Evan Dietrich // Team 8

```
In [1]:
```

```
import os
import numpy as np
import pandas as pd

import sklearn.linear_model
import sklearn.tree
import sklearn.metrics

from matplotlib import pyplot as plt
import seaborn as sns
```

Pt One: Dropout-Risk Screen

1.1: Compute true/false positives/negatives.

```
In [2]:
def calc TP TN FP FN(ytrue N, yhat N):
    TP = 0.0
    TN = 0.0
    FP = 0.0
    FN = 0.0
    length = len(ytrue_N)
    for i in range(length):
        if (ytrue N[i] == 1 and yhat N[i] == 1):
            TP = TP + 1.0
        if (ytrue N[i] == 0 and yhat N[i] == 0):
            TN = TN + 1.0
        if (ytrue N[i] == 0 and yhat N[i] == 1):
            FP = FP + 1.0
        if (ytrue_N[i] == 1 and yhat N[i] == 0):
            FN = FN + 1.0
```

return TP, TN, FP, FN

calc TP TN FP FN(all0, all1)

```
all0 = np.zeros(10)
all1 = np.ones(10)
```

Out[3]:

In [3]:

(0.0, 0.0, 10.0, 0.0)

In [4]:

```
calc_TP_TN_FP_FN(all1, all0)
```

```
Out[4]:
(0.0, 0.0, 0.0, 10.0)
```

```
In [5]:
calc_TP_TN_FP_FN(all1, all1)
Out[5]:
(10.0, 0.0, 0.0, 0.0)
In [6]:
calc_TP_TN_FP_FN(all0, all0)
Out[6]:
(0.0, 10.0, 0.0, 0.0)
```

Functions for later use

```
In [7]:
```

```
def calc perf metrics for threshold(ytrue N, yprobal N, thresh):
    ''' Compute performance metrics for a given probabilistic cl
assifier and threshold
    tp, tn, fp, fn = calc TP TN FP FN(ytrue N, yprobal N >= thre
sh)
    ## Compute ACC, TPR, TNR, etc.
    acc = (tp + tn) / float(tp + tn + fp + fn + 1e-10)
    tpr = tp / float(tp + fn + 1e-10)
    tnr = tn / float(fp + tn + 1e-10)
    ppv = tp / float(tp + fp + 1e-10)
    npv = tn / float(tn + fn + 1e-10)
    return acc, tpr, tnr, ppv, npv
def print perf metrics for threshold(ytrue N, yprobal N, thresh)
:
    acc, tpr, tnr, ppv, npv = calc perf metrics for threshold(yt
rue N, yprobal N, thresh)
    ## Pretty print the results
   print("%.3f ACC" % acc)
    print("%.3f TPR" % tpr)
   print("%.3f TNR" % tnr)
   print("%.3f PPV" % ppv)
    print("%.3f NPV" % npv)
```

```
In [8]:
def calc confusion matrix for threshold(ytrue N, yprobal N, thre
sh):
    ''' Compute the confusion matrix for a given probabilistic c
lassifier and threshold
    Args
    ytrue N : 1D array of floats
        Each entry represents the binary value (0 or 1) of 'true
' label of one example
        One entry per example in current dataset
    yprobal N : 1D array of floats
        Each entry represents a probability (between 0 and 1) th
```

at correct label is positive (1)

One entry per example in current dataset Needs to be same size as ytrue N

thresh : float

Scalar threshold for converting probabilities into hard decisions

Calls an example "positive" if yproba1 >= thresh

```
Returns
cm df : Pandas DataFrame
```

Can be printed like print(cm df) to easily display resul 1 1 1

cm = sklearn.metrics.confusion matrix(ytrue N, yprobal N >= thresh)

cm df = pd.DataFrame(data=cm, columns=[0, 1], index=[0, 1]) cm df.columns.name = 'Predicted' cm df.index.name = 'True' return cm df

In [9]:

ts

def compute perf metrics across thresholds(ytrue N, yprobal N, t hresh grid=None): ''' Compute common binary classifier performance metrics acr oss many thresholds

