

# Knowledge Representation and Processing

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# Administrative Information

# Format

## Zoom

- ▶ lectures and exercises via zoom
- ▶ participants muted by default for simplicity
- ▶ interaction strongly encouraged      We don't want to lecture —  
we want to have a conversation during which you learn
- ▶ let's try out zoom
  - ▶ use reactions to say yes no, ask for break etc.
  - ▶ feel free to annotate my slides
  - ▶ talk in the chat

## Recordings

- ▶ maybe prerecorded video lectures or recorded zoom meeting
- ▶ to be decided along the way

# Background

## Instructors

- ▶ Prof. Dr. Michael Kohlhase  
Professor of Knowledge Representation and Processing
- ▶ PD Dr. Florian Rabe  
same research group

## Course

- ▶ This course is given for the first time
- ▶ Always a little bit of an experiment      cutting edge vs. unpolished
- ▶ Could become signature course of our research group      same name!

# Prerequisites

## Required

- ▶ basic knowledge about formal languages, context-free grammars  
but we'll do a quick revision here

## Helpful

- ▶ Algorithms and Data Structures mostly as a contrast to this lecture
- ▶ Basic logic we'll revise it slightly differently here
- ▶ all other courses as examples of how knowledge pervades all of CS

## General

- ▶ Curiosity this course is a bit unusual
- ▶ Interest in big picture  
this course touches on lots of things from all over CS

# Examination and Grading

## Suggestion

- ▶ grade determined by single exam
- ▶ written or oral depends on number of students
- ▶ some acknowledgment for practical exercises

to be finalized next week

## Exam-relevant

- ▶ anything mentioned in notes
- ▶ anything discussed in lectures

neither is a superset of the other!

# Materials and Exam-Relevance

## Textbook

- ▶ does not exist
- ▶ normal for research-near specialization courses

## Notes

- ▶ textbook-style but not as comprehensive
- ▶ developed along the way

## Slides

- ▶ not comprehensive
- ▶ used as visual aid, conversation starters

# Communication

## Open for questions

- ▶ open door policy in our offices if the lockdown ever ends
- ▶ always room for questions during lectures
- ▶ for personal questions, contact me during/after lecture or by email
- ▶ forum at <https://fsi.cs.fau.de/forum/154-Wissensrepraesentation-und-Verarbeitung>

## Materials

- ▶ official notes and slides as pdf:  
<https://kwarc.info/teaching/WuV/>  
will be updated from time to time
- ▶ watch me prepare the materials: <https://github.com/florian-rabe/Teaching/tree/master/WuV>  
pull requests and issues welcome



# Exercises

## Learning Goals

- ▶ Get acquainted with state of the art of practice
- ▶ Try out real tools

## Homeworks

- ▶ one major project as running example
- ▶ homeworks building on each other

build one large knowledge-based system  
details on later slides

# Overview and Essential Concepts

# Representation and Processing

Common pairs of concepts:

Representation	Processing
Static	Dynamic
Situation	Change
Be	Become
Data Structures	Algorithms
Set	Function
State	Transition
Space	Time

## Data and Knowledge

$2 \times 2$  key concepts

Syntax	Data
Semantics	Knowledge

- ▶ Data: any object that can be stored in a computer  
Example:  $((49.5739143, 11.0264941), "2020 - 04 - 21 T16 : 15 : 00 CEST")$
- ▶ Syntax: a system of rules that describes which data is **well-formed**  
Example: "a pair of (a pair of two IEEE double precision floating point numbers) and a string encoding of a time stamp"
- ▶ Semantics: system of rules that determines the meaning of well-formed data
- ▶ Knowledge: combination of some data with its syntax and semantics

# Knowledge is Elusive

## Representation of key concepts

- ▶ Data: using primitive objects  
implemented as bits, bytes, strings, records, arrays, ...
- ▶ Syntax: (context-free) grammars, (context-sensitive) type systems  
implemeted as inductive data structures
- ▶ Semantics: functions for evaluation, interpretation, of well-formed data  
implemented as recursive algorithms on the syntax
- ▶ Knowledge: elusive  
emerges from applying and interacting with the semantics

## Semantics as Translation

- ▶ Knowledge can be captured by a higher layer of syntax
- ▶ Then semantics is translation into syntax

Data syntax	Semantics function	Knowledge syntax
SPARQL query	evaluation	result set
SQL query	evaluation	result table
program	compiler	binary code
program expression	interpreter	result value
logical formula	interpretation in a model	mathematical object
HTML document	rendering	graphics context

