

Esercizio u.3

Web service 50 requests per second

Workload is equally distributed across

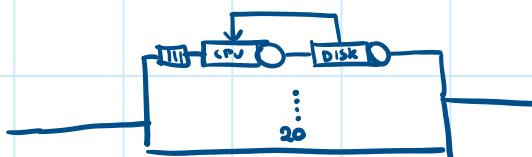
Max concurrent requests is 4

10 msec

Requests require 8 CPU msec and 5 disks read

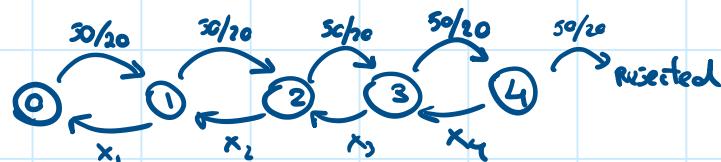
Average request service time? Throughput? Percentage of rejected requests?

Performance improvement with cache (access time of 100 msec) but 70%?



$$S_{CPU} = 8 \text{ msec}$$

$$D_{Disk} = 50 \text{ msec} = \sqrt{V_i} \cdot S_{Disk}$$



Caso 1: (u=1)

$$R_{CPU_1} = D_{CPU} = 8 \text{ msec}$$

$$R_{Disk_1} = D_{Disk} = 50 \text{ msec}$$

$$R_{TOT_1} = 58 \text{ msec}$$

$$x(1) = \frac{1}{R_{TOT_1}}$$

$$N_{CPU_1} = R_{CPU_1} \cdot X_0(1) = 0,14$$

$$N_{Disk} = R_{Disk_1} \cdot X_0(1) = 0,86$$

Caso 2 (u=2):

$$R_{CPU_2} = D_{CPU_2} = 16 \text{ msec}$$

$$R_{Disk_2} = 73$$

$$R_{TOT_2} = 102$$

$$x(2) = \frac{2}{R_{TOT_2}}$$

$$\parallel D_{CPU}(1 + N_{CPU_{i-1}})$$

$$\parallel 50 (1 + N_{CPU_{i-1}})$$

$$N_{CPU_2} = R_{CPU_2} \cdot X(2) = 0,18$$

$$N_{Disk} = R_{Disk_2} \cdot X(2) = 1,82$$

Caso u.3

$$R_{CPU_3} = 9,44$$

$$R_{Disk_3} = 141$$

$$R_{TOT_3} = 150,44$$

$$X(3) = 19,94$$

$$N_{CPU_2} = 0,18$$

$$N_{Disk_2} = 2,81$$

Caso u.4

$$R_{CPU_4} = 0,504 \text{ msec}$$

$$R_{Disk_4} = 130 \text{ msec}$$

$$R_{TOT_4} = 200,004 \text{ msec}$$

$$X(4) = 19,93 \text{ msec}$$

$$N_{CPU_4} = 0,19$$

$$N_{Disk} = 3,81$$

$$\begin{cases} P_0 \cdot \frac{5}{2} = P_1 \cdot X_0 \\ P_1 \cdot \frac{5}{2} = P_2 \cdot X_0 \end{cases}$$

$$P_1 = \frac{P_0 \cdot \frac{5}{2}}{X_0(1)}$$

$$P_0 \left[1 + \frac{2.5}{R_{CPU}} \dots \right]$$

$$\left\{ \begin{array}{l} P_1 \cdot \frac{5}{2} = P_2 \cdot X_{02} \\ P_3 \cdot \frac{5}{2} = P_3 \cdot X_{03} \\ P_4 \cdot \frac{5}{2} = P_4 \cdot X_{04} \\ P_1 + P_2 + P_3 + P_4 + P_0 = 1 \end{array} \right.$$

$$P_2 = \frac{X_0(1)}{P_1 \cdot \frac{5}{2}}$$

$$P_3 = \frac{P_2 \cdot \frac{5}{2}}{X_0(2)}$$

$$P_4 = \frac{P_3 \cdot \frac{5}{2}}{X_0(3)}$$

$$P_4 = \frac{P_3 \cdot \frac{5}{2}}{X_0(4)}$$

P_0 è costante

$$\text{Probabilità Loss} = 1 - (P_0 + P_1 + P_2 + P_3 + P_4)$$

$$\text{Throughput media} = X(1) \cdot P_1 + X(2) \cdot P_2 + X(3) \cdot P_3 + X(4) \cdot P_4$$

$$\text{Average response time } \frac{N}{R} = \frac{P_1 \cdot 1 + P_2 \cdot 2 + P_3 \cdot 3 + P_4 \cdot 4}{P_1 \cdot X(0) + P_2 \cdot X(2) + P_3 \cdot X(3) + P_4 \cdot X(4)} = \frac{\bar{N}}{2.4}$$

Considering cache

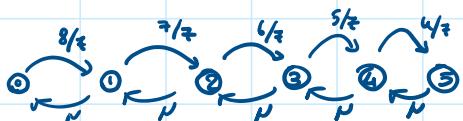
$$R_{disk,i} = P_{miss} (D_{disk} + D_{cache}) + (1 - P_{miss}) (D_{cache}) [1 + u_{i-1}]$$

Esercizio n.1

Server composed of a single unit with user 5 users in queue, limited 8 users

$$\lambda = 30 \text{ sec}$$

$$S = 20 \text{ sec}$$



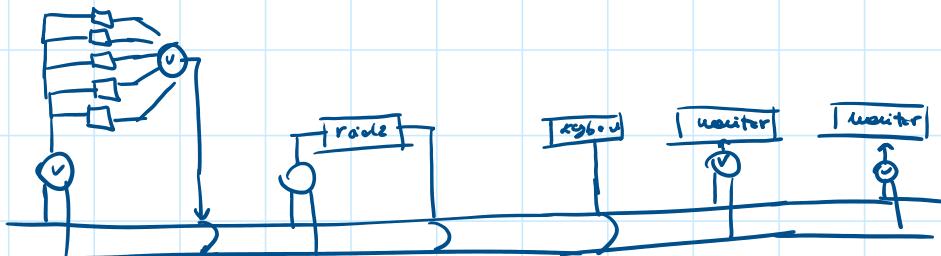
$$N = \frac{1}{\lambda} = \frac{1}{30} = 0.0333$$

$$\begin{cases} P_0 \frac{\lambda}{\mu} = P_1 \mu \\ P_1 \frac{\lambda}{\mu} = P_2 \mu \\ P_2 \frac{\lambda}{\mu} = P_3 \mu \\ P_3 \frac{\lambda}{\mu} = P_4 \mu \\ P_4 \frac{\lambda}{\mu} = P_5 \mu \\ P_1 + P_2 + P_3 + P_4 + P_5 = 1 \end{cases} \Rightarrow \begin{cases} P_1 = 3,95 \cdot 10^{-5} \\ P_2 = 18,43 \cdot 10^{-5} \\ P_3 = 73,73 \cdot 10^{-5} \\ P_4 = 215,77 \cdot 10^{-5} \\ P_5 = 655,40 \cdot 10^{-5} \end{cases} \quad P_0 = 0,000742$$

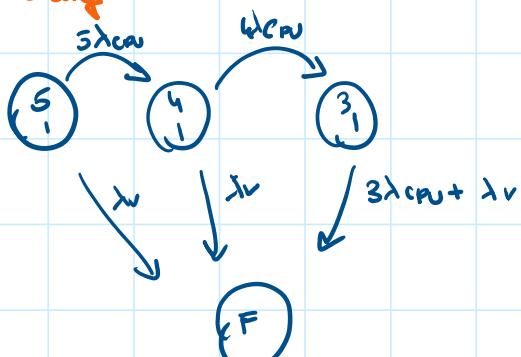
$$\bar{X} = \sum P_i \cdot M_i = P_1 \cdot M_1 + P_2 \cdot M_2 + P_3 \cdot M_3 + P_4 \cdot M_4 + P_5 \cdot M_5 = 49,85 \text{ riduzione/sec}$$

$$\bar{N} = \sum_{i=1}^5 i \cdot P_i \quad R = \frac{\bar{N}}{\bar{X}}$$

Esercizio 1



Reliability



$$\dot{P}_{S,1}(t) = P_{S,1}(t) \cdot (-5\lambda_{CPU} - \lambda_v)$$

$$\dot{P}_{4,1}(t) = P_{4,1}(t) \cdot (-4\lambda_{CPU} - \lambda_v) + P_{S,1}(t) \cdot 5\lambda_{CPU}$$

$$\dot{P}_{3,1}(t) = P_{3,1}(t) \cdot (-3\lambda_{CPU} - \lambda_v) + P_{4,1}(t) \cdot 4\lambda_{CPU}$$

$$\dot{P}_F(t) = -\lambda_v (P_{S,1}(t) + P_{4,1}(t) + P_{3,1}(t)) - 3\lambda_{CPU} P_{3,1}(t)$$

$$P_{S,1}(t) + P_{4,1}(t) + P_{3,1}(t) + P_F(t) = 1$$

$$P_{S,1}(0) = 1$$

$$R_{CPU} = 1 - P_F(t) = P_{S,1}(t) + P_{4,1}(t) + P_{3,1}(t)$$

Keyboard - Printer - Monitor



$$\dot{P}_1(t) = P_1(t) \cdot (-\lambda_i)$$

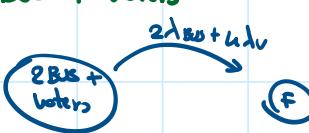
$$P_1(t) = P_1(t) \cdot \lambda_i$$

$$P_1(t) + P_F(t) = 1$$

$$P_1(0) = 1$$

$$R_{KPM} = 1 - P_F(t) = P_1(t)$$

Bus + Voters



$$R_{BSV} = 1 - P_F(t) = P_{BSV}(t)$$

$$\dot{P}_{BSV}(t) = P_{BSV}(t) \cdot (-2\lambda_{BS} - \lambda_v)$$

$$P_0(t) = 1$$

$$R_k P_k = 1 - P_F(t) = P_i(t)$$

Raid



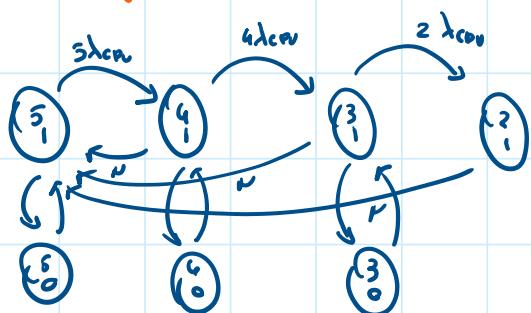
Availability: $\prod R_i$

$$\dot{P}_7(t) = -\lambda_{\text{disk}} \cdot P_7(t)$$

$$P'_6(t) = +\lambda_{\text{disk}} P_7(t) - 6\lambda_{\text{disk}} P_6$$

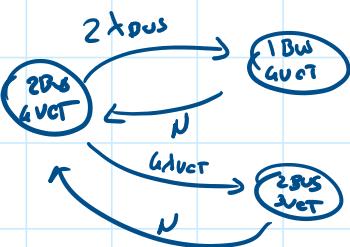
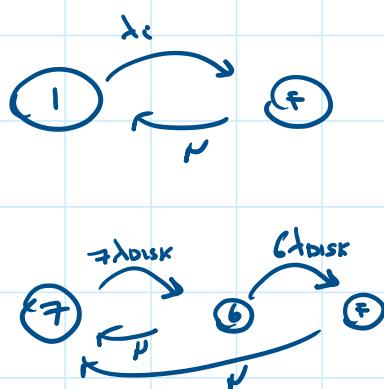
$$P'_F(t) = 6\lambda_{\text{disk}} P_6(t)$$

