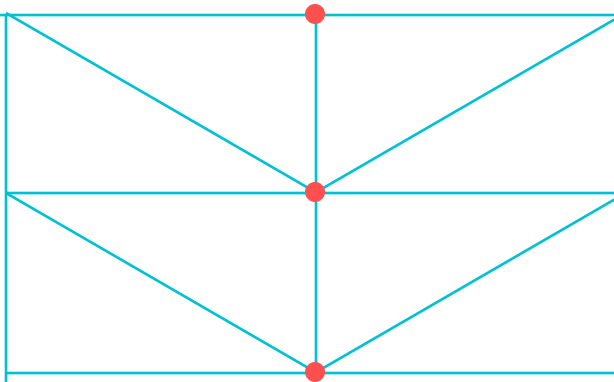


# Introduction to IEEE 802.15.4



**TUHH**  
Institute of  
Communication  
Networks



**Yevhenii Shudrenko and Koojana Kuladinithi**  
**14<sup>th</sup> of April – 17<sup>th</sup> of April 2025**

# Course Contents

## Online lectures

- ~~Lecture 1 – Introduction~~
- ~~Lecture 2 – IEEE 802.15.4~~
- ~~Lecture 3 – IETF 6TiSCH~~

## Physical Meeting 13<sup>th</sup> to 17<sup>th</sup> of April

- Lecture 4 – Theoretical Analysis
- Cooja Simulations and Experiments
- Industrial visit and a talk
- Team Presentations on self learned material
- Lecture 5 – Research Project Results

More details on our padlet,

<https://tuhh.padlet.org/c00zll01/enabling-industry-4-0-j88rkh1i3j7rzmV3>

# Performance Evaluation of 6TiSCH

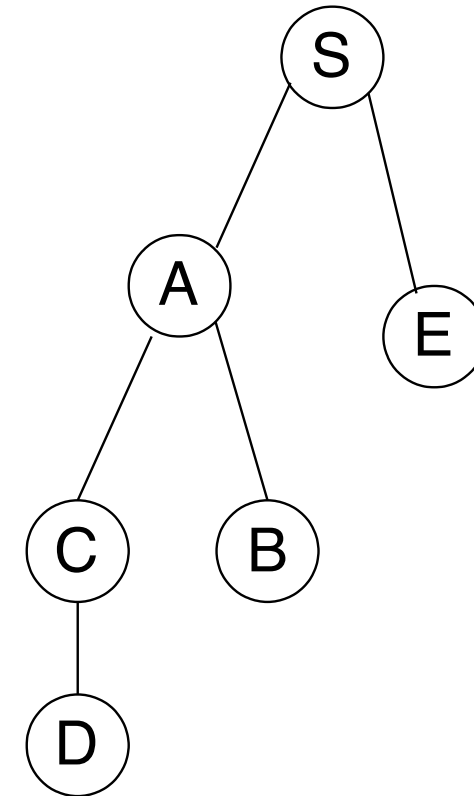
These slides were prepared using the following reference.

[1] Shudrenko, Yevhenii, and Andreas Timm-Giel. "Modeling end-to-end delays in TSCH wireless sensor networks using queuing theory and combinatorics." Computing (2024):1-25.



**Discuss the following:**

- **What kind of delays are involved when A sends data to S?**
- **When C sends data to S?**
- **What is definition of end-to-end delay?**



