

Data:

- $\lambda = 100 \text{ (req/sec)}$ ;
- $B_{ISP} = 1 \text{ Gbps}$ ; (full duplex  $\Rightarrow$   $\longleftrightarrow$ )
- $L = 100 \text{ (usec/pkt)}$  { router latency }
- $F = 100 \text{ Kbytes} = 100 \cdot 1024 \text{ bytes} = 100000 \text{ bytes}$  { file dimension }
- $R = 300 \text{ bytes}$  { Http request }
- $S_{CPU/PL} = 1 \text{ (msec)}$ ;
- $P_{hit} = 60\%$       |       $P_{miss} = 40\%$ 
  - $S_{CPU/AL}^{hit} = 5 \text{ (ms)}$
  - $S_{CPU/AL}^{miss} = 10 \text{ (ms)}$
- $S_{Disk/AL} = 5 \text{ (msec} \cdot 10 \text{ Kbytes}) \Rightarrow$  To serve the 100 Kbytes (file dimension)  $\Rightarrow V_{Disk/AL} = 10$
- $S_{CPU/FS} = 10 \text{ (msec)}$
- $S_{Disk/FS} = 3 \text{ (msec} \cdot 10 \text{ Kbytes}) \Rightarrow$  To serve the 100 Kbytes (file dimension)  $\Rightarrow V_{Disk/FS} = 10$
- $B_{LAN1} = 1 \text{ GBS}$
- $B_{LAN2} = 1 \text{ GBS}$
- $B_{LAN3} = 0,5 \text{ GBs}$

Being a multiclass open QNs, we use these formulas:

$\left\{ \begin{array}{l} i = \text{queue identification} \\ r = \text{layer identification} \end{array} \right.$

$$\bullet D_{i,r} = \frac{P_{hit} [ S_{i,r}^{\text{hit}} \cdot V_{i,r}^{\text{hit}} ] + P_{miss} [ S_{i,r}^{\text{miss}} \cdot V_{i,r}^{\text{miss}} ]}{n_{i,r}} \quad \text{where } n_{i,r} = \text{n}^{\circ} \text{ of } i\text{-th components for the r-th layer}$$

general formula

$$\bullet U_{i,r} = \lambda \cdot D_{i,r} \quad (\text{utilization factor})$$

$$\bullet R'_{i,r} = \frac{D_{i,r}}{1 - U_{i,r}} \quad (\text{residence time})$$

$$\bullet R_r = \sum_{i=1}^k R'_{i,r} \quad \text{where } k = \text{n}^{\circ} \text{ of queues} \quad (\text{response time})$$

Thus:

$$- D_{CPU/PL} = \frac{S_{CPU/PL} \cdot V_{CPU/PL}}{n_{CPU/PL}} = \frac{1 \text{ (ms)} \cdot 1}{2} = 0,5 \text{ (ms)} = 0,0005 \text{ (s)}$$

$$- D_{CPU/AL} = \frac{P_{hit} [ S_{CPU/AL}^{\text{hit}} \cdot V_{CPU/AL}^{\text{hit}} ] + P_{miss} [ S_{CPU/AL}^{\text{miss}} \cdot V_{CPU/AL}^{\text{miss}} ]}{n_{CPU/AL}} = \frac{0,6 [ 5 \text{ (ms)} \cdot 1 ] + 0,4 [ 10 \text{ (ms)} \cdot 1 ]}{5} = 1,4 \text{ (ms)} = 0,0014 \text{ (s)}$$

$P_{miss} [ S_{CPU/AL}^{\text{miss}} \cdot V_{CPU/AL}^{\text{miss}} ] = 0,4 \cdot 10 \text{ (ms)} = 4 \text{ (ms)}$

is independent from the fact that 3 have a hit or a miss.