Availability



$$P_{S,1}(t) = -P_{S,1}(t)(5\lambda_{\text{cpu}} + \lambda_v) + \lambda(P_{S,0}(t) + P_{U,1}(t) + P_{3,1}(t) + P_{2,1}(t))$$

:



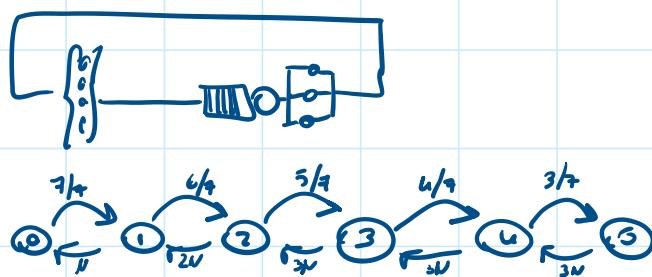
Availability totale:
 $\prod_i A_i$

Safety:

Se una segnale va con posso

Esercizio 11.3

Response time, throughput, probability of loss?



$$\left\{ \begin{array}{l} P_0 \frac{7}{4} = P_1 \cdot 4 \\ P_1 \frac{6}{4} = P_2 \cdot 4 \\ P_2 \frac{5}{4} = P_3 \cdot 4 \\ P_3 \frac{4}{4} = P_4 \cdot 4 \\ P_4 \frac{3}{4} = P_5 \cdot 4 \\ P_0 + P_1 + P_2 + P_3 + P_4 + P_5 = 1 \end{array} \right. \Rightarrow \begin{array}{l} P_0 = 0,054 \\ P_1 = 0,183 \\ P_2 = 0,2835 \\ P_3 = 0,23625 \\ P_4 = 0,1575 \\ P_5 = 0,07875 \end{array}$$

$$\bar{x} = \sum_{i=1}^5 P_i \cdot u_i; \quad \text{Il throughput medio}$$

$$\bar{N} = \sum i \cdot P_i \quad \text{Il numero di utenti medi}$$

Esercizio 11.3

100 requests x secondi

4 identical servers (CPU+RAM)

Fileserver: CPU + 8 disks **connected with 8 channels**

connected with Router (no delay)

File dimension: 100 kB/s

Request: 500 bytes

$$D_{CPU} = 5 \text{ micros (lat)}$$

$$D_{CPU} = 10 \text{ micros} \quad \text{HTTP} = 1000 \text{ hours}$$

$$D_{CPU+RS} = 10 \text{ micros} \quad \text{HTTR} = 1 \text{ hour}$$

$$D_{Router} = 10 \text{ micros}$$

average service time, throughput, final bottleneck

$$F_{ETH}^{req} = \frac{500}{65535} = 1 \text{ fragments ETH}$$

$$F_{ETH}^{req} = \frac{100.000}{65535} = 2 \text{ fragments ETH}$$

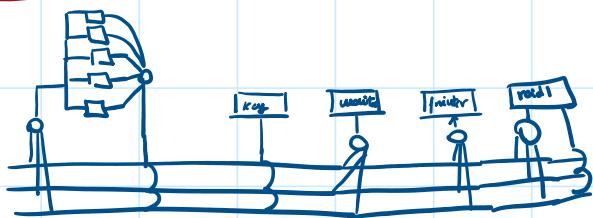
$$\text{Frames} = \text{datagrammi} = \frac{100.000}{1460} = 69+3$$

$$\text{Overhead} = (69+3) (20+20+16) = 4196$$

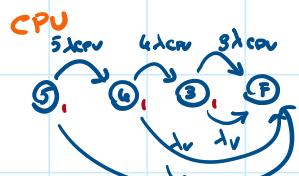
$$D_{ETH}^{req} = \frac{100.000 + 4196}{2 \cdot 10^3} = 5208 \cdot 10^{-5}$$

R,S

Esercizio n° 1



Reliability



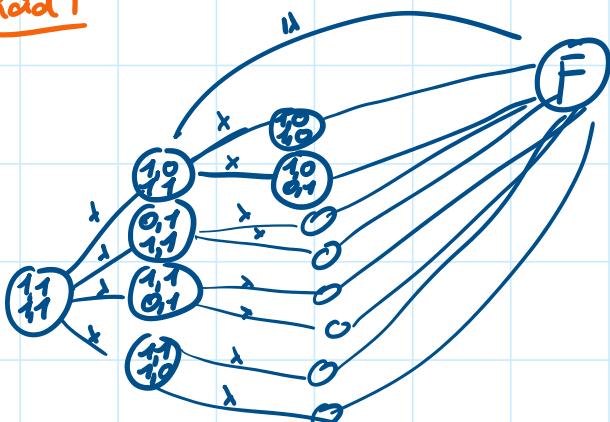
$$\begin{aligned} \dot{P}_S(t) &= P_S(t) \cdot -3\lambda_{CPU} + P_F(t) \cdot \lambda_V \\ \dot{P}_U(t) &= P_S(t) \cdot 5\lambda_{CPU} - P_U(t) \cdot 4\lambda_{CPU} - P_U(t) \cdot \lambda_{VOT} \\ \dot{P}_F(t) &= P_U(t) \cdot 4\lambda_{CPU} - P_U(t) \cdot \lambda_V + P_U(t) \cdot \lambda_{VOT} \\ \dot{P}_F(t) &= P_S \lambda_V + P_U \lambda_V + P_3(t) \cdot 3\lambda_{CPU} \\ P_S(t) &= 1 \quad \text{Reliability}(t) = 1 - P_F(t) \end{aligned}$$

Keyboard / Monitor / Printer



$$\text{Reliability}(t) = 1 - P_F(t)$$

Raid 1



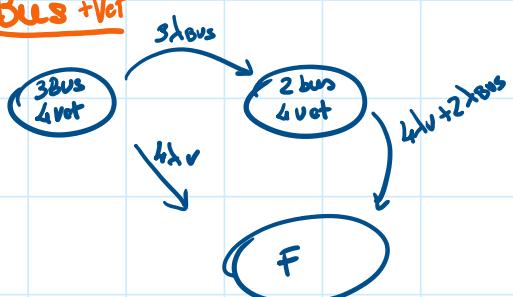
2-5

1 failure

Raid 0

0 failure

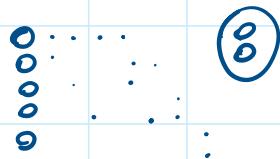
BUS + VOT



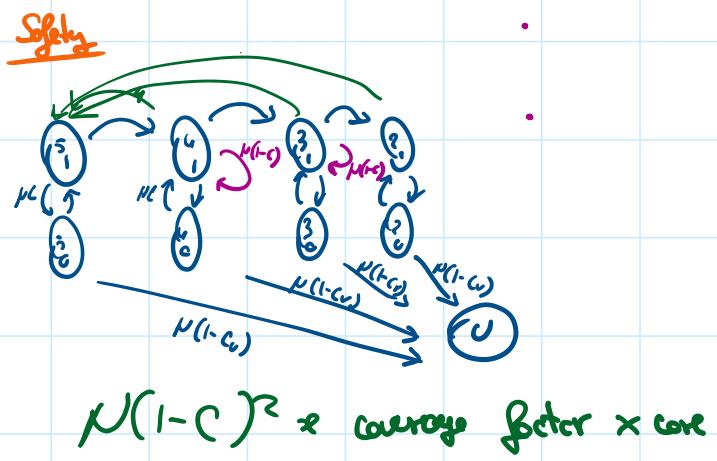
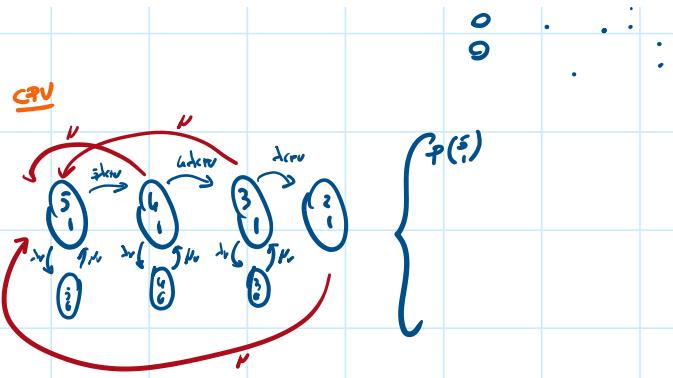
$$\begin{cases} \dot{P}(z_u)(t) = -P(z_u)(3\lambda_{bus} + 4\lambda_V) \\ \dot{P}(z_u)(t) = P(z_u)(t) \cdot (3\lambda_{bus}) + -P(z_u)(t) \cdot (4\lambda_V + 2\lambda_{bus}) \\ \dot{P}(F)(t) = (4\lambda_V) \cdot P(z_u)(t) + (4\lambda_V + 2\lambda_{bus}) P(z_u)(t) \\ P(z_u)(t) = 1 \end{cases}$$

