

9/1 Review the following topics from June.  
Complete problems 1-3.

## Quadratics

① solutions  $\rightarrow$  factoring  
 $\rightarrow$  quadratics

② vertex  $f(x) = ax^2 + bx + c$

$$f(x) = a(x-h)^2 + k; \quad h = -\frac{b}{2a}$$

③ discriminant  $= b^2 - 4ac$

$$b^2 - 4ac > 0 \quad 2 \text{ distinct}$$

$$b^2 - 4ac = 0 \quad 1 \text{ distinct (tangent)}$$

$$b^2 - 4ac < 0 \quad 0 \text{ real}$$

④ inequalities

⑤ substitution

## Coordinate Geometry

① midpoint  $\left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$

② gradient  $m = \frac{y_2 - y_1}{x_2 - x_1}$

③ distance  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

④ parallel/perpendicular  $m_1 = m_2$   
 $m_1 \cdot m_2 = -1$

⑤ line  $y = mx + b$

⑥ circle  $(x-h)^2 + (y-k)^2 = r^2$   $x^2 + y^2 + 2gx + 2fy + c = 0$

## Sequence / Series

① Binomial expansion

a) Pascal's triangle

$$b) nCr = \binom{n}{r} = \frac{n!}{r!(n-r)!}$$

$$c) (a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + b^n$$

② arithmetic sequence/series \* common difference  $a_n - a_{n-1}$

$$a) a_n = a_1 + (n-1)d$$

$$b) S_n = \frac{n}{2} (a_1 + a_n) = \frac{n}{2} (a_1 + (n-1)d)$$

③ geometric sequence/series \* common ratio  $\frac{a_n}{a_{n-1}}$

$$a) a_n = a_1 r^{n-1}$$

$$b) S_n = \frac{a_1(1-r^n)}{1-r}$$

$$c) S_\infty = \frac{a_1}{1-r}$$

① The function  $f$  is such that  $f(x) = a^2x^2 - ax + 3b$  for  $x \leq \frac{1}{2a}$ , where  $a$  and  $b$  are constants.

(i) For the case where  $f(-2) = 4a^2 - b + 8$  and  $f(-3) = 7a^2 - b + 14$ , find the possible values of  $a$  and  $b$ . [3]

② Solve the inequality  $x^2 - x - 2 > 0$ . [3]

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(i) Express  $x^2 + 6x + 2$  in the form  $(x+a)^2 + b$ , where  $a$  and  $b$  are constants. [2]

(ii) Hence, or otherwise, find the set of values of  $x$  for which  $x^2 + 6x + 2 > 9$ . [2]

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(i) Express  $2x^2 - 10x + 8$  in the form  $a(x+b)^2 + c$ , where  $a$ ,  $b$  and  $c$  are constants, and use your answer to state the minimum value of  $2x^2 - 10x + 8$ . [4]

(ii) Find the set of values of  $k$  for which the equation  $2x^2 - 10x + 8 = kx$  has no real roots. [4]

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# 9/2 Complete problems 1-6

- ① The point A has coordinates  $(-2, 6)$ . The equation of the perpendicular bisector of the line AB is  $2y = 3x + 5$ .
- (i) Find the equation of AB. [3]
  - (ii) Find the coordinates of B. [3]

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- ② Two points have coordinates  $A(5, 7)$  and  $B(9, -1)$ .
- (i) Find the equation of the perpendicular bisector of AB. [3]
- The line through  $C(1, 2)$  parallel to AB meets the perpendicular bisector of AB at the point X.
- (ii) Find, by calculation, the distance BX. [5]

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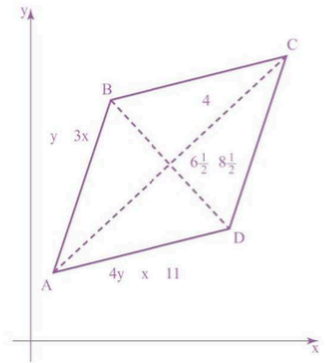
- ③ The point A has coordinates  $(p, 1)$  and the point B has coordinates  $(9, 3p + 1)$ , where  $p$  is a constant.
- (i) For the case where the distance AB is 13 units, find the possible values of  $p$ . [3]
  - (ii) For the case in which the line with equation  $2x + 3y = 9$  is perpendicular to AB, find the value of  $p$ . [4]

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- ④ A line has equation  $y = 2x - 7$  and a curve has equation  $y = x^2 - 4x + c$ , where  $c$  is a constant. Find the set of possible values of  $c$  for which the line does not intersect the curve. [3]

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- ⑤ The diagram shows a parallelogram ABCD, in which the equation of AB is  $y = 3x$  and the equation of AD is  $4y = x + 11$ . The diagonals AC and BD meet at the point  $E(6\frac{1}{2}, 8\frac{1}{2})$ . Find, by calculation, the coordinates of A, B, C and D. [9]



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- ⑥ Find the set of values of  $m$  for which the line  $y = mx + 4$  intersects the curve  $y = 3x^2 - 4x + 7$  at two distinct points. [5]

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# 9/3 Complete problems 1-3. Check your answers!