If no array of thresholds is provided, will use all 'unique'

```
values
    in the yprobal N array to define all possible thresholds wit
h different performance.
   Args
    ytrue N : 1D array of floats
        Each entry represents the binary value (0 or 1) of 'true
' label of one example
        One entry per example in current dataset
   yprobal N : 1D array of floats
        Each entry represents a probability (between 0 and 1) th
at correct label is positive (1)
        One entry per example in current dataset
    Returns
    thresh grid : 1D array of floats
        One entry for each possible threshold
   perf dict : dict, with key, value pairs:
        * 'acc' : 1D array of accuracy values (one per threshold
        * 'ppv' : 1D array of positive predictive values (one pe
r threshold)
        * 'npv' : 1D array of negative predictive values (one pe
r threshold)
        * 'tpr' : 1D array of true positive rates (one per thres
hold)
        * 'tnr' : 1D array of true negative rates (one per thres
hold)
    if thresh grid is None:
        bin edges = np.linspace(0, 1.001, 21)
        thresh grid = np.sort(np.hstack([bin edges, np.unique(yp
robal N)]))
    tpr grid = np.zeros like(thresh grid)
    tnr grid = np.zeros like(thresh grid)
   ppv grid = np.zeros like(thresh grid)
    npv grid = np.zeros like(thresh grid)
    acc grid = np.zeros like(thresh grid)
    for tt, thresh in enumerate(thresh grid):
        # Apply specific threshold to convert probas into hard b
inary values (0 or 1)
        # Then count number of true positives, true negatives, e
```

```
tc.
        # Then compute metrics like accuracy and true positive r
ate
        acc, tpr, tnr, ppv, npv = calc perf metrics for threshol
d(ytrue N, yprobal N, thresh)
        acc grid[tt] = acc
        tpr grid[tt] = tpr
        tnr grid[tt] = tnr
        ppv grid[tt] = ppv
        npv grid[tt] = npv
    return thresh grid, dict(
        acc=acc grid,
        tpr=tpr grid,
        tnr=tnr grid,
        ppv=ppv grid,
        npv=npv grid)
def make plot perf vs threshold(ytrue N, yprobal N, bin edges=np
.linspace(0, 1, 21)):
    ''' Make pretty plot of binary classifier performance as thr
eshold increases
    Produces a plot with 3 rows:
    * top row: hist of predicted probabilities for negative exam
ples (shaded red)
    * middle row: hist of predicted probabilities for positive e
xamples (shaded blue)
    * bottom row: line plots of metrics that require hard decisi
ons (ACC, TPR, TNR, etc.)
    1 1 1
    fig, axes = plt.subplots(nrows=3, ncols=1, figsize=(12, 8))
    sns.distplot(
        yprobal N[ytrue N == 0],
        color='r', bins=bin edges, kde=False, rug=True, ax=axes[
0]);
    sns.distplot(
        yprobal N[ytrue N == 1],
        color='b', bins=bin edges, kde=False, rug=True, ax=axes[
1]);
    thresh grid, perf grid = compute perf metrics across thresho
lds(ytrue N, yprobal N)
    axes[2].plot(thresh grid, perf grid['acc'], 'k-', label='acc
uracy')
    axes[2].plot(thresh grid, perf grid['tpr'], 'b-', label='TPR
```

```
(recall/sensitivity)')
    axes[2].plot(thresh_grid, perf_grid['tnr'], 'g-', label='TNR
(specificity)')
    axes[2].plot(thresh_grid, perf_grid['ppv'], 'c-', label='PPV
(precision)')
    axes[2].plot(thresh_grid, perf_grid['npv'], 'm-', label='NPV
')

axes[2].legend()
    axes[2].set_ylim([0, 1])
```