Avoidability

N riparo tutto il componente



CPU



Esercizio 2

Sei p e n uguali per quanto riguarda
calcolo P $\bar{x} = \bar{N}$

Se tempo scontato delle retture sono indipendenti

$$A = \frac{\text{MTTR}}{\text{MTTF} + \text{MTTR}} = 0.38$$

$$q_3 = 1 \cdot A^3 \quad q_2 = A^2(1-A) \quad q_1 = 3A(1-A)^2$$

$$q_0 = (1-A)^3$$

$$\bar{R} = q_1 \cdot R_1 + q_2 \cdot R_2 + q_3 \cdot R_3$$

$$\bar{x} = q_1 \bar{x}_1 + q_2 \bar{x}_2 + q_3 \bar{x}_3$$

1 Gbps FDDI

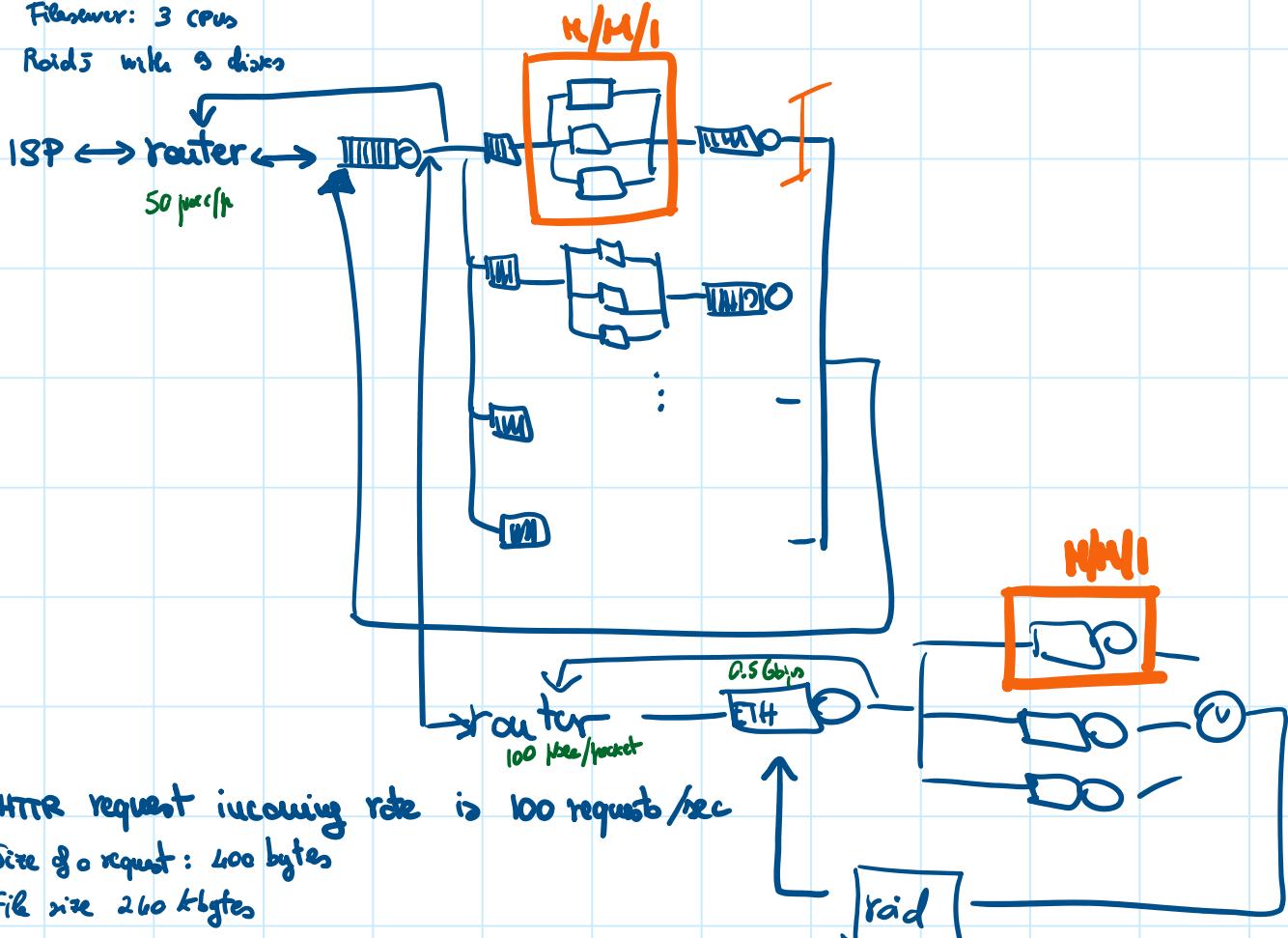
50 μsec/packet latency

FDDI Router 1.66 Gbps

Website: 4 cores, local mem, local disk

Fileserver: 3 cpus

Raid5 with 3 disks



HTTP request incoming rate is 100 requests/sec

Size of a request: 400 bytes

File size 260 kbytes

$$D_{CPU} = 5 \text{ msec} \quad \text{if stored in main memory}$$

$$D_{CPU-DISK} = 10 \text{ msec} \quad \text{if local-disk}$$

$$D_{CPU-NETWORK} = 30 \text{ msec}$$

$$D_{NETWORK} = 10 \text{ msec}$$

$$\text{Single disk} = 10 \text{ msec} \times 20 \text{ kbytes} \\ \text{or RAID5}$$

$$D_{DISK} = \frac{260}{20} \cdot 10 = 120$$

Networking Course MTU

$$\text{packets} = \frac{260,000}{1460} = 165$$

$$\text{ackets/brequest} = \frac{600}{1460} = 1$$

$$D_{FDDI} = 1 + 3(20 + 20 + 28) + 400 + (165 + 3)(20 + 20 + 28) + 260,000 = 240,224$$

↑ 165 - 20 - 28 →

rate generated

$$D_{ROUTER} = 172 \cdot 50 \text{ μsec} = 8,6 \text{ μ/sec}$$

IP: choose 2 packets, optimize jacks

Rete Immobiliare

$$D_{\text{Router}} = 172 \cdot 50 \text{ } \mu/\text{sec} = 8,6 \text{ } \mu/\text{sec}$$

D_{Router} = uguale o quello minimo con $16 \text{ Gbit} = 2,0 \text{ } \mu/\text{sec}$

$$P_{\text{idle}} = \sum_{i=1}^5 k_i \quad 20\% \text{ hit rate}, 80\% \text{ miss}$$

$$P_{\text{disk}} = \sum_{i=1}^5 k_i \quad 60\% \text{ hit disk}, 40\% \text{ miss}$$

Average response time:

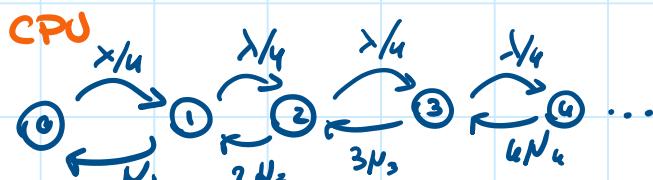
$$\bar{R}_i = \frac{D}{1-U_i}$$

$R_{\text{tot}} = \sum R_i$

U = X · D

diff:

~~$\frac{1}{N}$~~



$$P_0 = \left[1 + \sum_{k=1}^{\infty} \frac{\lambda^k}{k!} p(k) + \frac{\lambda^I}{I!} \frac{p^I}{1-p} \right]$$

$$\begin{aligned} x_1 &= p_1 \\ x_2 &= p_2 \\ x_3 &= p_3 \\ x_4 &= p_4 \end{aligned}$$

$$\Rightarrow \bar{x}$$

Disk

Router:

ipercapte

Esercizio n. 1

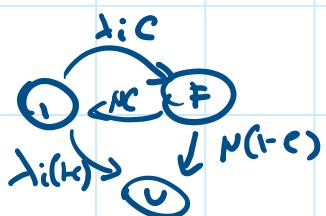
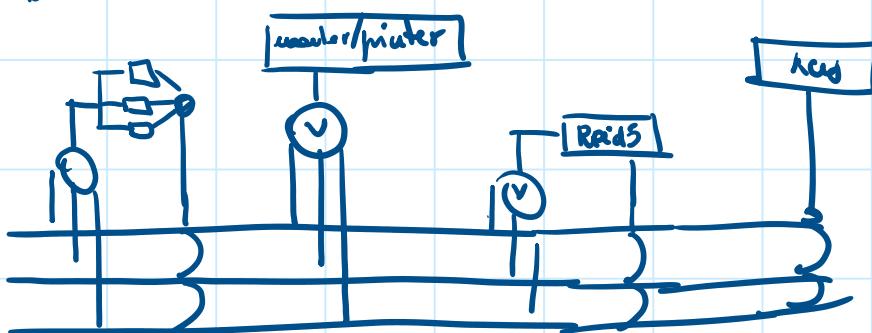
3 CPU in parallelo with voter

