## Dig-In:

## The Extreme Value Theorem

We examine a fact about continuous functions.

## Definition 1.

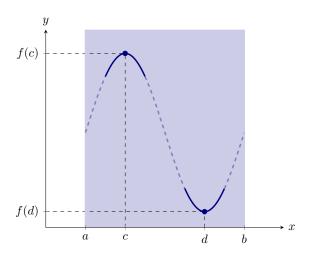
- (a) A function f has an **global maximum** at x = a, if  $f(a) \ge f(x)$  for every x in the domain of the function.
- (b) A function f has an **global minimum** at x = a, if  $f(a) \le f(x)$  for every x in the domain of the function.

A global extremum is either a global maximum or a global minimum.

If we are working on an finite closed interval, then we have the following theorem.

**Theorem 1** (Extreme Value Theorem). If f is a continuous function for all x in the closed interval [a,b], then there are points c and d in [a,b], such that (c, f(c)) is a global maximum and (d, f(d)) is a global minimum on [a,b].

Below, we see a geometric interpretation of this theorem.



Question 1 Would this theorem hold if we were working on an open interval?

## Multiple Choice:

Learning outcomes: Understand the statement of the Extreme Value Theorem.

- (a) yes
- (b) no ✓

**Hint:** Consider  $\tan(\theta)$  for  $-\pi/2 < \theta < \pi/2$ . Does this function achieve its maximum and minimum?