Loading dataset

```
In [10]:
```

```
# 3 feature version of x arrays
x_tr_M3 = np.loadtxt('./data_client/x_train.csv', delimiter=',',
skiprows=1)
x_va_N3 = np.loadtxt('./data_client/x_valid.csv', delimiter=',',
skiprows=1)
x_te_N3 = np.loadtxt('./data_client/x_test.csv', delimiter=',',
skiprows=1)

# 2 feature version of x arrays
x_tr_M2 = x_tr_M3[:, :2].copy()
x_va_N2 = x_va_N3[:, :2].copy()
x_te_N2 = x_te_N3[:, :2].copy()
```

In [11]:

```
y_tr_M = np.loadtxt('./data_client/y_train.csv', delimiter=',',
skiprows=1)
y_va_N = np.loadtxt('./data_client/y_valid.csv', delimiter=',',
skiprows=1)
y_te_N = np.loadtxt('./data_client/y_test.csv', delimiter=',', s
kiprows=1)
```

1.2: Computing fractional dropout

In [12]:

```
fractionDropInTrain = 0.0
fractionDropInValid = 0.0
fractionDropInTest = 0.0
countDropInTrain = 0.0
countDropInValid = 0.0
countDropInTest = 0.0
lengthDropTrain = len(y tr M)
lengthDropValid = len(y va N)
lengthDropTest = len(y te N)
for i in range(lengthDropTrain):
        if (y tr M[i] == 1):
            countDropInTrain = countDropInTrain + 1.0
fractionDropInTrain = (countDropInTrain / lengthDropTrain)
for i in range(lengthDropValid):
        if (y va N[i] == 1):
            countDropInValid = countDropInValid + 1.0
fractionDropInValid = (countDropInValid / lengthDropValid)
for i in range(lengthDropTest):
        if (y te N[i] == 1):
            countDropInTest = countDropInTest + 1.0
fractionDropInTest = (countDropInTest / lengthDropTest)
print("Fraction with drop in TRAIN: %.3f" % fractionDropInTrain)
print("Fraction with drop in VALID: %.3f" % fractionDropInValid)
print("Fraction with drop in TEST: %.3f" % fractionDropInTest)
```

Fraction with drop in TRAIN: 0.141 Fraction with drop in VALID: 0.139 Fraction with drop in TEST: 0.139

1.3: Predict-0-always baseline

(a) Computes accuracy of the always-0 classifier.

```
In [13]:
```

```
# See how accurate our prediction is when it predicts always zer
0
# as there are a large number of zeros in the data set... our al
ways-zero
# classifier should have a high % accuracy
lengthDropValid = len(y va N)
alwaysZeroCountValid = 0.0
alwaysZeroCountTest = 0.0
for i in range(lengthDropValid):
        if (y \ va \ N[i] == 0):
            alwaysZeroCountValid = alwaysZeroCountValid + 1.0
accuracyOnValid = (alwaysZeroCountValid / lengthDropValid)
for i in range(lengthDropTest):
        if (y te N[i] == 0):
            alwaysZeroCountTest = alwaysZeroCountTest + 1.0
accuracyOnTest = (alwaysZeroCountTest / lengthDropTest)
print("Always-0: accuracy on VALID: %.3f" % accuracyOnValid)
print("Always-0: accuracy on TEST: %.3f" % accuracyOnTest)
```

```
Always-0: accuracy on VALID: 0.861
Always-0: accuracy on TEST: 0.861
```

(b) Confusion matrix for the always-0 classifier.

In [14]:

```
ytrue_N = y_va_N.copy()
hold_value = float(1 - accuracyOnValid)
yprobal_N = np.copy(ytrue_N)

for i in range(len(ytrue_N)):
    yprobal_N[i] = hold_value

# print(ytrue_N)
# print(yprobal_N)

thresh = 0.5

cm_df = calc_confusion_matrix_for_threshold(ytrue_N, yprobal_N, thresh)
print(cm_df)
```

```
Predicted 0 1
True
0 155 0
1 25 0
```

1.4: Logistic Regression

(a) Creating set of LogisticRegression models.

Each model will use a different control parameter, C, and each will be fit to 2-feature data. Probabilistic predictions will be made on both training set and validation set inputs, and logistic-loss for each will be recorded.