$$D_{DISK/AL} = \frac{P_{hit} [ S_{DISK/AL} \cdot V_{DISK/AL} ] + \cancel{P_{miss} [ S_{DISK/AL} \cdot V_{DISK/AL} ]}}{n_{DISK/AL}} = \frac{0,6 [ 5 \text{ (ms)} \cdot 10 ]}{5} = 6 \text{ (ms)} = 0,006 \text{ (s)}$$

$$- D_{CPU/FS} = \frac{\emptyset + P_{miss} [ S_{CPU/FS} \cdot V_{CPU/FS} ]}{n_{CPU/FS}} = \frac{0,4 [ 10 \text{ (ms)} \cdot 1 ]}{1} = 4 \text{ (ms)} = 0,004 \text{ (s)}$$

$$D_{DISK/FS} = \frac{\emptyset + P_{miss} [ S_{DISK/FS} \cdot V_{DISK/FS} ]}{n_{DISK/FS}} = \frac{0,4 [ 3 \text{ (ms)} \cdot 10 ]}{10} = \frac{1,2}{10} \text{ (ms)} = 0,0012 \text{ (s)}$$

$$- U_{CPU/PL} = \lambda \cdot D_{CPU/PL} = 100 \left( \frac{\text{req}}{\text{sec}} \right) \cdot 0,0005 \text{ (sec)} = 0,05$$

$$- U_{CPU/AL} = \lambda \cdot D_{CPU/AL} = 100 \cdot 0,0014 = 0,14$$

$$U_{DISK/AL} = \lambda \cdot D_{DISK/AL} = 100 \cdot 0,006 = 0,6$$

$$- U_{CPU/FS} = \lambda \cdot D_{CPU/FS} = 100 \cdot 0,004 = 0,4$$

$$U_{DISK/FS} = \lambda \cdot D_{DISK/FS} = 100 \cdot 0,0012 = 0,12$$

$$- R'_{CPU/PL} = \frac{D_{CPU/PL}}{1 - U_{CPU/PL}} = \frac{0,5 \text{ (ms)}}{0,95} = 0,53 \text{ (ms)}$$

$$- R'_{CPU/AL} = \frac{D_{CPU/AL}}{1 - U_{CPU/AL}} =$$

$$R'_{DISK/AL} = \frac{D_{DISK/AL}}{1 - U_{DISK/AL}} =$$

$$- R'_{CPU/FS} = \frac{D_{CPU/FS}}{1 - U_{CPU/FS}} =$$

$$R'_{DISK/FS} = \frac{D_{DISK/FS}}{1 - U_{DISK/FS}} =$$

Regarding the networks: Hypothesis: TCP doesn't know the local MTU of the LAN.

**REQUEST**

$$\# \text{Segment} = \left\lceil \frac{R}{\text{MTU}_{\text{TCP}}} \right\rceil = \left\lceil \frac{300}{65,515} \right\rceil = 1;$$

$$\# \text{datagram} = \left\lceil \frac{R + \# \text{seq}(\text{TCP overhead})}{\text{MSS}} \right\rceil = \left\lceil \frac{300 + (1 \cdot 20)}{1480} \right\rceil = \# \text{frame} \quad \left\{ \begin{array}{l} \text{MSS} = \text{MTU}_{\text{ETH}} - \text{IP overhead} \\ = 1500 - 20 \end{array} \right\}$$

$$\begin{aligned} \text{Overhead} &= \# \text{segment} (\text{TCP overhead}) + \# \text{datagram} (\text{IP overhead} + \text{Eth overhead}) = \\ &= (1 \cdot 20) + 1 (20 + 18) = 58 \text{ bytes} \end{aligned}$$

$$S_{\text{ISP}}^{\text{req}} = \frac{8 (R + \text{Overhead})}{B_{\text{ISP}}} = \frac{2864 \cdot \frac{(\text{bit})}{1 \cdot 10^9 \frac{\text{bit}}{\text{sec}}}}{1 \cdot 10^9 \frac{\text{bit}}{\text{sec}}} = 2864 \cdot 10^{-9} \text{ (sec)} = 0,002864 \text{ (ms)}$$

$$S_{\text{rout}}^{\text{req}} = \# \text{datagram} \cdot L = 1 \cdot 100 \frac{(\mu\text{sec})}{\frac{(\text{PKT})}{\text{PKT}}} = 100 \text{ } \mu\text{sec} = 0,1 \text{ (ms)}$$