# Heterogeneity of Data and Knowledge

- ▶ Capturing knowledge is difficult
- ▶ Many different approaches to semantics
  - ▶ fundamental formal and methodological differences
  - ▶ often captured in different fields, conferences, courses, languages, tools
- ▶ Data formats equally heterogeneous
  - ▶ ontologies
  - ▶ programs
  - ▶ logical proofs
  - ▶ databases
  - ▶ documents

# Challenges of Heterogeneity

## Challenges

- ▶ collaboration across communities
- ▶ translation across languages
- ▶ conversion between data formats
- ▶ interoperability across tools

## Sources of problems

- ▶ interoperability across formats/tools major source of
  - ▶ complexity
  - ▶ bugs
- ▶ friction in project team due to differing preferences, expertise
- ▶ difficult choice between languages/tools with competing advantages
  - ▶ reverting choices difficult, costly
  - ▶ maintaining legacy choices increases complexity



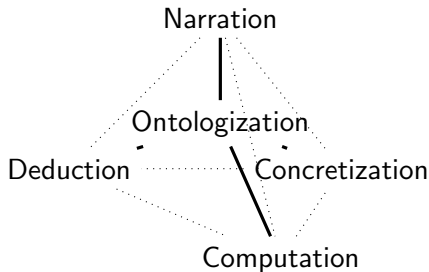
## Aspects of Knowledge

- ▶ Tetrapod model of knowledge      **active research by our group**
- ▶ classifies approaches to knowledge into five aspects

Aspect	KRLs (examples)
ontologization	ontology languages (OWL), description logics (ALC)
concretization	relational databases (SQL, JSON)
computation	programming languages (C)
deduction	logics (HOL)
narration	document languages (HTML, LaTeX)

## Relations between the Aspects

Ontology is distinguished: capture the knowledge that the other four aspects share



## Complementary Advantages of the Aspects

Aspect	objects	characteristic		
		advantage	joint advantage of the other aspects	application
ded. comp.	formal proofs programs	correctness efficiency	ease of use well-definedness	verification execution
concr. narr.	concrete objects texts	tangibility flexibility	abstraction formal semantics	storage/retrieval human understanding

Aspect pair	characteristic advantage
ded./comp. narr./concr.	rich meta-theory simple languages
ded./narr. comp./concr.	theorems and proofs normalization
ded./concr. comp./narr.	decidable well-definedness Turing completeness

# Structure of the Course

## Aspect-independent parts

- ▶ general methods that are shared among the aspects
- ▶ to be discussed as they come up

## Aspects-specific parts

- ▶ one part (about 2 weeks) for each aspect
- ▶ high-level overview of state of the art
- ▶ focus on comparison/evaluation of the aspect-specific results

## Structure of the Exercises

### One major project

- ▶ representative for a project that a CS graduate might be put in charge of
- ▶ challenging heterogeneous data and knowledge
- ▶ requires integrating/combining different languages, tools

unique opportunity in this course because knowledge is everywhere

### Concrete project

- ▶ develop a univis-style system for a university
- ▶ lots of heterogeneous knowledge
  - ▶ course and program descriptions
  - ▶ legal texts
  - ▶ websites
  - ▶ grade tables
  - ▶ transcript generation code
- ▶ build a completely functional system applying the lessons of the course

# Ontological Knowledge

## Components of an Ontology

8 main declarations

- ▶ **individual** — concrete objects that exist in the real world, e.g., "Florian Rabe" or "WuV"
- ▶ **concept** — abstract groups of individuals, e.g., "instructor" or "course"
- ▶ **relation** — binary relations between two individuals, e.g., "teaches"
- ▶ **properties** — binary relations between an individuals and a concrete value (a number, a date, etc.), e.g., "has-credits"
- ▶ **concept assertions** — the statement that a particular individual is an instance of a particular concept
- ▶ **relation assertions** — the statement that a particular relation holds about two individuals
- ▶ **property assertions** — the statement that a particular individual has a particular value for a particular property
- ▶ **axioms** — statements about relations between concepts, e.g., "instructor"  $\sqsubseteq$  "person"

# Divisions of an Ontology

## Abstract vs. concrete

- ▶ TBox: concepts, relations, properties, axioms  
everything that does not use individuals
- ▶ ABox: individuals and assertions

## Named vs. unnamed

- ▶ Signature: individuals, concepts, relations, properties  
together called entities or resources
- ▶ Theory: assertions, axioms



# Comparison of Terminology

Here	OWL	Description logics	ER model	UML	semantics via logics
individual	instance	individual	entity	object, instance	constant
concept	class	concept	entity-type	class	unary predicate
relation	object property	role	role	association	binary predicate
property	data property	(not common)	attribute	field of base type	binary predicate

domain	individual	concept
type theory, logic	constant, term	type
set theory	element	set
database	row	table
philosophy <sup>1</sup>	object	property
grammar	proper noun	common noun

<sup>1</sup>as in <https://plato.stanford.edu/entries/object/>

## Ontologies as Sets of Triples

Assertion	Triple		
	Subject	Predicate	Object
concept assertion	"Florian Rabe"	is-a	"instructor"
relation assertion	"Florian Rabe"	"teaches"	"WuV"
property assertion	"WuV"	"has credits"	7.5

Efficient representation of ontologies using RDF and RDFS  
standardized special entities.