In [15]:

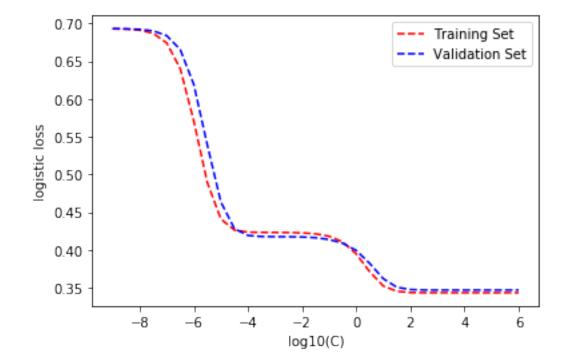
```
x = x_va_N2.copy()
y = y va N.copy()
def run valid loss(C):
    val = C
    C va used list.append(C)
    clf va = sklearn.linear model.LogisticRegression(C = val, so
lver = 'liblinear').fit(X,y)
    result1 = clf va.predict proba(X)
    result1 = result1[:, 1]
    log loss valid = (sklearn.metrics.log loss(y va N, result1))
    va loss list.append(log loss valid)
C grid = np.logspace(-9, 6, 31)
for C in C grid:
   val = 'none'
    run valid_loss(C)
######
X2 = x tr M2.copy()
y2 = y tr M.copy()
def run train loss(C):
    val = C
    C tr used list.append(C)
    clf tr = sklearn.linear model.LogisticRegression(C = val, so
lver = 'liblinear').fit(X2,y2)
    result2 = clf tr.predict proba(X2)
    result2 = result2[:, 1]
    log loss train = (sklearn.metrics.log loss(y tr M, result2))
    tr loss list.append(log loss train)
C grid = np.logspace(-9, 6, 31)
for C in C_grid:
   val = 'none'
    run train loss(C)
```

Plotting logistic loss (y-axis) vs. C (x-axis) on the training set and validation set.

The best values for C and the loss should be printed.

```
In [16]:
```

```
# TODO make plot
plt.xlabel('log10(C)');
plt.ylabel('logistic loss');
log10 C tr used list = C tr used list.copy()
log10 C va used list = C va used list.copy()
for idx in range(len(log10 C tr used list)):
    hold val = log10 C tr used_list[idx]
    new val = np.log10(hold val)
    log10 C tr used list[idx] = new val
for idx in range(len(log10 C_va_used_list)):
    hold val = log10 C va used list[idx]
    new val = np.log10(hold val)
    log10 C va used list[idx] = new val
# print(log10_C_tr_used_list)
plt.plot(log10 C tr used list, tr loss list, 'r--', log10 C va us
ed list, va loss list, 'b--')
plt.legend(['Training Set','Validation Set'])
plt.show()
print(C va used list)
C \text{ val} = C \text{ va used list}[-1]
best val = tr loss list[-1]
# print(C val)
# print(best_val)
# last element of either tr loss list or va loss list
# TODO add legend
# plt.legend(...);
print("Best C-value for LR with 2-feature data: %.1f" % C val) #
TODO
print("Validation set log-loss at best C-value: %.4f" % best val
```



Best C-value for LR with 2-feature data: 1000000.0 Validation set log-loss at best C-value: 0.3433

(b) Plot the performance of the predictions made by the best classifier from step (a) on the validation set.

```
In [17]:
```

```
C = C_val
# print(C)
def run2_valid_loss(C):
    val = C
    C_va_used_list.append(C)
    clf_va = sklearn.linear_model.LogisticRegression(C = val, so
lver = 'liblinear').fit(X,y)
    resultnew1 = clf_va.predict_proba(X)
    resultnew1 = resultnew1[:, 1]
    return resultnew1

resultnew1 = run2_valid_loss(C)

# print(len(resultnew1))

# make_plot_perf_vs_threshold(ytrue_N, resultnew1, bin_edges=np.
linspace(0, 1, 21))
```

(c) Model fitting with 3-feature data

Repeating model generation from 1.4 (a), using full 3-feature data.