- ① (i) Find the coefficient of  $x$  in the expansion of  $\left(2x - \frac{1}{x}\right)^5$ . [2]  
 (ii) Hence find the coefficient of  $x$  in the expansion of  $\left(1 + 3x^2\right)\left(2x - \frac{1}{x}\right)^5$ . [4]

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- ② The sum of the 1st and 2nd terms of a geometric progression is 50 and the sum of the 2nd and 3rd terms is 30. Find the sum to infinity. [6]

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- ③ A water tank holds 2000 litres when full. A small hole in the base is gradually getting bigger so that each day a greater amount of water is lost.  
 (i) On the first day after filling, 10 litres of water are lost and this increases by 2 litres each day.  
 (a) How many litres will be lost on the 30th day after filling? [2]  
 (b) The tank becomes empty during the  $n$ th day after filling. Find the value of  $n$ . [3]  
 (ii) Assume instead that 10 litres of water are lost on the first day and that the amount of water lost increases by 10% on each succeeding day. Find what percentage of the original 2000 litres is left in the tank at the end of the 30th day after filling. [4]

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- 4) The function  $f$  is such that  $f(x) = a^2x^2 - ax + 3b$  for  $x \leq \frac{1}{2a}$ , where  $a$  and  $b$  are constants.

- (i) For the case where  $f(-2) = 4a^2 - b + 8$  and  $f(-3) = 7a^2 - b + 14$ , find the possible values of  $a$  and  $b$ . [5]

$$\begin{cases} 4a^2 - b + 8 = 4a^2 + 2a + 3b \\ 7a^2 - b + 14 = 9a^2 + 3a + 3b \end{cases} \Rightarrow \begin{cases} 2a - 8 = 4b \\ 2a^2 + 2a + 4b - 14 = 0 \end{cases}$$

- 1 Solve the inequality  $x^2 - x - 2 > 0$ .

$$x < -1 \text{ or } x > 2$$

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- 2 (i) Express  $x^2 + 6x + 2$  in the form  $(x + a)^2 + b$ , where  $a$  and  $b$  are constants.

$$(x+3)^2 - 7$$

- (ii) Hence, or otherwise, find the set of values of  $x$  for which  $x^2 + 6x + 2 > 9$ . [2]

$$x > 1 \text{ or } x < -7$$

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- 3 (i) Express  $2x^2 - 10x + 8$  in the form  $a(x + b)^2 + c$ , where  $a$ ,  $b$  and  $c$  are constants, and use your answer to state the minimum value of  $2x^2 - 10x + 8$ . [4]

$$2(x - \frac{5}{2})^2 - \frac{9}{2}$$

- (ii) Find the set of values of  $k$  for which the equation  $2x^2 - 10x + 8 = kx$  has no real roots. [4]

$$-18 < k < -2$$

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- 1 The point A has coordinates  $(-2, 4)$ . The equation of the perpendicular bisector of the line AB is  $2y = 3x + 5$ .

- (i) Find the equation of AB.

$$y = -\frac{2}{3}x + \frac{11}{6}$$

- (ii) Find the coordinates of B.

$$B(4, 2) \rightarrow \text{Symmetry}$$

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- 2 Two points have coordinates  $A(5, 7)$  and  $B(8, -1)$ .

- (i) Find the equation of the perpendicular bisector of AB.

$$y = \frac{1}{2}x - \frac{1}{2}$$

- (ii) The line through C  $(1, 2)$  parallel to AB meets the perpendicular bisector of AB at the point X.

- (iii) Find, by calculation, the distance BC.

$$BC = 7.32$$

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- 3 The point A has coordinates  $(p, 1)$  and the point B has coordinates  $(9, p)$ , where  $p$  is a constant.

- (i) For the case where the distance AB is 13 units, find the possible values of  $p$ .

$$p = -15 \text{ or } 14$$

- (ii) For the case where the line with equation  $2x + y + 3$  is perpendicular to AB, find the value of  $p$ .

$$p = 3$$

- 4 A line has equation  $y = 2x - 7$  and a curve has equation  $y = x^2 - 4x + c$ , where  $c$  is a constant.

- (i) Find the set of possible values of  $c$  for which the line does not intersect the curve.

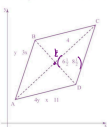
$$c < 2$$

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- 5 The diagram shows a parallelogram ABCD, in which the equation of AB is  $y = 3x$  and the equation of AD is  $y = x + 1$ . The diagonals AC and BD meet at the point E  $(\frac{1}{2}, \frac{1}{2})$ .

- (i) Find, by calculation, the coordinates of A, B, C and D.

$$\begin{aligned} A(1, 3) \\ C(12, 11) \rightarrow \text{symmetry} \\ B(4, 12) \\ D(9, 5) \end{aligned}$$



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- 6 Find the set of values of  $m$  for which the line  $y = mx + 4$  intersects the curve  $y = 3x^2 - 4x + 7$  at two distinct points.

$$m < -10 \text{ or } m > 2$$

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- 1 (i) Find the coefficient of  $x$  in the expansion of  $\left(2x - \frac{1}{x}\right)^5$ . [2]

$$80x$$

- (ii) Hence find the coefficient of  $x$  in the expansion of  $\left(1 + 3x^2\right)\left(2x - \frac{1}{x}\right)^5$ . [4]

$$-40x$$

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- 2 The sum of the 1st and 2nd terms of a geometric progression is 50 and the sum of the 2nd and 3rd terms is 30. Find the sum to infinity. [6]

$$78.1$$

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- 3 A water tank holds 2000 litres when full. A small hole in the base is gradually getting bigger so that each day a greater amount of water is lost.

- (i) On the first day after filling, 10 litres of water are lost and this increases by 2 litres each day.

$$68$$

- (a) How many litres will be lost on the 30th day after filling? [2]

- (b) The tank becomes empty during the  $n$ th day after filling. Find the value of  $n$ . [3]

- (ii) Assume instead that 10 litres of water are lost on the first day and that the amount of water lost increases by 10% on each succeeding day. Find what percentage of the original 2000 litres is left in the tank at the end of the 30th day after filling. [4]

$$17.81\%$$

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