## End-to-End Delay contd.

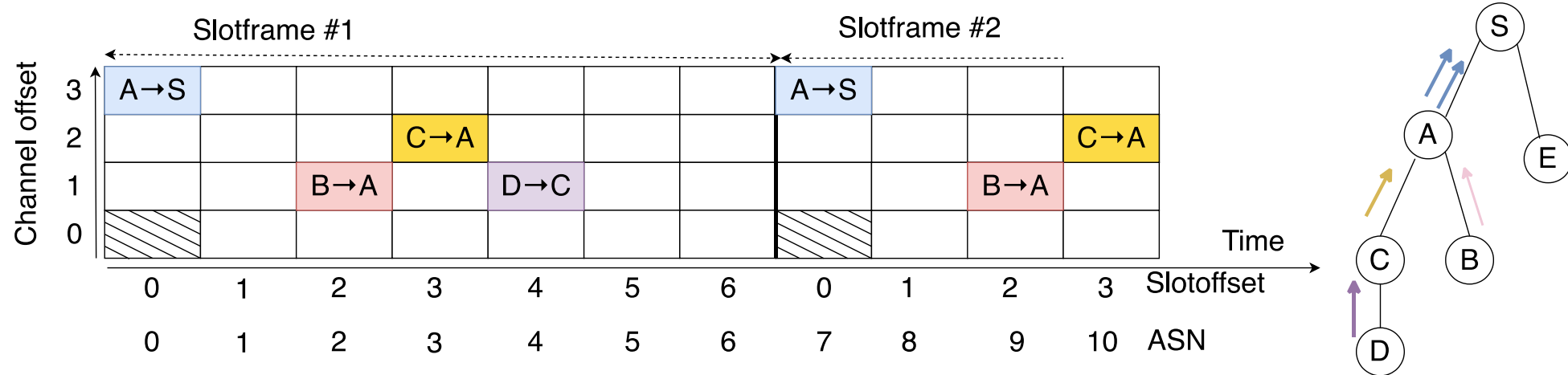
$$D(h) = \sum_{i=1}^h D_i = \sum_{i=1}^h (D_p + D_s + D_t + T_i),$$

- $D_p$  is the propagation delay
- $D_s$  is the processing delay
- $D_t$  is the transmission delay
- $T_i$  is the queuing delay (sojourn time)
  - consists of the service time  $W$  and queuing time  $Q$

**Any delays to be ignored?**

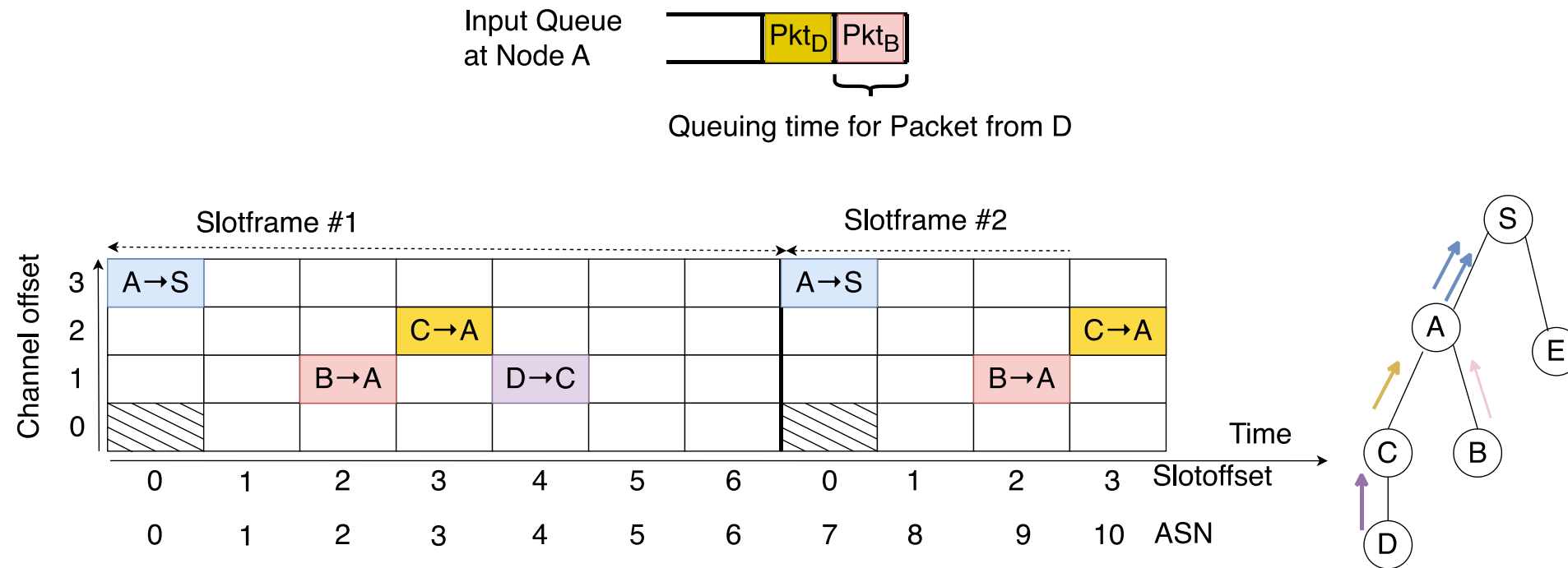
# Service Time

- D transmits a packet at ASN = 4.
  - How many slots does this packet wait at C?
  - How many slots does this packet wait at A?