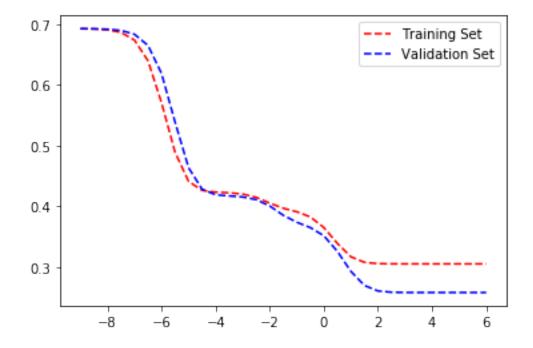
In [18]:

```
lver = 'liblinear').fit(X,y)
   result1 = clf va.predict proba(X)
   result1 = result1[:, 1]
   log loss valid = (sklearn.metrics.log loss(y va N, result1))
   va3 loss list.append(log loss valid)
C grid = np.logspace(-9, 6, 31)
for C in C grid:
   val = 'none'
   run valid loss3(C)
def run train loss3(C):
   val = C
   C3 tr used list.append(C)
   clf tr = sklearn.linear model.LogisticRegression(C = val, so
lver = 'liblinear').fit(X2,y2)
   result2 = clf tr.predict proba(X2)
   result2 = result2[:, 1]
   log loss train = (sklearn.metrics.log loss(y tr M, result2))
   tr3 loss list.append(log loss train)
C grid = np.logspace(-9, 6, 31)
for C in C_grid:
   val = 'none'
   run train loss3(C)
```

Plotting logistic loss (y-axis) vs. C (x-axis) for the 3-feature classifiers on the training set and validation set.

In [19]:

```
log103 C tr used list = C3 tr used list.copy()
log103 C va used list = C3 va used list.copy()
for idx in range(len(log103 C tr used list)):
    hold val = log103 C tr used list[idx]
    new val = np.log10(hold val)
    log103 C tr used list[idx] = new val
for idx in range(len(log103_C_va_used_list)):
    hold val = log103 C va used list[idx]
    new val = np.log10(hold val)
    log103 C va used list[idx] = new_val
plt.plot(log103 C tr used list, tr3 loss list, 'r--', log103 C va
_used_list, va3_loss_list, 'b--')
plt.legend(['Training Set','Validation Set'])
plt.show()
C \text{ val} = C3 \text{ va used list}[-1]
best val = va3 loss list[-1]
print("Best C-value for LR with 3-feature data: %.3f" % C val) #
TODO
print("Validation set log-loss at best C-value: %.4f" % best val
)
```



Best C-value for LR with 3-feature data: 1000000.000 Validation set log-loss at best C-value: 0.2577

Plotting performance of predictions made by the best 3-valued classifier on the validation set.

```
In [20]:
```

```
C = C_val
def run3_valid_loss(C):
    val = C
    C3_va_used_list.append(C)
    clf_va = sklearn.linear_model.LogisticRegression(C = val, so
lver = 'liblinear').fit(X,y)
    resultnew1 = clf_va.predict_proba(X)
    resultnew1 = resultnew1[:, 1]
    return resultnew1

resultnew1 = run3_valid_loss(C)

# make_plot_perf_vs_threshold(ytrue_N, resultnew1, bin_edges=np.
linspace(0, 1, 21))
```

1.5: ROC Curves

Curves allow us to compare model performance in terms of trade-offs between false positive and true positive results.

(a) Plotting ROC curves on the validation set.

Two curves in the plot, one for each of the best two classifiers from prior steps.

