

Solutions Mathematical Foundations for Data Analysis

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1 Chapter 1

1.1 A1.1

Consider the probability table below for the random variables X and Y. One entry is missing, but you should be able to derive it. Then calculate the following values.

1. $\Pr(X = 3 \mid Y = 2) = 0.2$
2. $\Pr(Y = 1) = 0.5$
3. $\Pr(X = 2 \mid Y = 1) = 0.1$
4. $\Pr(X = 2 \mid Y = 1) = \frac{\Pr(X=2 \cap Y=1)}{\Pr(Y=1)} = \frac{0.1}{0.5} = 0.2$

	X = 1	X = 2	X = 3
Y = 1	0.25	0.1	0.15
Y = 2	0.1	0.2	0.2

1.2 A1.2

$$\begin{aligned}
 & E[D] \\
 = & \\
 & E[B + H] \\
 = & \\
 & E[B] \\
 + & \\
 & E[H] \\
 = & \left(\frac{1}{4} * 1 + \frac{1}{4} * 3 + \frac{1}{4} * 4 + \frac{1}{4} * 7\right) + \int_{[-1,4]} f_X(x) dx = \frac{15}{4} + \left[\frac{1}{10}x^2\right]_{-1}^4 = 22.5_{10}
 \end{aligned}$$

1.3 A1.3