}_{AE}(X, g(f(X))) = \frac{1}{2m} \sum_{i=1}^m \|\mathbf{x}_i - g(f(\mathbf{x}_i))\|_2^2 = \frac{1}{2m} \|X - g(f(X))\|_F^2$ .



### 3.2 The Proposed Model



the  $i$ th feature contributes little to the representation of other features; on the other hand, if  $i$ th feature plays important role in the representation of other features, then  $\|\mathbf{w}_i\|_2$  must be significant. To select the most discriminative features from original ones, we impose row-

sparse regularization on  $W^{(1)}$ . That is to say, we use  $\mathcal{R}(\Theta) = \|W^{(1)}\|_{2,1} = \sum_i^d \sqrt{\sum_j^h (w_{ij}^{(1)})^2}$



$$\min_{W^{(1)}, W^{(2)}} \frac{1}{2m} \|X - X W^{(1)} W^{(2)}\|_F + \alpha \|W^{(1)}\|_{2,1}. \quad (6)$$

We can find that this form is equivalent to (5), so AEFS is a nonlinear extension of RSR.

## 4 Optimization



We construct a synthetic dataset as shown in Fig. 1. The dataset consists of 200 samples with 3 features  $\{A, B, C\}$ . The dataset are split into 2 classes about fifty-fifty. Feature A



---

**Algorithm 1** Optimization Algorithm of Autoencoder Feature Selector

---



<sup>6</sup><http://www.ncbi.nlm.nih.gov/pubmed/12381711>

<sup>7</sup><http://yann.lecun.com/exdb/mnist/>

<sup>8</sup><http://attributes.kyb.tuebingen.mpg.de/>

Table 1: Summary of used datasets.



<sup>9</sup>Since the result of  $k$ -means depends on initialization, we repeat the experiments 20 times with random initialization and report the average results with standard deviation.



Given two variables  $P$  and  $Q$ , NMI between them is defined as



AWA	14.4±0.3	11.6±0.3	13.2±0.2	12.2±0.3	12.2±0.3	<b>13.4±0.4</b>
-----	----------	----------	----------	----------	----------	-----------------

Table 4: Classification results (ACC%) of different feature selection methods. The best results are highlighted in bold



with much fewer features than the original. However, the reconstructed face of RSR is less similar to raw face than AEFS, especially when the number of selected features is small.

We also evaluate reconstruction ability of denoising AEFS on the face dataset warp-



features.



PIE10P with Gaussian noise. The noise is set zero mean value and 0.5 standard deviation.



- [9] Geoffrey E Hinton and Richard S Zemel. Autoencoders, minimum description length, and helmholtz free energy. *Advances in neural information processing systems*, pages 3–3, 1994.

- [10] Emanuel F. Petricoin Iii, David K. Ornstein, Cloud P. Paweletz, Ali Ardekani, Paul S. Horn, and David A. King. A deep autoencoder for clinical feature extraction. In *Proceedings of the 2016 ACM conference on Health, inference and learning*, pages 1–10. ACM, 2016.



- [24] Pascal Vincent, Hugo Larochelle, Yoshua Bengio, and Pierre-Antoine Manzagol. Extracting and composing robust features with denoising autoencoders. In *Proceedings of the 25th international conference on Machine learning*, pages 1096–1103. ACM, 2008.

- [25] Yi Yang, Heng Tao Shen, Zhigang Ma, Zi Huang, and Xiaofang Zhou. 12, 1-