Raid 5 with 8 disks

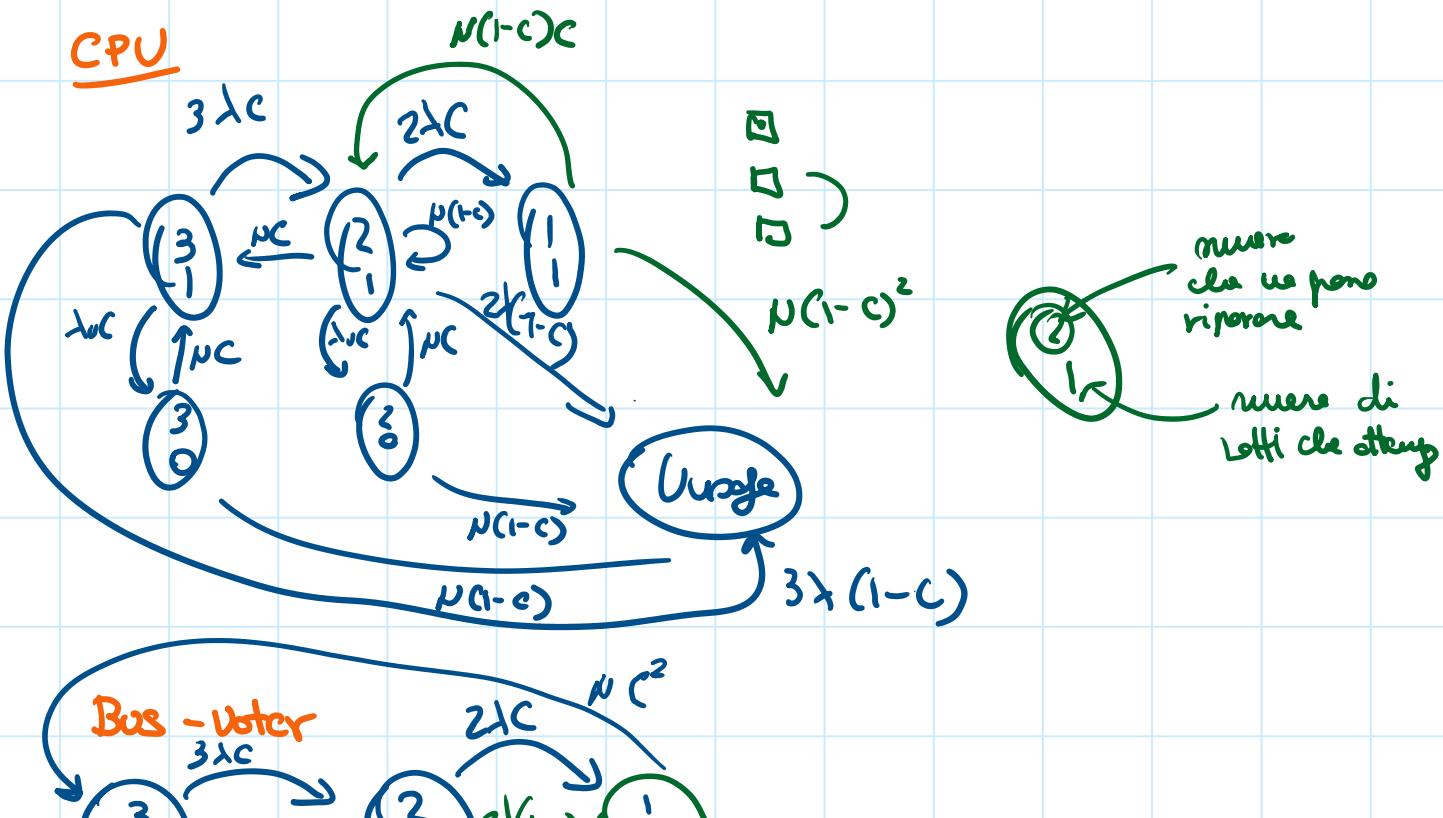
3 bus

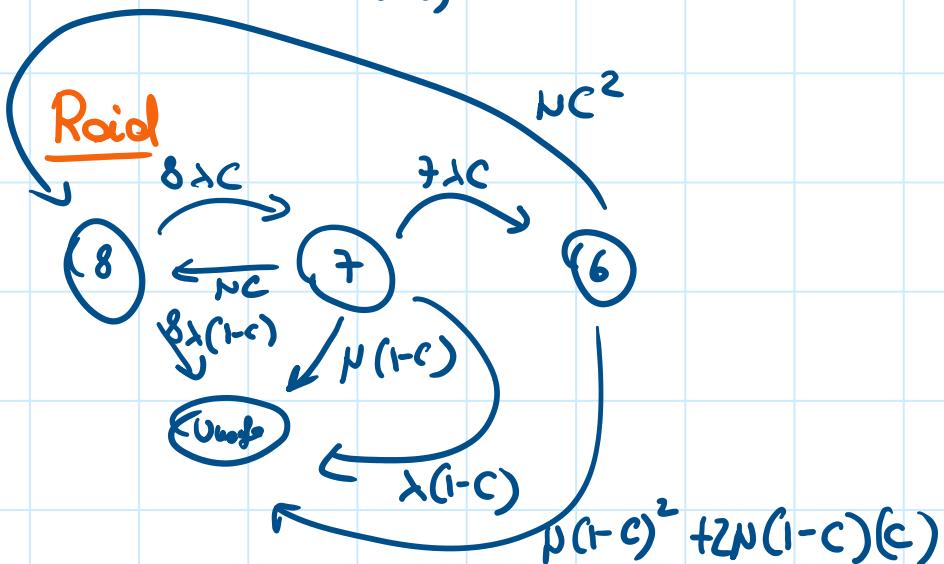
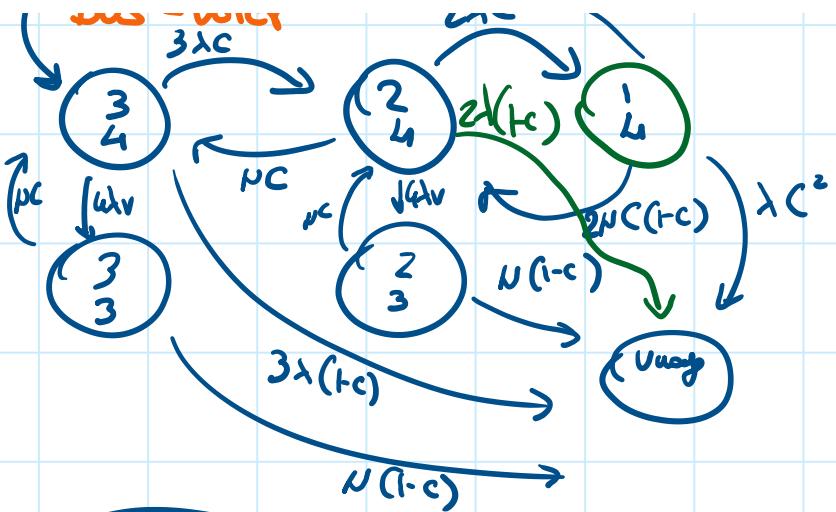
1 keyboard

1 monitor



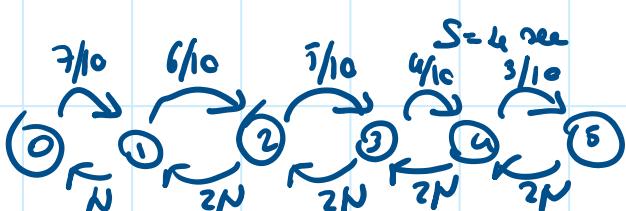
$$\left\{ \begin{array}{l} P_i(t) = P_i(0) \cdot (-\lambda_{iC}) + P_F(\mu_C) \\ P_F(t) = P_F(0) \cdot (-\mu_C - N(1-C)) + P_i(t)\lambda_{iC} \\ V(t) = P_F(t)N(1-C) + P_i(t)\cdot\lambda_{i(1-C)} \end{array} \right.$$





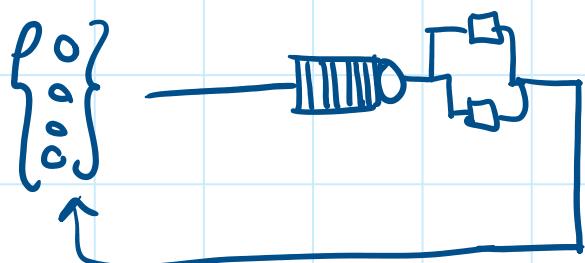
Esercizio n. 2

\bar{R} \bar{x} ?



10 sec think time

$S = 4$ sec



2. Funzionanti

$$\left\{ \begin{array}{l} P_0 \frac{3}{10} = P_1 2N \\ P_1 \frac{6}{10} = P_2 2N \\ P_2 \frac{5}{10} = P_3 2N \\ P_3 \frac{4}{10} = P_4 2N \\ P_4 \frac{3}{10} = P_5 2N \\ P_0 + P_1 + P_2 + P_3 + P_4 + P_5 = 1 \end{array} \right.$$

=>

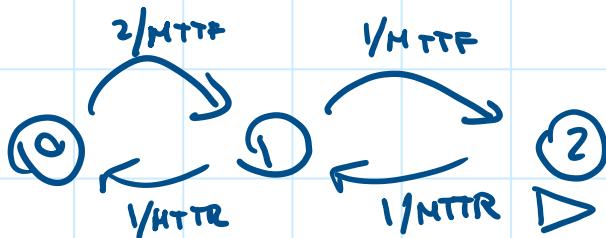
$$\begin{aligned} P_0 &= x_{1,2} \\ P_1 &= 0_{1,2} \\ P_2 &= \alpha_{2,1,2} \\ P_3 &= \alpha_{3,2} \\ P_4 &= \alpha_{4,2} \end{aligned}$$

X

1. Funzionanti

1. Fundamentals

$$\left\{ \begin{array}{l} P_0 \cdot \frac{2}{10} = P_1 \cdot 1 \\ P_1 \cdot \frac{6}{10} = P_2 \cdot 1 \\ P_2 \cdot \frac{5}{10} = P_3 \cdot 1 \\ P_3 \cdot \frac{4}{10} = P_4 \cdot 1 \\ P_4 \cdot \frac{3}{10} = P_5 \cdot 1 \\ P_0 + P_1 + P_2 + P_3 + P_4 + P_5 = 1 \end{array} \right. \Rightarrow \begin{array}{l} P_0 = \alpha_{1,1} \\ P_1 = \alpha_{1,1} \\ P_2 = \alpha_{2,1} \\ P_3 = \alpha_{3,1} \\ P_4 = \alpha_{4,1} \\ P_5 = \alpha_{5,1} \end{array}$$



Ip: T ripetutore x attacchi

$$\left\{ \begin{array}{l} P_0 \cdot \frac{2}{MTTF} = P_1 \cdot \frac{1}{MTTR} \\ P_1 \cdot \frac{1}{MTTF} = P_2 \cdot \frac{1}{MTTF} \\ P_0 + P_1 + P_2 = 1 \end{array} \right. \Rightarrow \begin{array}{l} P_0^F, P_1^F, P_2^F \end{array}$$

$$X_0^2 = \sum w_i P_i = \mu R + 2N P_2 \dots$$

$$X_0' = \sum p_i P_i = \mu R_1 + 2 \mu P_2 \dots$$

$$N^2 = \sum_i P_i = P_1^2 + 2P_2^2 + 3P_3^2$$

$$\bar{R}^2 = \frac{\bar{N}^2}{X_0^2}$$

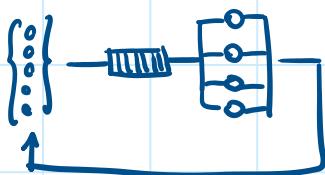
$$\bar{R}' = \frac{\bar{N}'}{X_0}$$

$$\bar{R} = P_0 \cdot \bar{R}^2 + P_1 \cdot \bar{R}'$$

Esercizi 19/02/15

lunedì 20 maggio 2019

14:47



$$\begin{aligned} t &= 10 \text{ sec} \\ S &= 2 \text{ sec} \\ \mu &= \frac{1}{S} = 0.5 \\ \text{MTTF} &= 10 \text{ sec} \\ \text{MTTR} &= 2 \text{ sec} \\ \text{MTBF} &= 10 - 2 = 8 \text{ sec} \end{aligned}$$



Caso 4/u

$$\left\{ \begin{array}{l} P_0 \cdot 0.5 = P_1 \cdot 0.5 \\ P_1 \cdot 0.2 = P_2 \\ P_2 \cdot 0.1 = P_3 \cdot 1.5 \\ P_3 \cdot 0.1 = P_4 \cdot 2 \\ P_4 \cdot 0.2 = P_5 \cdot 2 \\ P_5 \cdot 0.1 = P_6 \cdot 2 \\ P_6 + P_1 + P_2 + P_3 + P_4 + P_5 + P_6 = 1 \end{array} \right.$$

$$P_0 = 0.292$$

$$P_1 = 0.391$$

$$P_2 = 0.129$$

$$P_3 = 0.103$$

$$P_4 = 0.025$$

$$P_5 = 5 \cdot 10^{-3}$$

$$P_6 = 7 \cdot 10^{-4}$$

$$\bar{N}_u = \sum i P_i = 1.327$$

$$\bar{x}_u = \sum N_i P_i = 0.66$$

$$\bar{R} = \frac{\bar{N}_u}{\bar{x}_u} = 2.01$$

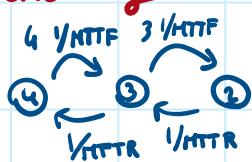
Caso 3/4



Caso 3/4

$$\left\{ \begin{array}{l} P_0 \cdot 0.5 = P_1 \cdot 0.5 \\ P_1 \cdot 0.2 = P_2 \\ P_2 \cdot 0.1 = P_3 \cdot 1.5 \\ P_3 \cdot 0.1 = P_4 \cdot 1.5 \\ P_4 \cdot 0.2 = P_5 \cdot 1.5 \\ P_5 \cdot 0.1 = P_6 \cdot 1.5 \\ P_6 + P_1 + P_2 + P_3 + P_4 + P_5 + P_6 = 1 \end{array} \right.$$

Availability



I_{fp} : Riparazione e guasti dipendenti

I_{fp} : Spese dopo 2

$$P(B)_{\text{time}} = P_6 \cdot \frac{1}{\text{MTTF}}$$

$$P_u = P_3 \cdot \frac{\text{MTTF}}{L + \text{MTTR}}$$

$$P_3 = \frac{4 \cdot \text{MTTR}}{\text{MTTF}} \cdot P_4$$

MTTR = 1/MTTF

$$\begin{cases} P_3/MTTF = P_u/MTTF \\ P_2/MTTF = P_3/MTTF \\ P_3 + P_2 + P_u = 1 \end{cases}$$

$$P_u = P_3 \cdot \frac{MTTF}{4 MTTF}$$

$$P_3 = P_2 \cdot \frac{MTTF}{3 MTTF}$$

$$P_3 + P_2 + P_u = 1$$

$$P_3 = \frac{4 MTTR}{MTTF} \cdot P_4$$

$$P_2 = \frac{3 MTTR}{MTTF} \cdot \cancel{P_3} \quad \frac{4 MTTR}{MTTF} \cdot P_4$$

$$\left(\frac{4 MTTR}{MTTF} + \frac{3 MTTR}{MTTF} \cdot \frac{4 MTTR}{MTTF} + 1 \right) P_4 = 1$$

$$\cancel{\frac{8}{1680}} + \cancel{\frac{6}{1680}} \cdot \cancel{\frac{8}{1680}} + 1$$

$$P_u \approx 0.537$$

$$P_3 = 4,76 \cdot 10^{-3}$$

$$P_2 = 2,256 \cdot 10^{-3}$$

$$\bar{R} = P_u \bar{R}_u + P^* \bar{R}_s$$

Esercizio 06/06/13

lunedì 20 maggio 2019 15:25

Requests 5 workstations (users)

$$Z = 5000 \text{ msec}$$

$$R_{CPU} = 20 \text{ usec}$$

$$D_{Disk} = 10 \cdot 5 = 50 \text{ msec}$$

At most 3 users

R ? $\bar{x}=?$ Percentage of refined requests = ?