$$S_{\text{LAN1}}^{\text{req}} = \frac{R + \text{Overhead}}{B_{\text{LAN1}}} = \frac{358 \text{ (byte)}}{1 \cdot 10^9 \frac{\text{byte}}{\text{sec}}} = 358 \cdot 10^{-9} \text{ (sec)} = 0,000358 \text{ (ms)} = S_{\text{LAN2}}^{\text{req}}$$

$$\begin{aligned} S_{\text{LAN3}}^{\text{req}} &= P_{\text{MSS}} \left[ \frac{R + \text{Overhead}}{B_{\text{LAN3}}} \right] = 0,4 \left[ \frac{358}{0,5 \cdot 10^9} \right] = \\ &= [716 \cdot 10^{-9} \text{ (s)}] \cdot 0,4 = 286,4 \cdot 10^{-9} \text{ (s)} = \end{aligned}$$

$$\# \text{Segment} = \left\lceil \frac{F}{\text{MTU}_{\text{TCP}}} \right\rceil = \left\lceil \frac{100'000}{65,515} \right\rceil = 2; \quad = 0,0002864 \text{ (ms)}$$

$$\# \text{datagram} = \# \text{frame} = \left\lceil \frac{F + \# \text{segment}(\text{TCP overhead})}{\text{MSS}} \right\rceil = \left\lceil \frac{100'000 + (2 \cdot 20)}{1480} \right\rceil = 68$$

$$\begin{aligned} \text{Overhead} &= \# \text{segment} (\text{TCP overhead}) + \# \text{datagram} (\text{IP overhead} + \text{Eth overhead}) = (2 \cdot 20) + 68(20 + 18) \text{ s} \\ &\approx 2624 \text{ (byte)} \end{aligned}$$

$$S_{\text{LAN3}}^{\text{rep}} = \left[ \frac{F + \text{Overhead}}{B_{\text{LAN3}}} \right] \cdot 10\% = \left[ \frac{102'624 \text{ (sec)}}{0,5 \cdot 10^9} \right] \cdot 0,1 = [205'248 \cdot 10^{-9} \text{ (sec)}] \cdot 0,1 =$$

$$= [0,205 \text{ (ms)}] \cdot 0,1 = 0,0205 \text{ (msec)}$$

$$S_{\text{LAN2}}^{\text{rep}} = \left[ \frac{F + \text{Overhead}}{B_{\text{LAN2}}} \right] \cdot 60\% = \left[ \frac{102'624}{1 \cdot 10^9} \right] \cdot 0,6 = 61'576,4 \cdot 10^{-9} \text{ (s)} = 0,0615764 \text{ (ms)}$$

=

$$S_{\text{LAN1}}^{\text{rep}} = \frac{F + \text{Overhead}}{B_{\text{LAN1}}} = \frac{102'624}{1 \cdot 10^9} = 102'624 \cdot 10^{-9} \text{ (sec)} = 0,10 \text{ (msec)}.$$

$$S_{\text{rout}}^{\text{rep}} = \# \text{datagram} \cdot L = 68 \cdot 100 = 6800 \text{ } \mu\text{sec} = 6,8 \text{ (ms)}$$

$$S_{\text{ISP}}^{\text{rep}} = \frac{(F + \text{Overhead}) 8}{B_{\text{ISP}}} = \frac{820'992}{1 \cdot 10^9} \frac{(\text{bit})}{\frac{(\text{bit})}{\text{sec}}} = 820'992 \cdot 10^{-9} \text{ (sec)} = 0,82 \text{ (ms)}$$

## HANDSHAKING

$$\# \text{segment} = \# \text{datagram} = \# \text{frame} = 6$$

$$\text{Overhead} = \# \text{frame} (\text{TCPoverhead} + \text{IPoverhead} + \text{Ethernetoverhead}) = 6 (20 + 20 + 18) = 348 \text{ (byte)}$$

$$S_{\text{ISP}}^{\text{hs}} = \frac{(\# \text{Overhead}) 8}{B_{\text{ISP}}} = \frac{2784}{1 \cdot 10^9} \text{ (sec)} = 2784 \cdot 10^{-9} \text{ (sec)} = 0,0028 \text{ (msec)}$$

$$S_{\text{root}}^{\text{hs}} = \# \text{datagram} \cdot L = 6 \cdot 100 = 600 \text{ (μsec)} = 0,6 \text{ (ms)}$$

$$S_{\text{LAN1}}^{\text{hs}} = \frac{0 + \text{Overhead}}{B_{\text{LAN1}}} = \frac{348}{1 \cdot 10^9} \text{ (sec)} = 348 \cdot 10^{-9} \text{ (sec)} = 0,00035 \text{ (ms)}$$

