

SCHOOL OF BUSINESS, ECONOMICS AND MANAGEMENT

BBA 240 – QUANTITATIVE METHODS

FINAL EXAMINATION FORMLAE AND TABLES

Formula Appendix

Sample mean $\bar{x} = \frac{\sum x}{n}$	$\text{Estimated Median} = L + \frac{(n/2) - cfb}{f_m} \times w$
Population mean $\mu = \frac{\sum x}{N}$	$\text{Estimated Mode} = L + \frac{f_m - f_{m-1}}{(f_m - f_{m-1}) + (f_m - f_{m+1})} \times w$
Sample standard deviation $s = \sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}}$ $s = \sqrt{\frac{SS_x}{n - 1}} \text{ where } SS_x = \sum x^2 - \frac{(\sum x)^2}{n}$	Range = Largest data value - smallest data value
Population standard deviation $\sigma = \sqrt{\frac{\sum (x - \mu)^2}{N}}$	Standard z value $z = \frac{x - \mu}{\sigma}$

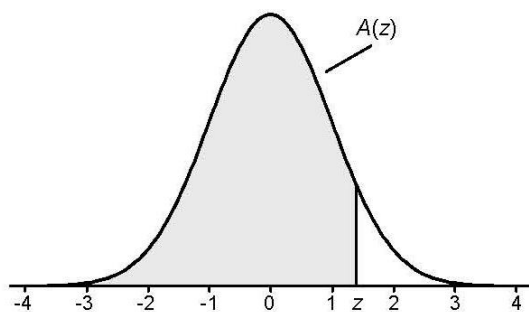
Sample mean for a frequency distribution $\bar{x} = \frac{\sum xf}{n}$	Original x value $x = \mu + z\sigma$
Sample standard deviation for a frequency distribution $s = \sqrt{\frac{\sum (x - \bar{x})^2 f}{n - 1}}$	Central limit theorem $z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}, \quad n \geq 30$
PROBABILITY FORMULAS	
Probability of an event A $P(A) = \frac{f}{n}$ where f = frequency of occurrence of event n = sample size	General addition rule $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$
Probability of the complement of event A $P(A)^c = 1 - P(A)$	Permutation rule $P_{n,r} = \frac{n!}{(n-r)!}$
Multiplication rule for independent events $P(A \text{ and } B) = P(A) \cdot P(B)$	Combination rule $C_{n,r} = \frac{n!}{r!(n-r)!}$
General multiplication rules $P(A \text{ and } B) = P(A) \cdot P(B \text{ given } A)$ $P(A \text{ and } B) = P(B) \cdot P(A \text{ given } B)$	Mean of a discrete probability distribution $\mu = \sum xP(x)$

Addition rule for mutually exclusive events $P(A \text{ or } B) = P(A) + P(B)$	Standard deviation of a discrete probability distribution $\sigma = \sqrt{\sum (x - \mu)^2 P(x)}$
Conditional Probability $P(A B) = \frac{P(A \cap B)}{P(B)}$	Bayes Theorem $P(A_i E) = \frac{P(E \cap A_i)}{P(E)}$ $= \frac{P(A_i) \cdot P(E A_i)}{\sum_{j=1}^n P(A_j) \cdot P(E A_j)}$
Binominal Distribution $p(x = k) = \binom{n}{k} p^k (1 - p)^{n-k}$ $= \binom{n}{k} p^k (q)^{n-k}$ $E(X) = np \quad V(X) = npq(1 - P) = npq$	Poisson distribution $P(X = k) = \frac{e^{-\lambda} \lambda^k}{k!}, \quad k = 0, 1, 2, 3, \dots$ $E(X) = \lambda \quad V(X) = \lambda$
CONFIDENCE INTERVALS	REGRESSION AND CORRELATION
Confidence interval for a mean (large samples) $\bar{x} - z_c \frac{\sigma}{\sqrt{n}} < \mu < \bar{x} + z_c \frac{\sigma}{\sqrt{n}}$	Correlation coefficient $r = \frac{n \sum xy - (\sum x)(\sum y)}{\sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y^2 - (\sum y)^2}}$
Confidence interval for a mean (Small samples) $\bar{x} - t_c \frac{s}{\sqrt{n}} < \mu < \bar{x} + t_c \frac{s}{\sqrt{n}}$	Regression line $\hat{y} = mx + b$

Confidence interval for a proportion (where $np > 5$ and $nq > 5$) $\frac{r}{n} - z_c \sqrt{\frac{\frac{r}{n} \left(1 - \frac{r}{n}\right)}{n}} < p < \frac{r}{n} + z_c \sqrt{\frac{\frac{r}{n} \left(1 - \frac{r}{n}\right)}{n}}$	$m = \frac{n \sum xy - (\sum x)(\sum y)}{n \sum x^2 - (\sum x)^2}$ $b = \bar{y} - m\bar{x} = \frac{\sum y}{n} - m \frac{\sum x}{n}$
Chi Square	Analysis of Variance
Expected Frequencies $E_{r,c} = \frac{(\text{Sum of row } r) \times (\text{Sum of column } c)}{\text{Sample Size}}$	Between-samples sum of squares $SSB = \sum_{i=1}^k n_i (\bar{x}_i - \bar{\bar{x}})^2$
Degrees of freedom $d.f = (r - 1)(c - 1)$	Within-samples sum of squares $SSW = \sum_{i=1}^k \sum_{j=1}^{n_j} (x_{ij} - \bar{x}_i)^2$
Test statistic $\chi^2 = \sum \frac{(O - E)^2}{E}$	Test statistic $F = \frac{MSB}{MSW} \quad df_{\cdot N} = k - 1 \quad df_{\cdot D} = N - k$ $MSB = \frac{SSB}{k-1} \quad MSW = \frac{SSW}{n-k}$