In [21]:

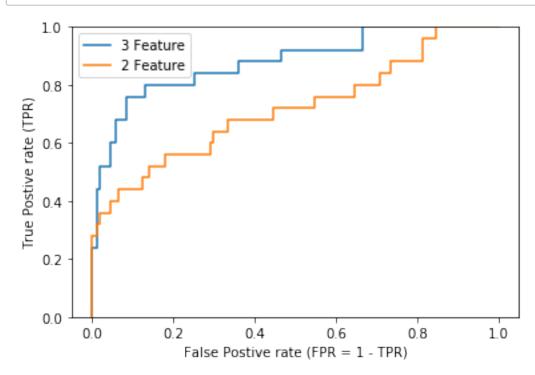
```
y3_3 = y_va_N.copy()
X = x va N3.copy()
y = y va N.copy()
C = 1000000
def run valid loss33(C):
   val = C
   clf vat = sklearn.linear model.LogisticRegression(C = val, s
olver = 'liblinear').fit(X,y)
   result1 = clf vat.predict proba(X)
   result1 = result1[:, 1]
   return result1
newy 3 = run \ valid \ loss33(C)
fpr, tpr, thr = sklearn.metrics.roc_curve(y3_3 ,newy_3) # (y_tru)
e, y score)
plt.plot(fpr, tpr)
# y22 = y tr M.copy()
y3_3 = y_va_N.copy()
X5 = x va N2.copy()
y5 = y_va_N.copy()
C = 1000000
dof run rrolid logg222/C)
```

```
val = C
  clf_va = sklearn.linear_model.LogisticRegression(C = val, so
lver = 'liblinear').fit(X5,y5)
  result2 = clf_va.predict_proba(X5)
  result2 = result2[:, 1]
  return result2

newy_2 = run_valid_loss333(C)
fpr2, tpr2, thr2 = sklearn.metrics.roc_curve(y3_3 ,newy_2)

plt.plot(fpr2, tpr2)
plt.legend(['3 Feature','2 Feature'])

plt.ylim([0, 1]);
plt.xlabel("False Postive rate (FPR = 1 - TPR)");
plt.ylabel("True Postive rate (TPR)");
```



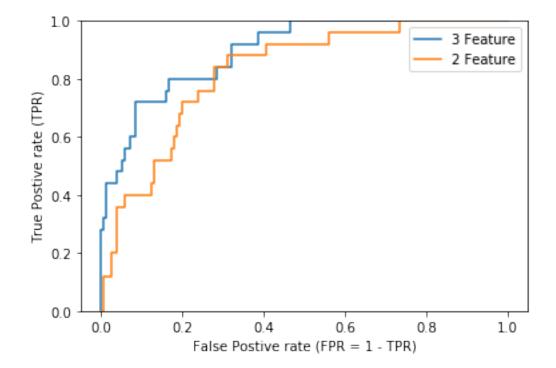
(b) Plot ROC curves on the test set.

There should be two curves in the plot, one for each of the best two classifiers from prior steps.

In [22]:

```
y3_3 = y_te_N.copy()
```

```
X = X \text{ te N3.copy()}
y = y_te_N.copy()
C = 1000000
def run valid loss33(C):
    val = C
    clf vat = sklearn.linear model.LogisticRegression(C = val, s
olver = 'liblinear').fit(X,y)
    result1 = clf vat.predict proba(X)
    result1 = result1[:, 1]
    return result1
newy_3 = run_valid_loss33(C)
fpr, tpr, thr = sklearn.metrics.roc curve(y3 3 ,newy 3)
plt.plot(fpr, tpr)
y3_3 = y_te_N.copy()
X5 = x \text{ te } N2.copy()
y5 = y \text{ te } N.copy()
C = 1000000
def run valid loss333(C):
    val = C
    clf va = sklearn.linear model.LogisticRegression(C = val, so
lver = 'liblinear').fit(X5,y5)
    result2 = clf va.predict proba(X5)
    result2 = result2[:, 1]
    return result2
newy 2 = run \ valid \ loss333(C)
fpr2, tpr2, thr2 = sklearn.metrics.roc curve(y3 3 ,newy 2)
plt.plot(fpr2, tpr2)
plt.legend(['3 Feature','2 Feature'])
plt.ylim([0, 1]);
plt.xlabel("False Postive rate (FPR = 1 - TPR)");
plt.ylabel("True Postive rate (TPR)");
```



(c) Analyzing results shown to compare classifier performance.

