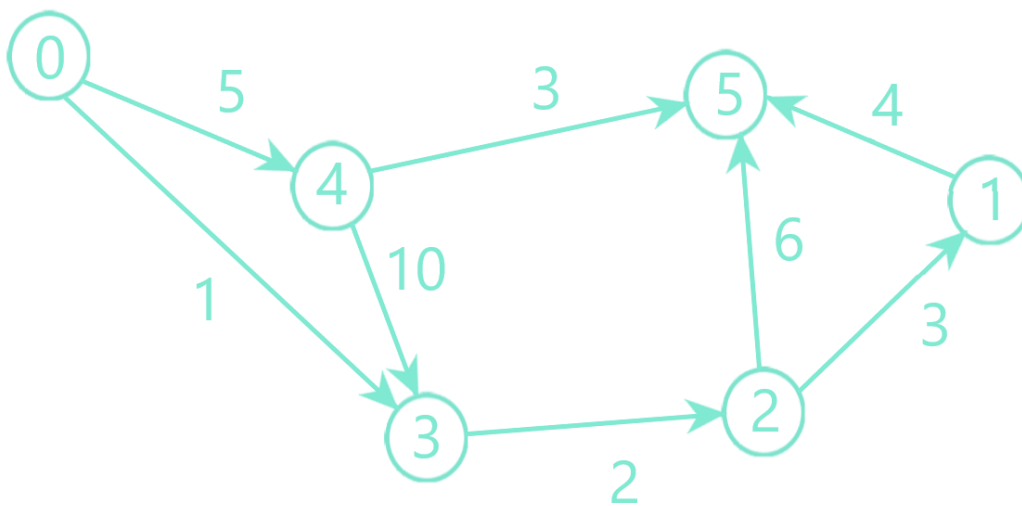


The implementation of `backwards_dijkstra(graph, start, end)` can be found in `Walks.py`.

The output of the function is composed of two dictionaries: `successors`(every node is mapped to it's successor in the minimum cost walk) and `distances`(every node is mapped to the minimum cost walk between start and itself). Then in the controller the path is computed using the `successors` dictionary and the distance using the `distances` dictionary.

For the following graph, the processed output is: $1 \leftarrow 2 \leftarrow 3 \leftarrow 0$ Length: 6, when start is 0 and end is 1.



And the unprocessed output is:

<code>successors={</code>	<code>Distances={</code>
<code>1: -1,</code>	<code>1: 0,</code>
<code>2: 1,</code>	<code>2: 3,</code>
<code>3: 2,</code>	<code>3: 5,</code>
<code>0: 3,</code>	<code>0: 6,</code>
<code>4: 3</code>	<code>4: 15</code>
<code>}</code>	<code>}</code>

Initial state:

Queue: (0, 1)

Successors: {1: -1}

Distances: {1: 0}

Step 1

Before changes

Queue after change: (0, 1)

Successors: {1: -1}

Distances: {1: 0}

After 2 is processed

Queue after change: (3, 2)

Successors: {1: -1, 2: 1}

Distances: {1: 0, 2: 3}

Step 2

Before changes

Queue after change: (3, 2)

Successors: {1: -1, 2: 1}

Distances: {1: 0, 2: 3}

After 3 is processed

Queue after change: (5, 3)

Successors: {1: -1, 2: 1, 3: 2}

Distances: {1: 0, 2: 3, 3: 5}

Step 3

Before changes

Queue after change: (5, 3)

Successors: {1: -1, 2: 1, 3: 2}

Distances: {1: 0, 2: 3, 3: 5}

After 0 is processed

Queue after change: (6, 0)

Successors: {1: -1, 2: 1, 3: 2, 0: 3}

Distances: {1: 0, 2: 3, 3: 5, 0: 6}

After 4 is processed

Queue after change: (6, 0) (15, 4)

Successors: {1: -1, 2: 1, 3: 2, 0: 3, 4: 3}

Distances: {1: 0, 2: 3, 3: 5, 0: 6, 4: 15}

Step 4

Before changes

Queue after change: (6, 0) (15, 4)

Successors: {1: -1, 2: 1, 3: 2, 0: 3, 4: 3}

Distances: {1: 0, 2: 3, 3: 5, 0: 6, 4: 15}

Now if start is in the keys of either dictionaries, then it means there is a walk between the two nodes and the path is reconstructed from the successors dictionary (implementation in controller.py, backwards_dijkstra).