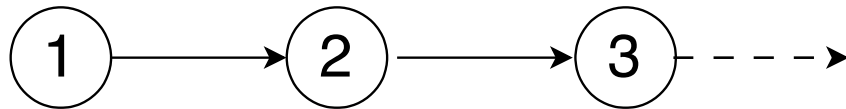


# Queuing Time

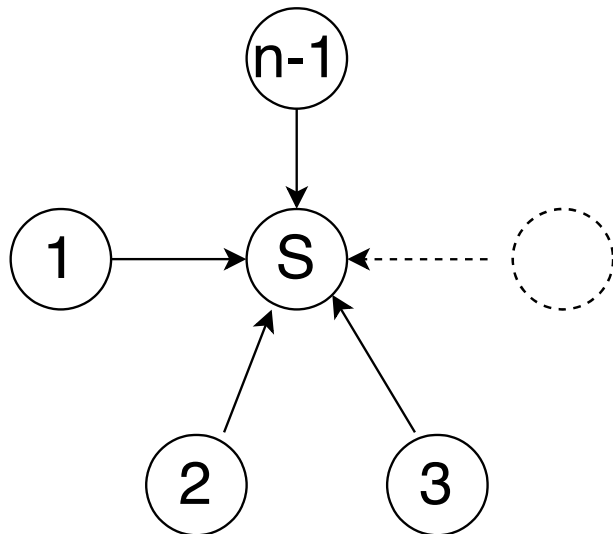
- Assume the case where B transmits at ASN = 2 and D transmits at ASN = 4



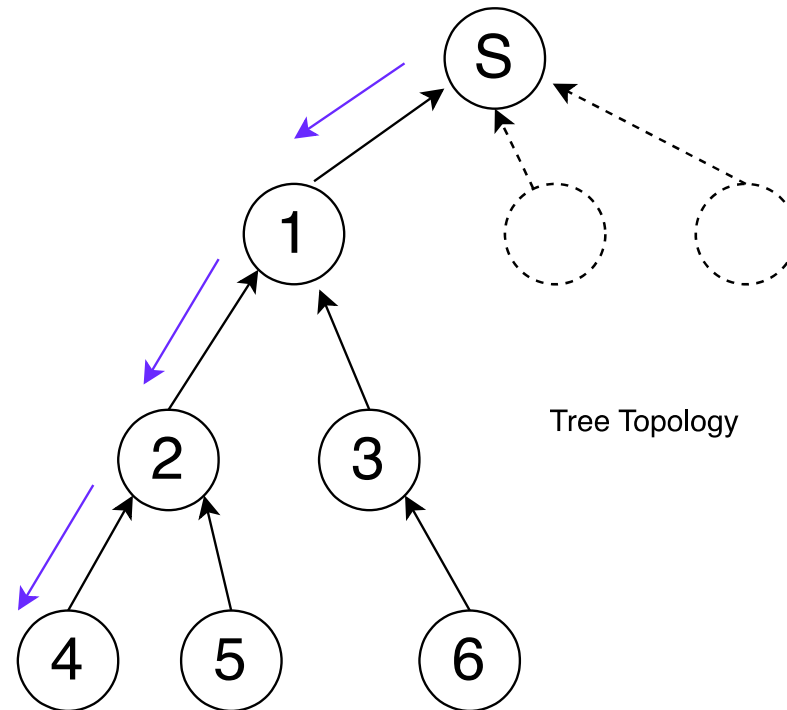
# Network Topologies



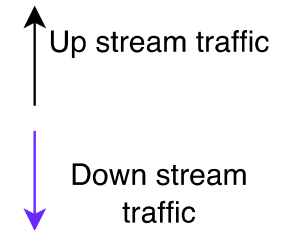
Linear Topology



Star Topology



Tree Topology





# Theoretical Analysis

- Why do we need theoretical analysis?
- Assumptions!
- Jupyter Notebook
  - linear topology
  - model end-to-end delay with
    - service, queuing times
    - periodic packet arrivals