Caso N=1

$$R_{CPU} = 20 \text{ usec}$$

$$D_{Disk} = 50 \text{ msec}$$

$$R_{TOT} = 70 \text{ msec}$$

$$\bar{x}_1 = \frac{1}{R_{TOT}} = 0,014$$

$$N_{CPU} = R_{CPU} \cdot X_0(1) = 0,28$$

$$N_{Disk} = R_{Disk} \cdot X_0(1) = 0,72$$

Caso N=2

$$R_{CPU} = R_{CPU}(1 + M_{CPU,i-1}) = 26,6 \text{ msec}$$

$$R_{Disk} = D_{Disk}(1 + M_{Disk,i-1}) = 86 \text{ msec}$$

$$\bar{x}_2 = \frac{2}{R_{TOT}} = \frac{2}{16,6} = 0,018$$

$$M_{CPU_2} = 25,6 \cdot 0,018 = 0,46$$

$$M_{Disk_2} = 86 \cdot 0,018 = 1,54$$

Caso u=3

$$R_{CPU} = R_{CPU}(1 + M_{CPU,2}) = 29,2$$

$$R_{Disk} = D_{Disk}(1 + M_{Disk,2}) = 127$$

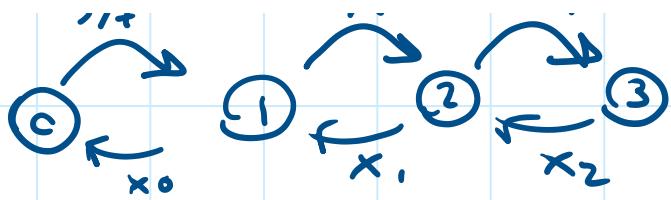
$$R_{TOT} = 156,2$$

$$N_{CPU_3} = 0,554$$

$$N_{Disk_3} = 2,413$$

$$X_3 = \frac{3}{R_{TOT}} = 0,0192$$





$$\begin{cases} P_0 \cdot x_0 = P_1 \cdot x_0 \\ P_1 \cdot x_1 = P_2 \cdot x_1 \\ P_2 \cdot x_2 = P_3 \cdot x_2 \\ P_0 + P_1 + P_2 + P_3 = 1 \end{cases}$$

$$P_0 = 0,930$$

$$P_1 = 0,066$$

$$P_2 = 2,953 \cdot 10^{-3}$$

$$P_3 = 9,328 \cdot 10^{-5}$$

$$\bar{x} = x_i - P_i = 9,79 \cdot 10^{-4} = 0.$$

$$\bar{R} = \frac{N}{x} = \frac{0,072}{9,79 \cdot 10^{-4}} = 73,55$$

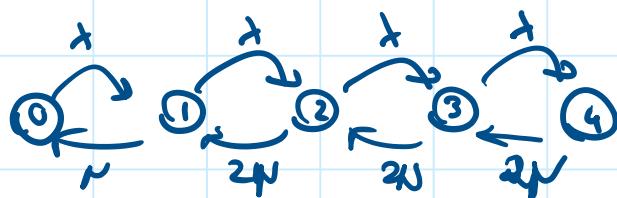
I controlli sono
di minor

0,013902 +

2 servers, max 4 users

$\lambda = 0.5$ (service rate)

$X = ?$ $V = ?$



Fluxus = flow out

$$\left\{ \begin{array}{l} p_0 \\ \vdots \\ p_N \end{array} \right\} \Rightarrow \left\{ \begin{array}{l} p_0 \\ p_1 \\ p_2 \\ p_3 \\ p_4 \end{array} \right\}$$

part by quantity

$$X = \sum_i \mu_i p_i =$$

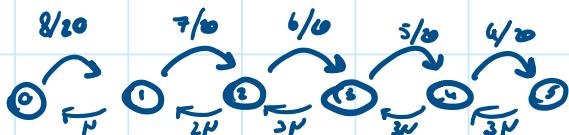
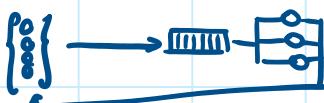
$$N = \sum_i i p_i =$$

$$p_0 = \frac{\lambda}{N}$$

$$V = 1 - p_0 = 0.24$$

Esercizio 2

$$\bar{R} = ?$$



$$N = 10$$

$$\frac{1}{MTTF} = \frac{1}{12} \text{ months} = \frac{1}{365 \cdot 24}$$

$$\frac{1}{MTTR} = \frac{1}{12} \text{ hours} =$$

$$P_0 = 0.03$$

$$\begin{cases} P_0 \cdot \frac{8}{20} = P_1 \cdot 0.1 \\ P_1 \cdot \frac{7}{20} = P_2 \cdot 0.2 \\ P_2 \cdot \frac{6}{20} = P_3 \cdot 0.3 \\ P_3 \cdot \frac{5}{20} = P_4 \cdot 0.3 \\ P_4 \cdot \frac{4}{20} = P_5 \cdot 0.3 \end{cases}$$

$$P_0 + P_1 + P_2 + P_3 + P_4 + P_5 = 1$$

$$P_1 = \frac{P_0 \cdot \frac{8}{20}}{0.1} = 0.12$$

$$P_2 = \frac{P_1 \cdot \frac{7}{20}}{0.2} = 0.14$$

$$P_3 = \frac{P_2 \cdot \frac{6}{20}}{0.3} = 0.21$$

$$P_4 = \frac{P_3 \cdot \frac{5}{20}}{0.3} = 0.175$$

$$P_5 = 0.116$$

$$N_i = \sum_i P_i = 2.45$$

$$\bar{X}_i = \sum N_i \cdot P_i = 0.20$$

$$\bar{R}_S = \frac{N}{N_i} = 12$$

Caso 2 server

$$\begin{cases} P_0 \cdot \frac{8}{20} = P_1 \cdot 0.1 \\ P_1 \cdot \frac{7}{20} = P_2 \cdot 0.2 \\ P_2 \cdot \frac{6}{20} = P_3 \cdot 0.2 \\ P_3 \cdot \frac{5}{20} = P_4 \cdot 0.2 \\ P_4 \cdot \frac{4}{20} = P_5 \cdot 0.2 \\ P_0 + P_1 + P_2 + P_3 + P_4 + P_5 = 1 \end{cases}$$

\Rightarrow

$$P_0 = \frac{1}{[P_1 + P_2 + P_3 + \dots]} = 0.02$$

$$P_{1T} = 4$$

$$P_{2T} = \frac{4 \cdot \frac{7}{20}}{0.2} = 7 \quad P_2 = 0.14$$

$$P_{3T} = 10.5$$

$$P_{4T} = 13.12$$

$$P_{5T} = 13.12$$

$$P_1 = 0.08$$

$$P_3 = 0.21$$

$$P_4 = 0.26$$

$$P_5 = 0.26$$

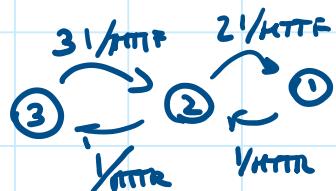
$$P_{ST} = 13,12$$

$$\bar{N}_2 = 3,33$$

$$x_2 = 0,18$$

$$R_2 = 18,29$$

Availability



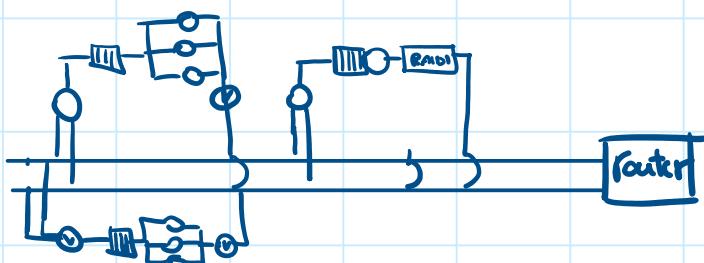
$$\begin{cases} P_3 Y_{hMTTF} = P_2 \cdot Y_{hMTTF} \\ P_2 Y_{hMTTF} = P_1 \cdot Y_{hMTTF} \\ P_3 + P_2 + P_1 = 1 \end{cases}$$

$$\begin{aligned} P_3 &= 0,995 \\ P_2 &= 4,08 \cdot 10^{-3} \\ P_1 &= 9,2 \cdot 10^{-6} \end{aligned}$$

$$\bar{x} = P_3 \cdot \bar{x}_3 + P_2 \cdot \bar{x}_2 = 0,203$$

$$\bar{R} = P_3 \cdot \bar{R}_3 + P_2 \cdot \bar{R}_2 = 12,01$$

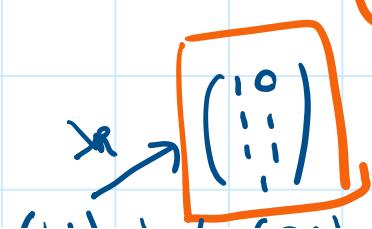
Esercizio 1

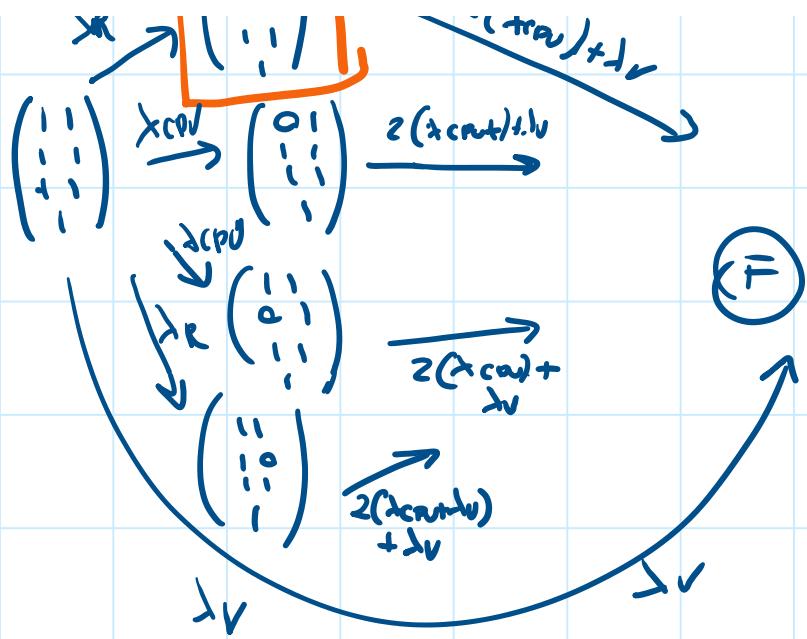


Reliability

(3 2) $\rightarrow F$

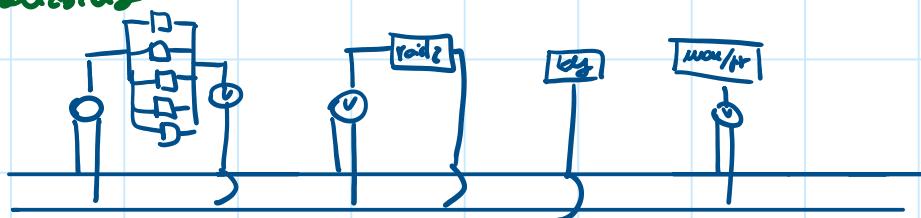
$2(\text{tra}) \times J_{\text{tra}}$



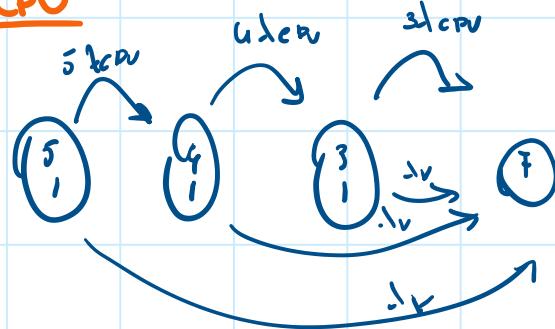


Esercizio 1

Reliability

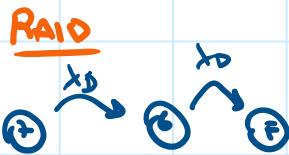
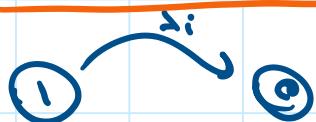