## Special Entities

RDF and RDFS define special entities for use in ontologies:

- ▶ "rdfs:Resource": concept of which all individuals are an instance and thus of which every concept is a subconcept
- ▶ "rdf:type": relates an entity to its type:
  - ▶ an individual to its concept (corresponding to is-a above)
  - ▶ other entities to their special type (see below)
- ▶ "rdfs:Class": special class for the type of classes
- ▶ "rdf:Property": special class for the type of properties
- ▶ "rdfs:subClassOf": a special relation that relates a subconcept to a superconcept
- ▶ "rdfs:domain": a special relation that relates a relation to the concepts of its subjects
- ▶ "rdfs:range": a special relation that relates a relation/property to the concept/type of its objects

Goal/effect: capture as many parts as possible as RDF triples.

## Declarations as Triples using Special Entities

Assertion	Triple		
	Subject	Predicate	Object
individual	individual	"rdf:type"	"rdfs:Resource"
concept	concept	"rdf:type"	"rdf:Class"
relation	relation	"rdf:type"	"rdf:Property"
property	property	"rdf:type"	"rdf:Property"
concept assertion	individual	"rdf:type"	concept
relation assertion	individual	relation	individual
property assertion	individual	property	value
for special forms of axioms			
$c \sqsubseteq d$	$c$	"rdfs:subClassOf"	$d$
$\text{dom } r \equiv c$	$r$	"rdfs:domain"	$c$
$\text{rng } r \equiv c$	$r$	"rdfs:range"	$c$

## An Example Ontology Language

see syntax of BOL in the lecture notes

# Semantics as Translation

## Example: Syntax of Arithmetic Language

Syntax: represented as formal grammar

### Numbers

$N ::= 0$		$1$	literals
		$N + N$	sum
		$N * N$	product

### Formulas

$F ::= N \doteq N$	equality
$N \leq N$	ordering by size

Implementation as inductive data type

## Example: Semantics of Arithmetic Language

Semantics: represented as translation into known language

Problem: Need to choose a known language first

Here: unary numbers represented as strings

Built-in data (strings and booleans):

$S ::= \varepsilon$	empty
(Unicode)	characters
$B ::= \text{true}$	truth
false	falsity

Built-in operations to work on the data:

- ▶ concatenation of strings  $S ::= \text{conc}(S, S)$
- ▶ replacing all occurrences of  $c$  in  $S_1$  with  $S_2$   
 $S ::= \text{replace}(S_1, c, S_2)$
- ▶ equality test:  $B ::= S_1 == S_2$
- ▶ prefix test:  $B ::= \text{startsWith}(S_1, S_2)$



## Example: Semantics of Arithmetic Language

Represented as function from syntax to semantics

- ▶ mutually recursive, inductive functions for each non-terminal symbol
- ▶ compositional: recursive call on immediate subterms of argument

For numbers  $n$ : semantics  $\llbracket n \rrbracket$  is a string

- ▶  $\llbracket 0 \rrbracket = \varepsilon$
- ▶  $\llbracket 1 \rrbracket = \text{"|"}$
- ▶  $\llbracket m + n \rrbracket = \text{conc}(\llbracket m \rrbracket, \llbracket n \rrbracket)$
- ▶  $\llbracket m * n \rrbracket = \text{replace}(\llbracket m \rrbracket, \text{"|"}, \llbracket n \rrbracket)$

For formulas  $f$ : semantics  $\llbracket f \rrbracket$  is a boolean

- ▶  $\llbracket m \dot{=} n \rrbracket = \llbracket m \rrbracket == \llbracket n \rrbracket$
- ▶  $\llbracket m \leq n \rrbracket = \text{startsWith}(\llbracket n \rrbracket, \llbracket m \rrbracket)$

## Semantics of BOL

Aspect	kind of semantic language	semantic language
deduction	logic	SFOL
concretization	database language	SQL
computation	programming language	Scala
narration	natural language	English

see details of each translation in the lecture notes

## General Definition

A semantics by translation consists of

- ▶ syntax: a formal language  $I$
- ▶ semantic language: a formal language  $L$   
different or same aspect as  $I$
- ▶ semantic prefix: a theory  $P$  in  $L$   
formalizes fundamentals that are needed to represent  $I$ -objects
- ▶ interpretation: translates every  $I$ -theory  $T$  to an  $L$ -theory  $P, \llbracket T \rrbracket$