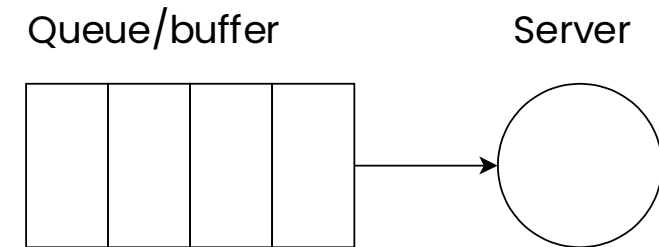


# Queue Model

- Single server
- Unlimited buffer
- Arrival rate  $\lambda$  in packets per slotframe (pkt/sf)
  - Periodic arrivals
- Service rate  $\mu$  in cells per slotframe

## Are these scenarios valid?

- $\lambda = 1.3, \mu = 2$
- $\lambda = 2.3, \mu = 2$
- $\lambda = 1.3, \mu = 1.6$

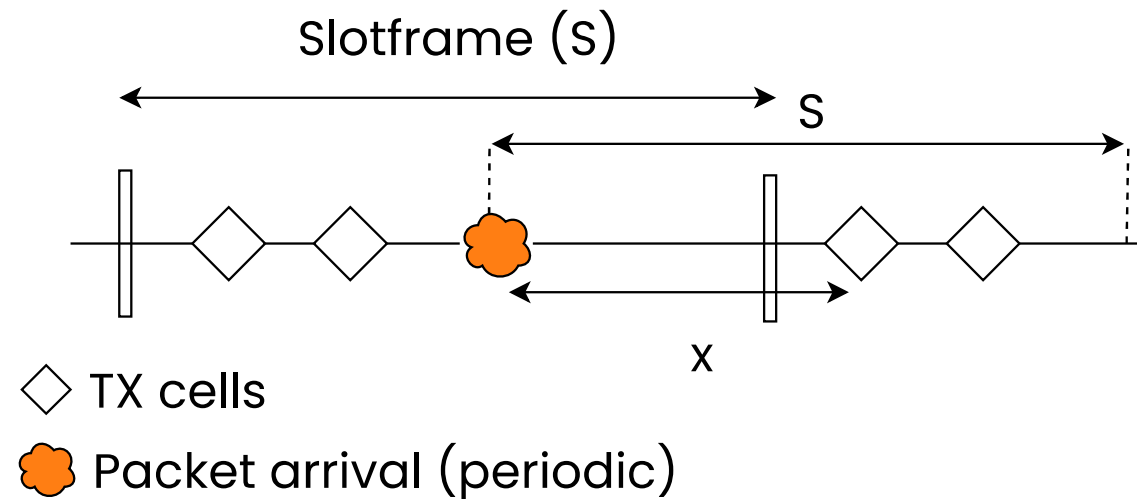


# Service Time Modeling

- Packet arrives in an empty queue
- The Cumulative Distribution Function (CDF) of the service time is

$$F_W = (W < x) = 1 - \left(1 - \frac{x}{S}\right)^\mu,$$

- $S$  is the slotframe length in time slots
- $0 < W < S$



**Run cell A1 of the Jupyter Notebook**

## Service Time Modeling contd.

- Given the CDF, the probability density function is (by definition):

$$f_W(x) = \frac{d}{dx} F_W(x) = \frac{\mu}{S} \left(1 - \frac{x}{S}\right)^{\mu-1}$$

- And the mean value:

$$E[W] = \int_0^S x f_W(x) dx = \dots = \frac{1}{\mu + 1}$$

**Run cell A2 of the Jupyter Notebook**

## Service Rate in MSF

- Adapted based on cell utilization
  - Upper threshold  $u_h$

$$\mu = \left\lceil \frac{\lambda}{u_h} \right\rceil$$

**What is the impact of a high/low  $u_h$ ?**

# Sojourn Time

- The total time  $T$  spent by a packet in the queue
  - Its own service time  $W$  (head of the queue)
  - But might also wait for previous packets to be served (queuing time  $Q$ )

$$T = W + Q$$

- Over  $n$  hops,

**Run cells B and C of the Jupyter Notebook**

$$T^{(n)} = \sum_{i=1}^n T_i$$

# Impact of Traffic Patterns on the Sojourn Time

- Periodic
  - Deterministic, no queuing (almost, check cell D of the Jupyter Notebook for more details)
- Event driven
  - Poisson arrivals, queuing delays due to exponentially distributed interarrival times

$$T_p = W + Q_p = \frac{1}{\mu + 1} + \frac{\rho}{2\mu(1 - \rho)},$$

$Q_p$  is the queuing time with Poisson traffic,

$\rho = \frac{\lambda}{\mu}$  is the system utilization.

**Run cells D & E of the Jupyter Notebook**