CPU

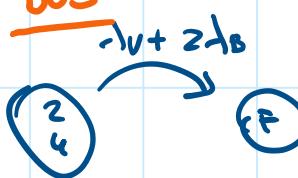


$$\left\{ \begin{array}{l} P_{S,1}(t) = P_{S,1}(t) - (-\lambda_{CPU}) \\ \vdots \\ P_{S,1}(0) = 1 \end{array} \right.$$

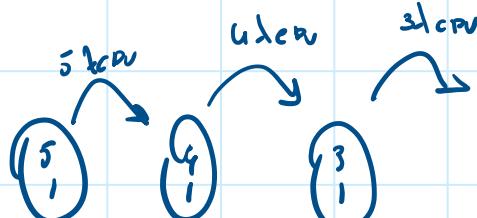
MONITOR PRINTER Keyboard



Bus



Availability



Esercizio cosa

martedì 21 maggio 2019 16:08

$$\text{SLA: } \lambda = 100 \text{ requests/sec}$$

$$R = 1 \text{ sec}$$

$$\text{Difp} = 95\% \quad \text{loss} = 2\%$$



$$S_{\text{CPU}} = 10 \text{ msec}$$

$$S_{\text{Disk}} = 20 \text{ msec}$$

max 4 utenti

$$\text{HTTR}_{\text{CPU}} = 1 \text{ week} = 52$$

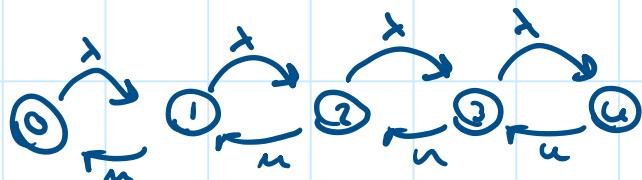
4 utenti max

$$\text{HTTR}_{\text{Disk}} = 6 \text{ months} = 26 \text{ sett}$$

$$\text{HTTR}_{\text{CPU}} = 1 \text{ week}$$

$$\text{HTTR}_{\text{Disk}} = 1 \text{ week}$$

maintenance indipendenti



$$A_{\text{CPU}} = \frac{\text{HTTR}}{\text{HTTR}_{\text{CPU}} + \text{HTTR}_{\text{CPU}}} = \frac{52}{1+52} = 0.98$$

$$A_{\text{Disk}} = \frac{\text{HTTR}}{\text{HTTR}_{\text{Disk}} + \text{HTTR}_{\text{Disk}}} = \frac{26}{1+26} = 0.96$$

$$A_{1/2 \text{ disk}} = 2 A_{\text{disk}} (1 - A_{\text{disk}}) = 0.076$$

$$A_{2/2 \text{ disk}} = 0.96 \cdot 0.96 = 0.92$$

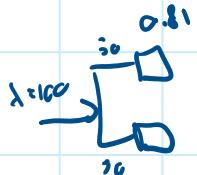
$$A_S = A_{\text{CPU}} \cdot A_{1/2 \text{ disk}} = 0.076\% \quad \text{Hanno disk, quindi}$$

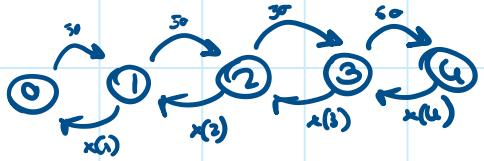
$$A_3 = A_{\text{CPU}} \cdot A_{2/2 \text{ disk}} = 0.90\% \quad \text{Non comuniti, come da SLA}$$

$$A_{\text{TOT}} = 1 - (1 - 0.90)^2 = 0.53\% \quad \text{Il resto di tempo è perde}$$

$$A_{\text{Attivi e 2}} = 0.81 \quad P_2$$

$$A_{\text{Attivi}} = 2(1 - 0.90)(0.50) = 0.18 \quad P_1$$





Caso u1

$$\begin{aligned} R_{CPU} &= 10 \\ R_{Disk} &= 20 \\ R_{RTT} &= 30 \\ X_1 &= \sqrt{3} \cdot 10^{-2} \\ N_{CPU} = D_{CPU} & X_1 = 0,33 \\ N_{Disk} = D_{Disk} & X_1 = 0,66 \end{aligned}$$

Caso u2

$$R_{CPU} = 10(1 + N_{CPU_1}) = 13,3$$

$$R_{Disk} = 20$$

$$R_{RTT} = 33,3$$

$$X_2 = 1/33,3 = 3$$

$$N_{CPU_2} = D_{CPU} X_1 =$$

$$N_{Disk} = D_{Disk} \cdot X_1 =$$

! ! ? ?

Caso u3

$$\begin{aligned} R_{CPU} &= 10(1 + N_{CPU_2}) \\ R_{Disk} &= 20(1 + N_{Disk_2}) \\ X_3 &= \\ N_{CPU_3} & \end{aligned}$$

Caso u4

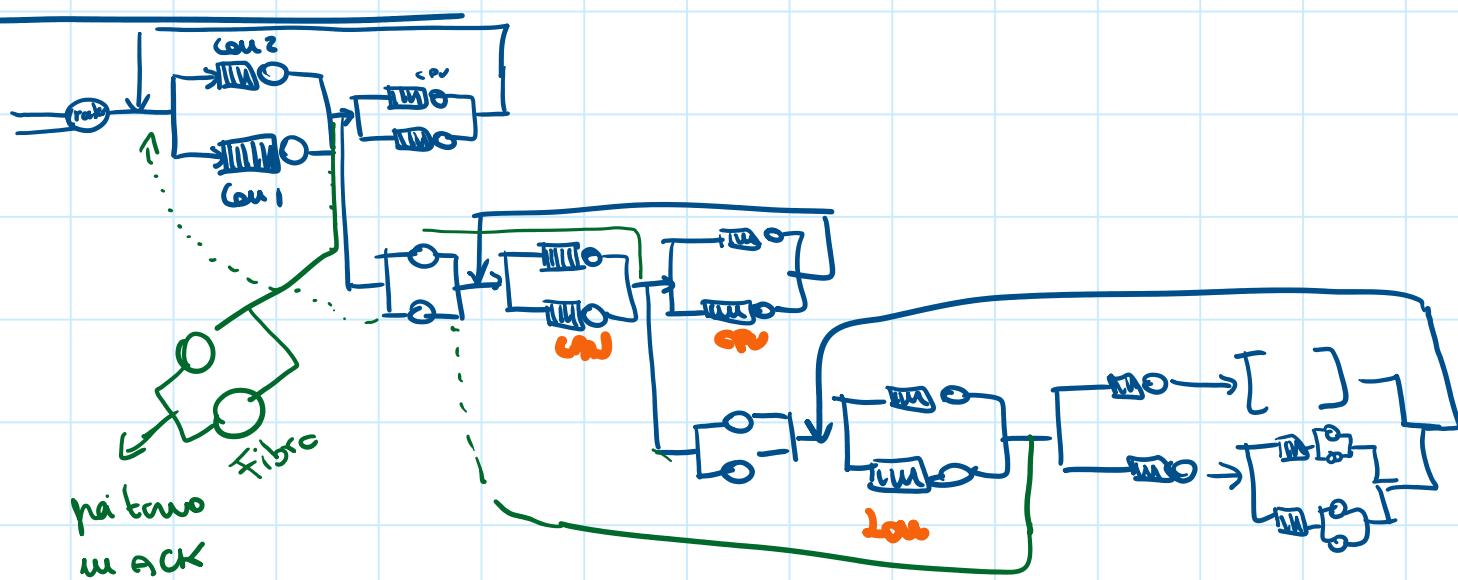
$$\begin{aligned} R_{CPU} &= \\ R_{Disk} &= R_{Disk_3} \\ X_4 & \end{aligned}$$

$$\bar{R}_2 = \sum P_i \cdot R_i$$

Rifore con 1 solo funzionante ($\lambda=100$)

→ Normalizzo con $(1 - P_0)$ se riduce solo al periodo funzionante

→ Non normalizo altrimenti



Esercizio perfezionability Alex

sabato 25 maggio 2019 17:29

$$\bar{R} = ? \quad \bar{x} = ?$$

6 server \rightarrow 1 CPU, RAM, RAID 1 (4+4)

$$MTTF_D = 500 \text{ ore} \quad MTTF_C = 1000 \text{ ore}$$

$$MTTR_D = 50 \text{ ore} \quad MTTR_C = 10 \text{ ore}$$

6 utenti con $\lambda = 10 \text{ user}$

$$A_{CPU} = \frac{1000}{1000} = 0.99$$

$$\mu = \frac{1}{5}$$

$$A_{Disk} = \frac{500}{500} = 0.90$$

$$A_{total} = (1 - (1 - A_{Disk})^6)^6 = 0.96$$

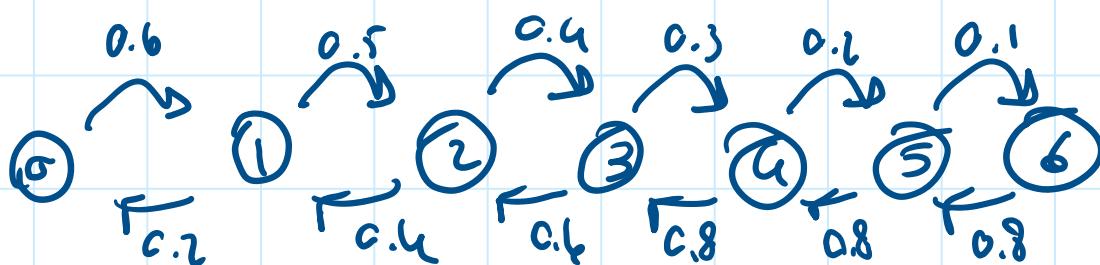
$$A_{server} = A_{CPU} \cdot A_{Disk}$$

$$q_0 = 0.95^6 = 0.81$$

$$q_1 = 6 \cdot 0.95^5 \cdot (1 - 0.95) = 0.17$$

$$q_2 = 6 \cdot 0.95^4 \cdot (1 - 0.95)^2 = 0.013$$

$${6 \choose 1} = \frac{6!}{1(5!)} = \frac{6}{6} = 1 \quad \begin{matrix} \text{in oggetti} \\ \text{per k o k} \end{matrix}$$