$S_{\text{LAN2}}^{\text{hs}}$  ?  
 $S_{\text{LAN3}}^{\text{hs}}$  ?

Then:

$$D_{\text{LAN1}} = (S_{\text{LAN1}}^{\text{hs}} + S_{\text{LAN1}}^{\text{req}} + S_{\text{LAN1}}^{\text{resp}}) \cdot 1 =$$

$$U_i = \lambda \cdot D_i$$

$$R_i^1 = \frac{D_i}{1 - U_i}$$

$$D_{\text{ISP}} = (S_{\text{ISP}}^{\text{hs}} + S_{\text{ISP}}^{\text{req}} + S_{\text{ISP}}^{\text{resp}}) \cdot 1 \text{ s}$$

$$D_{\text{root}} = (S_{\text{root}}^{\text{hs}} + S_{\text{root}}^{\text{req}} + S_{\text{root}}^{\text{resp}}) \cdot 1 \text{ s}$$

$$D_{\text{LAN2}} = S_{\text{LAN2}}^{\text{req}} + \left\{ [S_{\text{LAN2}}^{\text{resp}} \cdot 1] 0,6 + 0,4 [S_{\text{LAN2}}^{\text{resp}} \cdot 2] \right\} + S_{\text{LAN2}}^{\text{hs}}$$

$$D_{\text{LAN3}} = (S_{\text{LAN3}}^{\text{req}} + S_{\text{LAN3}}^{\text{resp}} + S_{\text{LAN3}}^{\text{hs}}) 0,4$$

Finally:

$$1) R_{PL} = R'_{CPU/PL}$$

$$R_{AL} = R'_{CPU/AL} + R'_{DISK/AL}$$

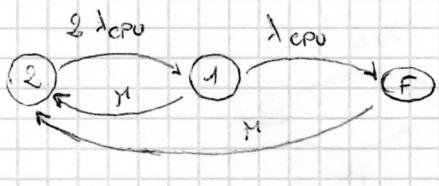
$$R_{FS} = R'_{CPU/FS} + R'_{DISK/FS}$$

$$R_{tot} = R_{PL} + R_{AL} + R_{FS} + R_{ISP} + R_{root} + R_{LAN1} + R_{LAN2} + R_{LAN3} \quad (\text{average response time})$$

The bottleneck is the maximum of the ~~the~~ response time

$$2) A_i = \frac{\text{MTTF}}{\text{MTTF} + \text{MTTR}} \quad \text{where MTTF} = \frac{1}{\lambda_i} \quad \text{and MTTR} = \frac{1}{\mu}$$

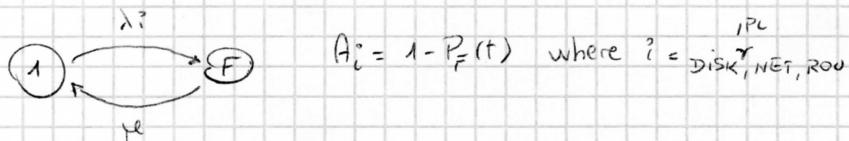
- CPU/PC (RAID 1)



$$\left\{ \begin{array}{l} P_2(t) = \phi = -P_2(2\lambda_{CPU}) + \mu(P_1 + P_F) \\ P_1(t) = \phi = -P_1(\mu + \lambda_{CPU}) + P_2(2\lambda_{CPU}) \\ P_F(t) = \phi = -P_F(\mu) + P_1(\lambda_{CPU}) \\ P_2(t) + P_1(t) + P_F(t) = 1 ; \quad P_2(\phi) = 1 \end{array} \right.$$

