

1. $91_{10} \rightarrow C6_{16} = 289$

$$\begin{array}{r} 45 \text{ R1} \\ 2 \overline{) 91} \\ \underline{-81} \\ 10 \\ \underline{-10} \\ 0 \end{array}$$

$$\begin{array}{r} 22 \text{ R1} \\ 2 \overline{) 45} \\ \underline{-44} \\ 1 \\ \underline{-2} \\ 1 \end{array}$$

$1011011 \leftarrow 91_{10} \text{ to binary}$

$$\begin{array}{r} 11 \text{ R0} \\ 2 \overline{) 22} \\ \underline{-22} \\ 0 \end{array}$$

$$\begin{array}{r} 5 \text{ R1} \\ 2 \overline{) 11} \\ \underline{-10} \\ 1 \end{array}$$

$$\begin{array}{r} 2 \text{ R1} \\ 2 \overline{) 5} \\ \underline{-4} \\ 1 \end{array}$$

$$\begin{array}{r} 1 \text{ R0} \\ 2 \overline{) 2} \\ \underline{-2} \\ 0 \end{array}$$

$$\begin{array}{r} 0 \text{ R1} \\ 2 \overline{) 1} \\ \underline{-2} \\ 1 \end{array}$$

0 1 2 3 4 5 6 7 8 9 A B C D E F

$C6 = (12 \times 16^1) + (6 \times 16^0) = 198 \leftarrow C6_{16} \text{ to decimal}$

$$\begin{array}{r} 49 \text{ R1} \\ 2 \overline{) 99} \\ \underline{-98} \\ 1 \end{array}$$

$$\begin{array}{r} 99 \text{ R0} \\ 2 \overline{) 198} \\ \underline{-198} \\ 0 \end{array}$$

$11000110 \leftarrow C6_{16} \text{ to binary}$

$$\begin{array}{r} 24 \text{ R1} \\ 2 \overline{) 49} \\ \underline{-48} \\ 1 \end{array}$$

$$\begin{array}{r} 12 \text{ R0} \\ 2 \overline{) 24} \\ \underline{-24} \\ 0 \end{array}$$

$$\begin{array}{r} 6 \text{ R0} \\ 2 \overline{) 12} \\ \underline{-12} \\ 0 \end{array}$$

$$\begin{array}{r} 3 \text{ R0} \\ 2 \overline{) 6} \\ \underline{-6} \\ 0 \end{array}$$

$$\begin{array}{r} 1 \text{ R1} \\ 2 \overline{) 3} \\ \underline{-2} \\ 1 \end{array}$$

$$\begin{array}{r} 0 \text{ R1} \\ 2 \overline{) 1} \\ \underline{-2} \\ 1 \end{array}$$

$$\begin{array}{r} 11000110 \\ + 1011011 \\ \hline 110010001 \end{array}$$

$1 + 32 + 256 = 289$

2. $11_8 - 11_{10}$

$11_8 \rightarrow 0 \ 1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7$

$(1 \times 8^1) + (1 \times 8^0) = 9 \leftarrow 11_8 \text{ to decimal}$

$1001 \leftarrow 11_8 \text{ to binary}$

-11_{10} to binary \rightarrow

$1011 \rightarrow 0100 \rightarrow 0101$

$$\begin{array}{r} 1 \\ 1001 \\ + 0101 \\ \hline 1110 \end{array}$$

$\rightarrow 0001 + 1 \rightarrow$ signed 0010

$\rightarrow \boxed{-2}$

3. $12.3125_{10} + 0110_{12Q2} = 13.8125$

\downarrow

$\rightarrow 1.5$ in decimal

$0.3125 \times 2 = 0.625 \rightarrow 1100.0101$ $\rightarrow 12.3125_{10}$ in binary.

$0.625 \times 2 = 1.25$

$0.25 \times 2 = 0.50$

$.50 \times 2 = 1.00$

$$\begin{array}{r} 1100.0101 \\ + 0110.0000 \\ \hline 110010.0101 \\ 01101.1101 \end{array}$$

$= \boxed{13.8125}$

4. $5.75_{10} + (-7.125_{10}) \rightarrow 12Q3$

\downarrow

101.110

$111.001 \rightarrow 000.111 = -7.125_{10}$

$$\begin{array}{r} 101.110 \\ + 000.111 \\ \hline 110.101 \end{array}$$

$\rightarrow 001.011 = \boxed{-1.375}$

-1.375

5. $9_{10} \cdot 3_{10}$

\swarrow \searrow
 1001 0011

$$\begin{array}{r}
 1001 \\
 \times 0011 \\
 \hline
 1001 \\
 0000 \\
 0000 \\
 \hline
 00011011 = \boxed{27_{10}}
 \end{array}$$

6. $(-5)_{10} \cdot (-6)_{10}$

$0101 \rightarrow 1010 + 1 \Rightarrow 1011 \rightarrow -5$ in binary.
 $0110 \rightarrow 1001 + 1 \Rightarrow 1010 \rightarrow -6$ in binary.

$$\begin{array}{r}
 0101 \\
 0110 \\
 \hline
 0000 \\
 0101 \\
 0101 \\
 0000 \\
 \hline
 0011110
 \end{array}$$

$0011110 \rightarrow$ since signs were same at the start, this number is positive.

$\boxed{30_{10}}$

7. $9.5_{10} \cdot 2.625_{10}$

\downarrow \downarrow
 1001.100 0010.101

$$\begin{array}{r}
 1001.100 \\
 \times 0010.101 \\
 \hline
 1001100 \\
 0000000 \\
 1001100 \\
 0000000 \\
 1001100 \\
 0000000 \\
 0000000 \\
 \hline
 0011000.11100
 \end{array}$$

$= \boxed{24.9375_{10}}$

$$8. \quad -1.25_{10} \cdot 3.5_{10} = -4.375$$

01.01 \rightarrow 10.10 + 1 \rightarrow 10.11 \rightarrow -1.25_{10} in binary.

11.10 \rightarrow 3.5_{10} in binary.

$$\begin{array}{r} 01.01 \\ 11.10 \\ \hline .0000 \\ 0.101 \\ 01.01 \\ 010.1 \end{array}$$

$$\text{signed } 100.0110 = \boxed{-4.375_{10}}$$