Initial state:

Path: []

Distance: -1

Step 1

Current: 0

Step 2

Current: 3

Path: [0]

Step 3

Current: 2

Path: [3, 0]

Step 4

Current: 1

Path: [2, 3, 0]

Step 5

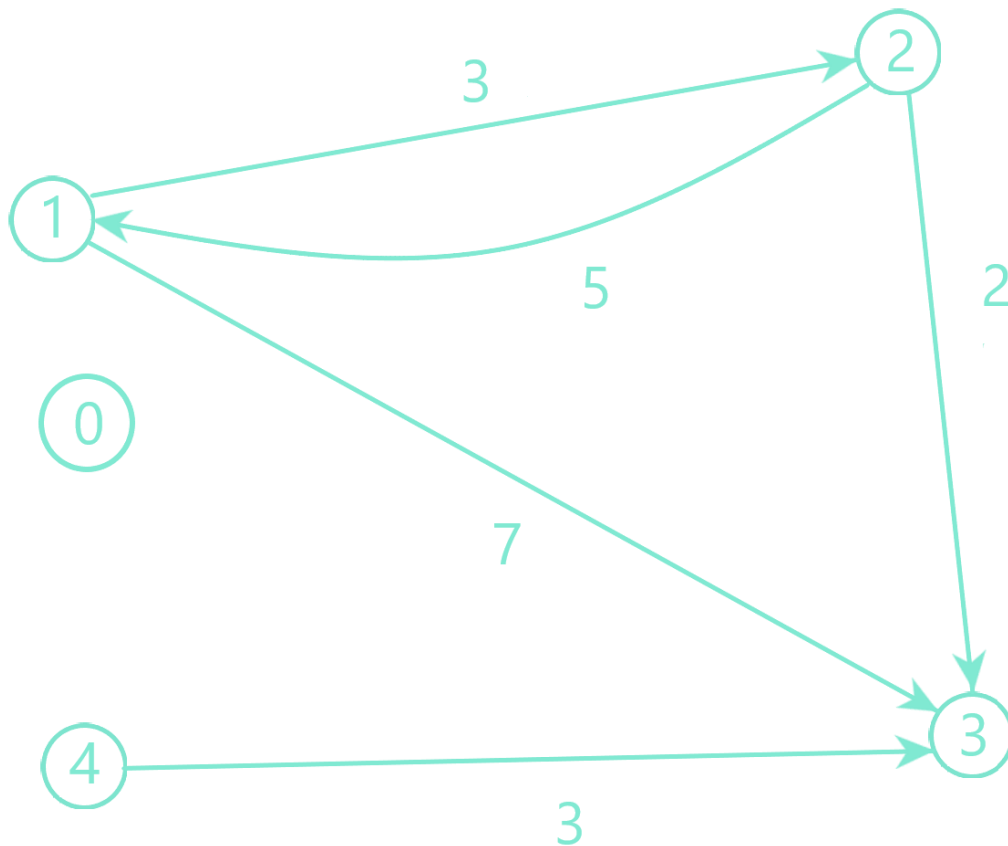
Current: -1

Path: [1, 2, 3, 0]

6

$1 \leftarrow 2 \leftarrow 3 \leftarrow 0$ Length: 6

Second example:



Start is 0 and end is 3

Initial state:

Queue: (0, 3)

Successors: {3: -1}

Distances: {3: 0}

Step 1

Before changes

Queue after change: (0, 3)

Successors: {3: -1}

Distances: {3: 0}

After 1 is processed

Queue after change: (7, 1)

Successors: {3: -1, 1: 3}

Distances: {3: 0, 1: 7}

After 2 is processed

Queue after change: (2, 2) (7, 1)

Successors: {3: -1, 1: 3, 2: 3}

Distances: {3: 0, 1: 7, 2: 2}

After 4 is processed

Queue after change: (2, 2) (3, 4) (7, 1)

Successors: {3: -1, 1: 3, 2: 3, 4: 3}

Distances: {3: 0, 1: 7, 2: 2, 4: 3}

Step 2

Before changes

Queue after change: (2, 2) (3, 4) (7, 1)

Successors: {3: -1, 1: 3, 2: 3, 4: 3}

Distances: {3: 0, 1: 7, 2: 2, 4: 3}

After 1 is processed

Queue after change: (3, 4) (5, 1) (7, 1)

Successors: {3: -1, 1: 2, 2: 3, 4: 3}

Distances: {3: 0, 1: 5, 2: 2, 4: 3}

Step 3

Before changes

Queue after change: (3, 4) (5, 1) (7, 1)

Successors: {3: -1, 1: 2, 2: 3, 4: 3}

Distances: {3: 0, 1: 5, 2: 2, 4: 3}

Step 4

Before changes

Queue after change: (5, 1) (7, 1)

Successors: {3: -1, 1: 2, 2: 3, 4: 3}

Distances: {3: 0, 1: 5, 2: 2, 4: 3}

Step 5

Before changes

Queue after change: (7, 1)

Successors: {3: -1, 1: 2, 2: 3, 4: 3}

Distances: {3: 0, 1: 5, 2: 2, 4: 3}

Initial state:

Path: []

Distance: -1

The start vertex is not accessible