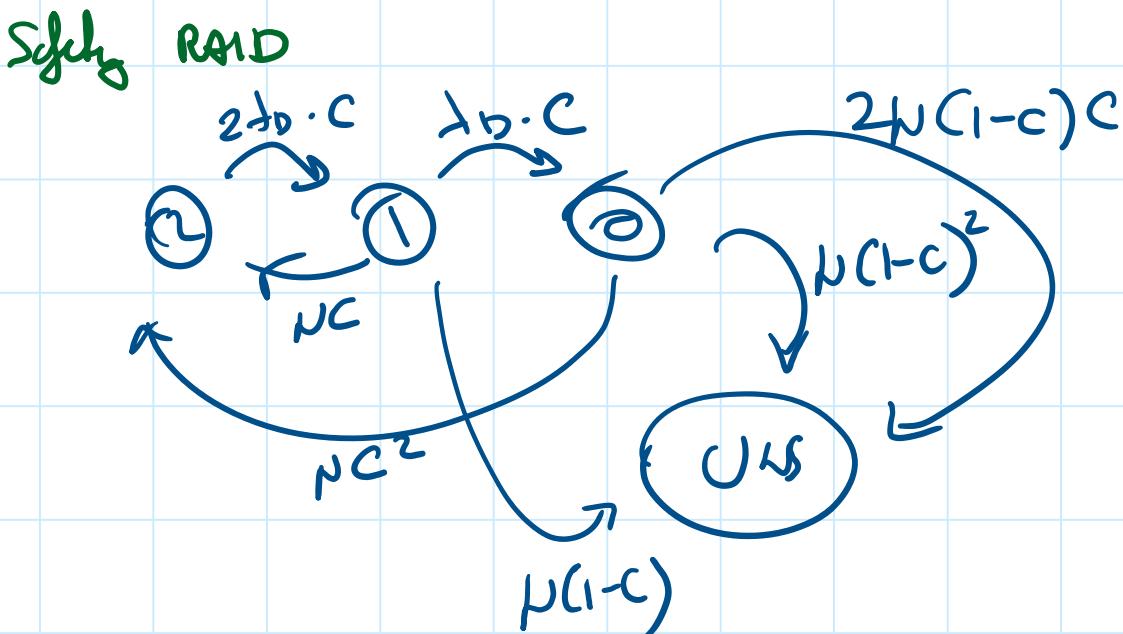
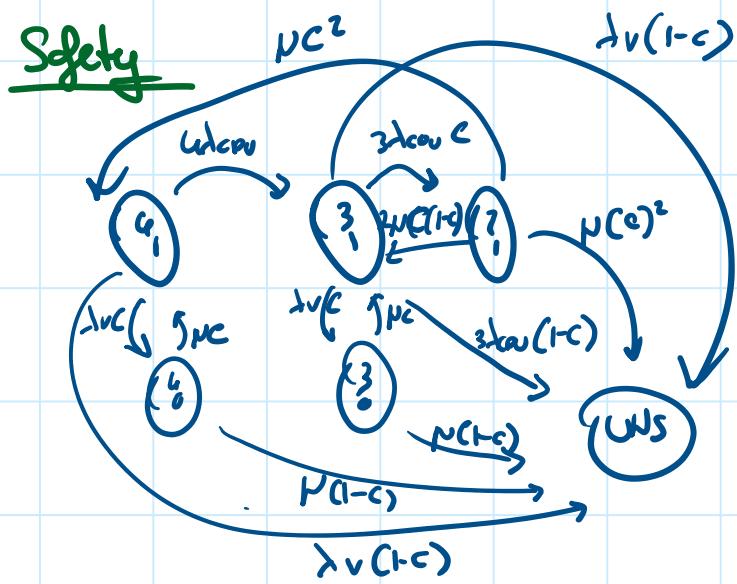
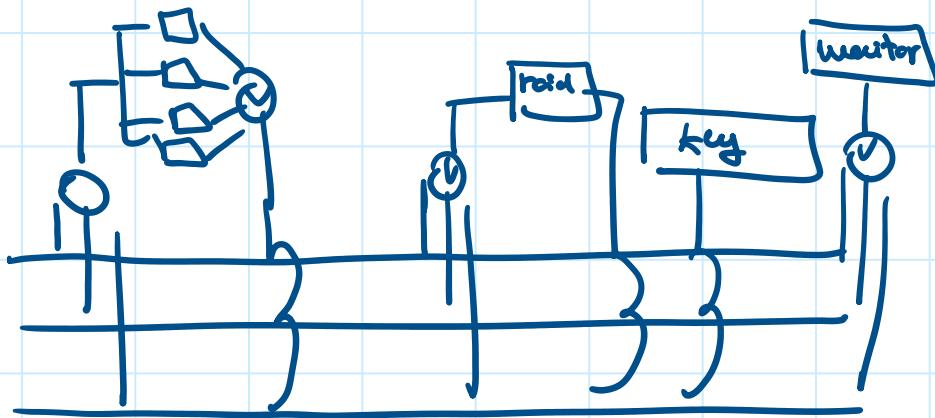
$$R_u = \sum i \cdot p_i = 1.87$$

$$X_u = \sum_N p_i = 0,39$$

$$\bar{R}_u = 5,05$$

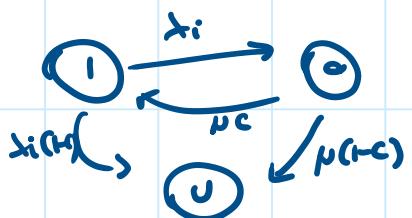
Fondo $\frac{1}{2} \cdot 3 \text{ gms}, \frac{1}{2} \text{ gms}, \frac{1}{2} \text{ gms}$

$$R_{\text{TOT}} = q_u \cdot R_u + q_3 \cdot R_3 + q_2 \cdot R_2 + q_1 \cdot R_1$$



$$\mu(1-c)$$

Safety Monitor/Printer



$$\bar{R} = ? \quad \bar{x} = ?$$

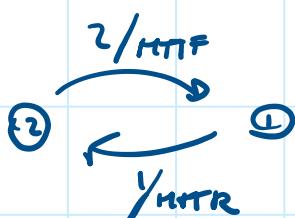
2 parallel system

at most 4 users

$$\tau = 100 \text{ sec}$$

$$MTTF = 3 \text{ week}$$

$$MTTR = 1 \text{ hour}$$



$$P_2 \frac{2}{\text{sec}} = P_1 \frac{1}{1}$$

$$P_1 \frac{1}{\text{sec}} = P_0 \frac{1}{1}$$

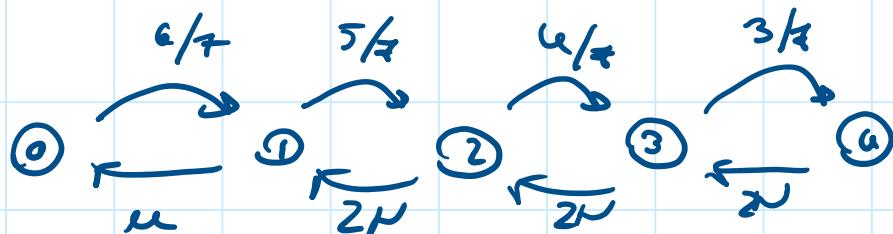
$$P_2 + P_1 + P_0 = 1$$

$$P_2 = \sqrt{1 + \frac{2}{\text{sec}} + \frac{2}{\text{sec}} \cdot \frac{1}{\text{sec}}} = 0,936$$

$$P_1 = 3,35 \cdot 10^{-3}$$

$$P_0 = 7,8 \cdot 10^{-6}$$

I_p : sistemi funzionano solo se entrambi funzionano



$$\left\{ \begin{array}{l} P_0 \\ P_1 \\ P_2 \\ P_3 \\ P_4 \end{array} \right.$$

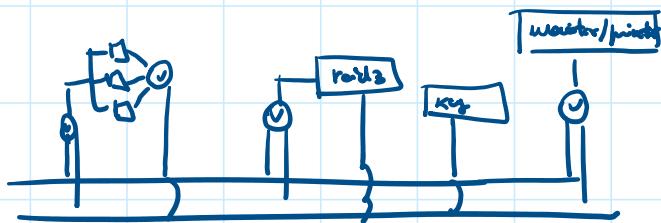
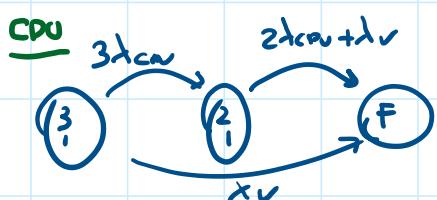
$$N = \sum_i P_i$$

$$X = \sum_i N_i \cdot P_i$$

$$R = \frac{N}{X}$$

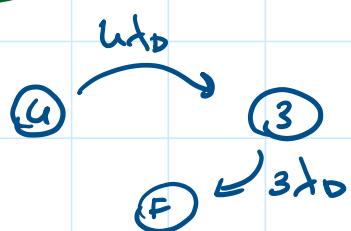
Esercizio 4.1.

3 CPU
Raid 3 4 disk
1 keyboard
1 Printer
1 monitor
2 bus

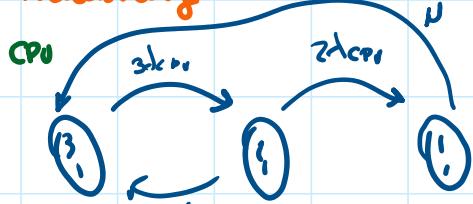
Reliability

$$\begin{cases} \dot{P}_{3,1}(t) = -P(3)(3\lambda_{CPU} + \lambda_V) \\ \dot{P}_{2,1}(t) = -P(2)(2\lambda_{CPU} + \lambda_V) + P(3) 3\lambda_{CPU} \\ \dot{P}_F(t) = +P(2)(t)(2\lambda_{CPU} + \lambda_V) + P(3)(t)(\lambda_V) \\ P(3)(0) = 1 \end{cases}$$

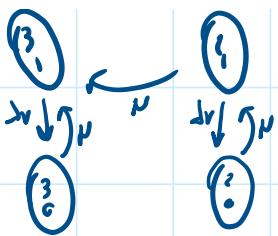
$$R_{CPU} = 1 - P_F(t)$$

DISK

$$\begin{cases} \dot{P}_4(t) = -P(4)(t) \lambda_D \\ \dot{P}_3(t) = +P(4)(t) \lambda_D - 3\lambda_D P_F(t) \\ \dot{P}_F(t) = P(F) 3\lambda_D \\ P(4)(0) = 1 \quad 0 \text{ otherwise} \end{cases}$$

MON / PRINTER / KEYBUSAvailability

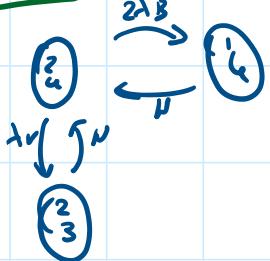
$$\begin{cases} P_{3,1}(3\lambda_{CPU} + \lambda_V) = P(3)\mu + P(1)N + P(3)N \\ P_{2,1}(2\lambda_{CPU} + \lambda_V) = P(2)\mu + P(3)3\lambda_C \\ P_{1,1}(N) = P(1)2\lambda_{CPU} \end{cases}$$