## Common Principles

Properties shared by all semantics of BOL

not part of formal definition, but best practices

- ▶  $I$ -declaration translated to  $L$ -declaration for the same name
- ▶ ontologies translated declaration-wise
- ▶ one inductive function for every kind of complex  $I$ -expression
  - ▶ individuals, concepts, relations, properties, formulas
  - ▶ maps  $I$ -expressions to  $L$ -expressions
- ▶ atomic cases (base cases):  $I$ -identifier translated to  $L$ -identifier of the same name or something very similar
- ▶ complex cases (step cases): compositional

## Compositionality

Case for operator  $*$  in interpretation function compositional iff interpretation of  $*(e_1, \dots, e_n)$  only depends on the interpretation of the  $e_i$

$$\llbracket *(e_1, \dots, e_n) \rrbracket = \llbracket * \rrbracket (\llbracket e_1 \rrbracket, \dots, \llbracket e_n \rrbracket)$$

for some function  $\llbracket * \rrbracket$

Example:  $;$ -operator of BOL in translation to FOL

- ▶ translation:  $\llbracket R_1; R_2 \rrbracket = \exists m : \iota. \llbracket R_1 \rrbracket(x, m) \wedge \llbracket R_2 \rrbracket(m, y)$
- ▶ special case of the above via
  - ▶  $* = ;$ ;
  - ▶  $n = 2$
  - ▶  $\llbracket ; \rrbracket = (p_1, p_2) \mapsto \exists m : \iota. p_1(x, m) \wedge p_2(m, y)$
- ▶ Indeed, we have  $\llbracket R_1; R_2 \rrbracket = \llbracket ; \rrbracket (\llbracket R_1 \rrbracket, \llbracket R_2 \rrbracket)$

## Compositionality (2)

Translation compositional iff

- ▶ one translation function for each non-terminal all written  $\llbracket - \rrbracket$
- ▶ each defined by one induction on syntax  
i.e., one case for production  
mutually recursive
- ▶ all cases compositional

Substitution theorem: a compositional translation satisfies

$$\llbracket E(e_1, \dots, e_n) \rrbracket = \llbracket E \rrbracket(\llbracket e_1 \rrbracket, \dots, \llbracket e_n \rrbracket)$$

for

- ▶ every expression  $E(N_1, \dots, N_n)$  with non-terminals  $N_i$
- ▶ some function  $\llbracket E \rrbracket$  that only depends on  $E$

## Compositionality (3)

$$\llbracket E(e_1, \dots, e_n) \rrbracket = \llbracket E \rrbracket(\llbracket e_1 \rrbracket, \dots, \llbracket e_n \rrbracket)$$

for every expression  $E(N_1, \dots, N_n)$  with non-terminals  $N_i$

Now think of

- ▶ variable  $x_i$  of type  $N_i$  instead of non-terminal  $N_i$
- ▶  $E(x_1, \dots, x_n)$  as expression with free variables  $x_i$  of type  $N_i$
- ▶ expressions  $e$  derived from  $N$  as expressions of type  $N$
- ▶  $E(e_1, \dots, e_n)$  as result of substituting  $e_i$  for  $x_i$
- ▶  $\llbracket E \rrbracket(x_1, \dots, x_n)$  as (semantic) expression with free variables  $x_i$

Then both sides of equations act on  $E(x_1, \dots, x_n)$ :

- ▶ left side yields  $\llbracket E(e_1, \dots, e_n) \rrbracket$  by
  - ▶ first substitution  $e_i$  for  $x_i$
  - ▶ then semantics  $\llbracket - \rrbracket$  of the whole
- ▶ right side yields  $\llbracket E \rrbracket(\llbracket e_1 \rrbracket, \dots, \llbracket e_n \rrbracket)$  by
  - ▶ first semantics  $\llbracket - \rrbracket$  of all parts
  - ▶ then substitution  $\llbracket e_i \rrbracket$  for  $x_i$

semantics commutes with substitution

# Non-Compositionality

## Examples

- ▶ deduction: cut elimination, translation from natural deduction to Hilbert calculus
- ▶ computation: optimizing compiler, e.g., loop unrolling
- ▶ concretization: query optimization, e.g., turning a WHERE of a join into a join of WHEREs,
- ▶ narration: ambiguous words are translated based on context

## Typical sources

- ▶ subcases in a case of translation function
  - ▶ based on inspecting the arguments, e.g., subinduction
  - ▶ based on context
- ▶ custom-built semantic prefix