Source of Variation	Degrees of Freedom	Sum of Squares	Mean Square	Value of the Test Statistic
Between	$k - 1$	SSB	MSB	$F = \frac{MSB}{MSW}$
Within	$n - k$	SSW	MSW	
Total	$n - 1$	SST		

Cumulative Standardized Normal Distribution



$A(z)$ is the integral of the standardized normal distribution from $-\infty$ to z (in other words, the area under the curve to the left of z). It gives the probability of a normal random variable not being more than z standard deviations above its mean. Values of z of particular importance:

z	$A(z)$	
1.645	0.9500	Lower limit of right 5% tail
1.960	0.9750	Lower limit of right 2.5% tail
2.326	0.9900	Lower limit of right 1% tail
2.576	0.9950	Lower limit of right 0.5% tail
3.090	0.9990	Lower limit of right 0.1% tail
3.291	0.9995	Lower limit of right 0.05% tail

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998
3.5	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998
3.6	0.9998	0.9998	0.9999							

Table A. 2

T Distribution Table

Table entry for p and C is the critical value t^* with probability p lying to its right and probability C lying between $-t^*$ and t^* .

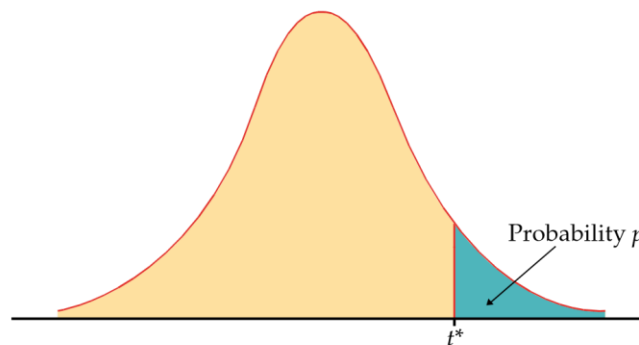


TABLE D

t distribution critical values

df	Upper-tail probability p											
	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.6
2	0.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.60
3	0.765	0.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.92
4	0.741	0.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.610
5	0.727	0.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.869
6	0.718	0.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.959
7	0.711	0.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.408
8	0.706	0.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5.041
9	0.703	0.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.781
10	0.700	0.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.587
11	0.697	0.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.437
12	0.695	0.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318
13	0.694	0.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.221
14	0.692	0.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.140
15	0.691	0.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.073
16	0.690	0.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252	3.686	4.015
17	0.689	0.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965
18	0.688	0.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922
19	0.688	0.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883
20	0.687	0.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850
21	0.686	0.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819
22	0.686	0.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792
23	0.685	0.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
24	0.685	0.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467	3.745
25	0.684	0.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.725
26	0.684	0.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.707
27	0.684	0.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690
28	0.683	0.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.674
29	0.683	0.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.659
30	0.683	0.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	3.030	3.385	3.646
40	0.681	0.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.551
50	0.679	0.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.496
60	0.679	0.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.460
80	0.678	0.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416
100	0.677	0.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390
1000	0.675	0.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300
z^*	0.674	0.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.291
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%
	Confidence level C											

NEGATIVE z Scores

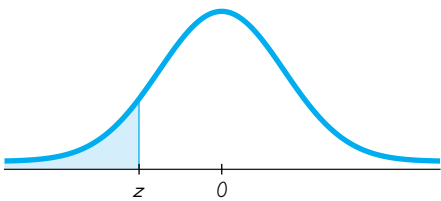


TABLE A-2 Standard Normal (z) Distribution: Cumulative Area from the LEFT										
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
−3.50 and lower	.0001									
−3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
−3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
−3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
−3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
−3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
−2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
−2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
−2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
−2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
−2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	*	.0049
−2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	↑	.0066
−2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089		.0087
−2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116		.0113
−2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150		.0146
−2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192		.0188
−1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244		.0239
−1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307		.0301
−1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384		.0375
−1.6	.0548	.0537	.0526	.0516	.0505	*	.0495	.0485		.0475
−1.5	.0668	.0655	.0643	.0630	.0618	↑	.0606	.0594		.0582
−1.4	.0808	.0793	.0778	.0764	.0749		.0735	.0721		.0708
−1.3	.0968	.0951	.0934	.0918	.0901		.0885	.0869		.0853
−1.2	.1151	.1131	.1112	.1093	.1075		.1056	.1038		.1020
−1.1	.1357	.1335	.1314	.1292	.1271		.1251	.1230		.1210
−1.0	.1587	.1562	.1539	.1515	.1492		.1469	.1446		.1423
−0.9	.1841	.1814	.1788	.1762	.1736		.1711	.1685		.1660
−0.8	.2119	.2090	.2061	.2033	.2005		.1977	.1949		.1922
−0.7	.2420	.2389	.2358	.2327	.2296		.2266	.2236		.2206
−0.6	.2743	.2709	.2676	.2643	.2611		.2578	.2546		.2514
−0.5	.3085	.3050	.3015	.2981	.2946		.2912	.2877		.2843
−0.4	.3446	.3409	.3372	.3336	.3300		.3264	.3228		.3192
−0.3	.3821	.3783	.3745	.3707	.3669		.3632	.3594		.3557
−0.2	.4207	.4168	.4129	.4090	.4052		.4013	.3974		.3936
−0.1	.4602	.4562	.4522	.4483	.4443		.4404	.4364		.4325
−0.0	.5000	.4960	.4920	.4880	.4840		.4801	.4761		.4721

NOTE: For values of z below −3.49, use 0.0001 for the area.

*Use these common values that result from interpolation:

z score	Area
−1.645	0.0500 ←
−2.575	0.0050 ←