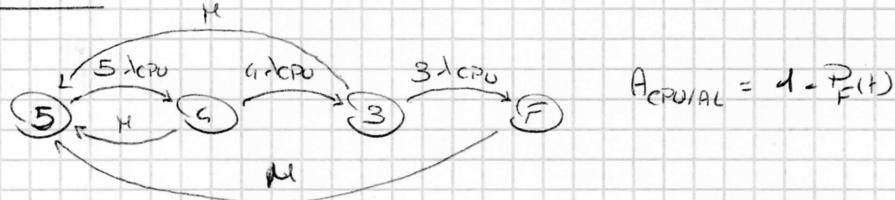
$$A_{\text{CPU/PC}}(t) = 1 - P_F(t)$$

- DISK/PC, ROUTER, LAN (1/2/3), DISK/AC, CPU/FS



$$A_{\text{PC}}(t) = A_{\text{CPU/PC}}(t) \cdot A_{\text{DISK/PC}}(t) \cdot A_{\text{LAN}(1)}(t)$$

- CPU/AC



$$A_{\text{AC}}(t) = A_{\text{CPU/AC}}(t) \cdot A_{\text{DISK/AC}}(t) \cdot A_{\text{LAN}2}(t)$$

- RAID (single pair)



$$A_{\text{FS}}(t) = A_{\text{CPU/FS}}(t) \cdot A_{\text{RAID}}(t) \cdot A_{\text{LAN}3}(t)$$

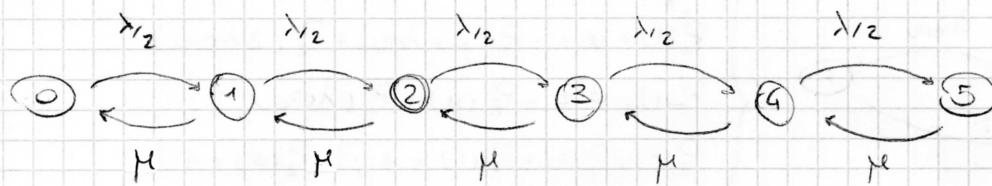
$$A_{\text{pair}} = 1 - P_F(t) \Rightarrow A_{\text{RAID}} = [A_{\text{pair}}]^5$$

$$\text{Finally : } A_{\text{system}}(t) = A_{\text{router}}(t) \cdot A_{\text{PC}}(t) \cdot A_{\text{AC}}(t) \cdot A_{\text{FS}}(t)$$

3) About the presentation layer, we have a requests queue of dimension 5.

So, hypothesize that the requests load is equally distributed on the CPU/PCs (that are 2).

So, the STD (State Transaction Diagram) is:



$$\text{Where } \mu = \frac{1}{S_{CPU/PC}} = \frac{1}{0.001 \text{ (sec)}} = 1000 \text{ (req/sec)}$$

Flow-in = Flow-out principle:

$$\left\{ \begin{array}{l} p_0 \cdot \frac{\lambda}{2} = p_1 \cdot \mu \\ p_1 \cdot \frac{\lambda}{2} = p_2 \cdot \mu \\ p_2 \cdot \frac{\lambda}{2} = p_3 \cdot \mu \\ p_3 \cdot \frac{\lambda}{2} = p_4 \cdot \mu \\ p_4 \cdot \frac{\lambda}{2} = p_0 \cdot \mu \\ \sum_{i=0}^4 p_i = 1 \end{array} \right.$$

About the single node:

$$X = \sum_{i=1}^5 p_i \cdot \mu ; \quad (\text{average throughput of a single node})$$

$$N = \sum_{i=0}^5 p_i \cdot i ; \quad (\text{average n° of requests in a single node}).$$

$$R = \frac{N}{X} ; \quad (\text{average response time for a single node}).$$

About ~~the~~ both nodes:

$$\bar{R} = R ; \quad (\text{average response time for the 2 computing nodes})$$

$$\text{Fraction of requests loss} = \frac{\lambda - \bar{X}}{\lambda} \quad \text{where } \bar{X} = 2 \cdot X \quad (\text{average throughput for the 2 computing nodes})$$