With nearly the entirety of the 3 Feature Model having greater accuracy than the 2 Feature Model examples (in both the Validation and Test Sets), it would be fair to say that the 3 Feature Model serves as a better predictive metric for the Drop Dataset in determining which users are likely to drop.

1.6: Selecting a decision threshold

(a) Using default 0.5

```
In [23]:
```

```
best_thr = 0.5

ytrue_N = y_te_N.copy()
yprobal_N = newy_3.copy()
thresh = best_thr

print("ON THE VALIDATION SET:")
print("Chosen best thr = %.4f" % best_thr)
print("")
print("ON THE TEST SET:")
print(calc_confusion_matrix_for_threshold(ytrue_N, yprobal_N, thresh))
print("")
print(print_perf_metrics_for_threshold(ytrue_N, yprobal_N, thresh))
ON THE VALIDATION SET:
Chosen best thr = 0.5000
```

```
ON THE VALIDATION SET:
Chosen best thr = 0.50

ON THE TEST SET:
Predicted 0 1

True
0 149 6
1 14 11

0.889 ACC
0.440 TPR
0.961 TNR
0.647 PPV
0.914 NPV
None
```

(b) Picking threshold to maximize TPR, with realistic PPV

```
In [24]:
```

```
best_thr = 0.69
thresh = best_thr

print("ON THE VALIDATION SET:")
print("Chosen best thr = %.4f" % best_thr)
print("")
print("ON THE TEST SET:")
print(calc_confusion_matrix_for_threshold(ytrue_N, yprobal_N, th resh))
print("")
print(print_perf_metrics_for_threshold(ytrue_N, yprobal_N, thresh))

ON THE VALIDATION SET:
Chosen best thr = 0.6900
```

```
ON THE TEST SET:
Predicted
              0
                 1
True
            155
0
                 0
1
             18
                 7
0.900 ACC
0.280 TPR
1.000 TNR
1.000 PPV
0.896 NPV
None
```

(c) Picking threshold to maximize PPV, while ensuring realistic TPR

```
In [25]:
```

```
best thr = 0.027
thresh = best thr
print("ON THE VALIDATION SET:")
print("Chosen best thr = %.4f" % 0.0)
print("")
print("ON THE TEST SET:")
print(calc confusion matrix for threshold(ytrue N, yprobal N, th
resh))
print("")
print(print perf metrics for threshold(ytrue N, yprobal N, thres
h))
ON THE VALIDATION SET:
Chosen best thr = 0.0000
ON THE TEST SET:
Predicted 0
              1
True
```

1 0.594 ACC

1.000 TPR

0.529 TNR

0.255 PPV

1.000 NPV

None

0

(d) Compare confusion matrices

82

0

73

25

The different thresholds dictate the different numbers of outcomes that occur within the 2x2 contingency matrix.

Matrix (a) delivers a TN value of 149, and a TP value of 11. Matrix (b) delivers a TN value of 155, and a TP value of 7. Matrix (c) delivers a TN value of 82, and a TP value of 25.

In Matrix (c), we succeed in correctly classifying the 25 actual drop cases, but state 73 false .

Matrix (b) delivers no false positives, delivers no improperly-earned Drops, but only acquires 7 actual drop cases (the true positives), and with the cost of missing 18 drop diagnoses (false negatives).

Matrix (a) delivers 6 false drops, by which we acquire 11 actual drop cases (true positives), but still miss 14 should-be diagnosed drops.

If looking to avoid having clients drop at all costs, we go with Matrix (c), as it is the only option from this set of matrices that delivers us the max number of true positives, albeit at the cost of more unnecessary requests.

If we are to use the classifier based in Matrix (c), we would be performing detailing a total of 98 (25+73) total drop-cases. This would let us avoid 82 (180-98) wouldn't-have-been drop-cases. We would in effect be avoiding 45.5% of the diagnoses otherwise used by applying this classifier in the user-base.

In []:			