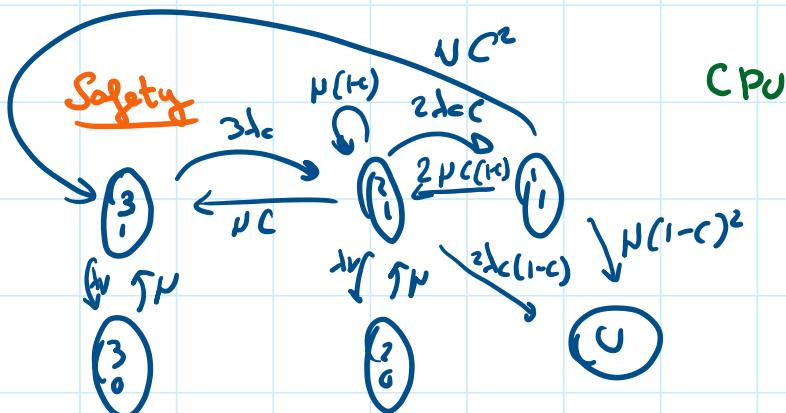
$$\left\{ \begin{array}{l} P_{1,0}(N) = P(1)2\lambda_{bus} \\ P_{3,0}(N) = P(3)\lambda_{bus} \\ P_{2,0}(N) = P(2)\lambda_{bus} \\ \sum_i P_i = 1 \end{array} \right.$$

$$A_C = P(3) + P(1)$$

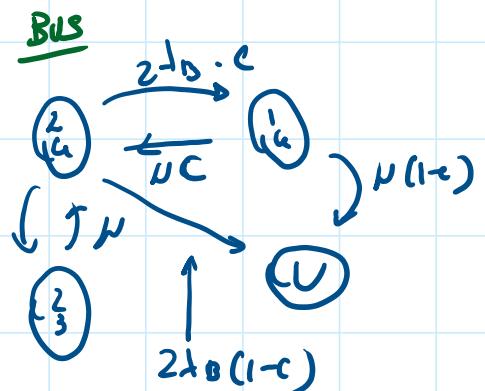
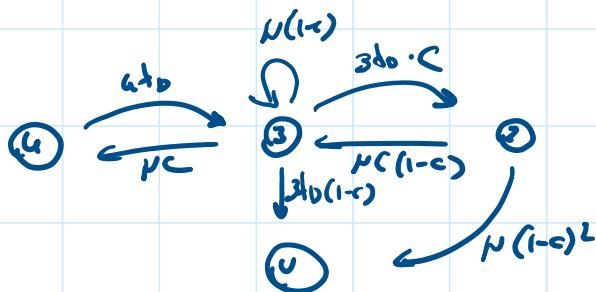
Bus



$$\left\{ \begin{array}{l} P(3)_N (2\lambda_B + \lambda_U) = P(1)_N + P(3)_N \\ P(1)_N = P(4)2\lambda_B \\ P(3)_N = P(1)\lambda_U \\ \sum_i P_i = 1 \end{array} \right.$$



DISK



Esercizio 11.3

$$R, \bar{x}$$

$$M/M/1/4/6$$

$$\tau = 30 \text{ sec}$$

$$S = 20 \text{ sec}$$

$$N = 1/S = 0,05 \text{ req/s}$$



$$\left\{ \begin{array}{l} 6/7 P_0 = \mu P_1 \\ 5/7 P_1 = \mu P_2 \\ 4/7 P_2 = \mu P_3 \\ 3/7 P_3 = \mu P_4 \\ \sum_i P_i = 1 \end{array} \right.$$

$$P_0 = 1 / \left[1 + \frac{6}{7\mu} + \frac{6}{7\mu} \cdot \frac{5}{7\mu} + \frac{6}{7\mu} \cdot \frac{5}{7\mu} \cdot \frac{4}{7\mu} + \frac{6}{7\mu} \cdot \frac{5}{7\mu} \cdot \frac{4}{7\mu} \cdot \frac{3}{7\mu} \right]$$

B.3
35.46

P_0

P_1

P_2

P_3

P_4

$$\bar{x} = \sum i \cdot P_i$$

$$N = \sum i \cdot P_i$$

$$\bar{R} = \frac{N}{\bar{x}}$$

Esercizio 6

$$\lambda = 10 \text{ req/s}$$

$$SCN = 10 \text{ ms}$$

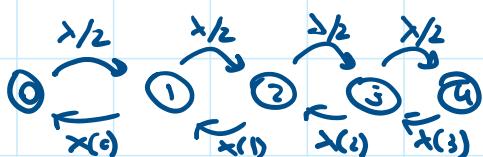
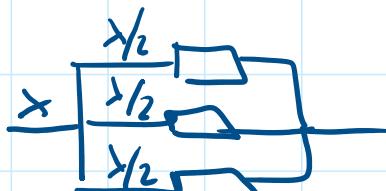
$$V = 2$$

$$S_{10} = 10 \text{ ms}$$

max 6 users

$$MTTF = 100000 \text{ s}$$

$$MTTR = 10 \text{ s}$$



Caso $\mu = 1$

Esercizio 2

Hip: questi e riparazioni indipendenti

2 parallel server

$\tau = 100 \text{ sec}$

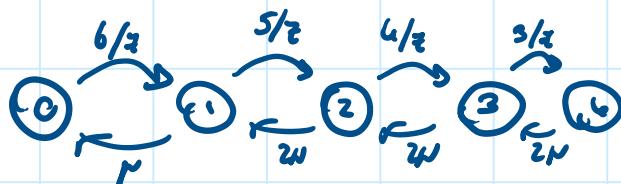
MTTF = 3 weeks

MTTR = 1 hour

$$A = \frac{\tau_2}{\tau_1 + \tau_2} = 0.38$$

$$A_2 = 0.38^2 = 0.36$$

$$A_1 = (0.58)(1 - 0.38) = 0.03$$



Due server online

$$\begin{cases} P_0 \cdot 6/\tau = P_1 \mu \\ P_1 \cdot 5/\tau = P_2 \mu \\ P_2 \cdot 4/\tau = P_3 \mu \\ P_3 \cdot 3/\tau = P_4 \mu \end{cases}$$

$$B = 1 / [1 + 0.06 + 1.5 \cdot 10^3 + 3 \cdot 10^{-5} + 4.5 \cdot 10^{-7}]$$

$$P_1 = 0.05$$

$$P_2 = 1.41 \cdot 10^{-3}$$

$$P_3 = 2.88 \cdot 10^{-5}$$

$$P_4 = 4.23 \cdot 10^{-7}$$

$$N = \sum i P_i = 0.05$$

$$X = \sum P_i \cdot \tau_i = 0.05$$

$$R = 1$$

Un server online

$$\begin{cases} P_0 \cdot 6/\tau = P_1 \mu \\ P_1 \cdot 5/\tau = P_2 \mu \\ P_2 \cdot 4/\tau = P_3 \mu \\ P_3 \cdot 3/\tau = P_4 \mu \end{cases}$$

$$P_0 = 1 / [1 + 0.06 + 3 \cdot 10^{-3} + 1.2 \cdot 10^{-4} + 3.6 \cdot 10^{-6}] = 0.96$$

$$P_1 = 0.05$$

$$P_2 = 2.5 \cdot 10^{-3}$$

$$P_3 = 1.10^{-4}$$

$$P_4 = 0.0006$$

$$\begin{cases} P_3 \cdot \frac{1}{2} = P_{4H} \\ P_3 = 1 \cdot 10^{-6} \\ P_4 = 3 \cdot 10^{-6} \end{cases}$$

$$N = \sum i \cdot P_i = 0.05$$

$$X = \sum N \cdot P_i = 0.05$$

$$k \geq 1$$

$$R = (A_2)(R_2) + (A_{\text{angle}})(R_1) \approx 1$$

Esercizio 11/12/2014

lunedì 27 maggio 2019

10:47

SLA:

0.2 seconds Response time

2% request loss

$$\begin{cases} 10 \text{ ms} & 0:00 - 12:00 \\ 20 \text{ ms} & 12:00 - 24:00 \end{cases}$$

Prime provider

$$D_{CPU} = 10 \text{ ms}$$

$$D_{DISK} = 30 \text{ ms} \text{ of I/O disk}$$

$$3 \text{ clients max}$$

$$12 \text{ euro } \times \text{day}$$

Second provider

$$D_{CPU} = 20 \text{ ms}$$

$$D_{DISK} = 20 \text{ ms}$$

$$4 \text{ clients max}$$

$$0.5 \text{ euro}$$

Availability:

$$A = \frac{24}{25} = 0.96$$

$$A_{1/1} = 0.92$$

$$A_{1/2} = 0.0768$$

99%

Prime provider



Case u=1

$$D_{CPU} = 10$$

$$D_{DISK} = 30 \cdot 10^{-3}$$

$$R_{CPU} = 40 \cdot 10^{-3}$$

$$X_1 = 1/10 = 0.1$$

$$N_{CPU,1} = X \cdot R_{CPU} = 0.25$$

$$N_{DISK,1} = X \cdot R_{DISK} = 0.75$$

$$\begin{cases} P_0 \lambda/2 = P_1 \cdot X_1 \\ P_1 \lambda/2 = P_2 \cdot X_2 \\ P_2 \lambda/2 = P_3 \cdot X_3 \\ \sum_i P_i = 1 \end{cases}$$

Case u=2

$$D_{CPU} = R_{CPU} (1 + 0.25) = 12.5 \cdot 10^{-3}$$

$$D_{DISK} = 30(1 + 0.35) = 52.5$$

$$X_2 = 30,7$$

$$N_{CPU,2} = 30,7 \cdot 12,5 \cdot 10^{-3} = 0.38$$

$$N_{DISK,2} = 30,7 \cdot 52,5 \cdot 10^{-3} = 1,61$$

$$P_0 = 1 / [1 + 0.4 + 0.13 + 0.03] = 0.64$$

$$P_1 = 0.25$$

$$P_2 = 0.08$$

$$P_3 = 0.02$$

$$N = \sum_i P_i = 0.67$$

$$X = \sum_i P_i \cdot X_i = 9,35$$

$$R = u/X = 0.05$$

Case u=3

$$D_{CPU} = R_{CPU} (1 + 0.38) = 13.8 \cdot 10^{-3}$$

$$D_{DISK} = R_{DISK} (1 + 1.61) = 58,3 \cdot 10^{-3}$$

$$X_3 = 32,4 \Rightarrow 32$$

$$N_{CPU,3} = 32,4 \cdot 13,8 \cdot 10^{-3} = 0,45$$

$$N_{DISK,3} = 32,4 \cdot 58,3 \cdot 10^{-3} = 2,15$$

$$\begin{cases} P_0 \lambda = P_1 \cdot X_1 \\ P_1 \lambda = P_2 \cdot X_2 \\ P_2 \lambda = P_3 \cdot X_3 \\ \sum_i P_i = 1 \end{cases}$$

$$P_0 = 1 / [1 + 0.8 + 0.53 + 0.30] = 0.59$$

$$P_1 = 0.304$$

$$P_2 = 0.2$$

$$P_3 = 0.11$$

$$\left\{ \begin{array}{l} P_1 x = P_2 x_2 \\ P_2 x = P_3 x_3 \end{array} \right.$$

$$\begin{aligned} P_1 &= 0,300 \\ P_2 &= 0,2 \\ P_3 &= 0,11 \end{aligned}$$

$$N = 1,01$$

$$X = 17,11$$

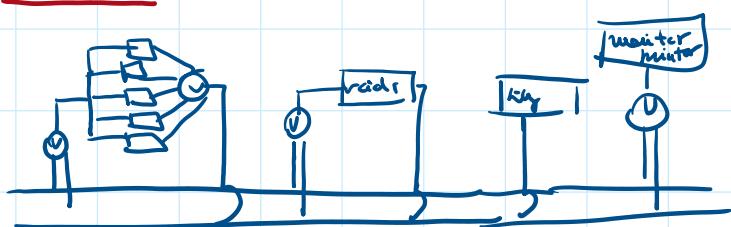
$$R = 0,06$$

$$\overline{P} = A_2(R_2) + A_{1/2}(R_1) = 0,05 \text{ RC}$$

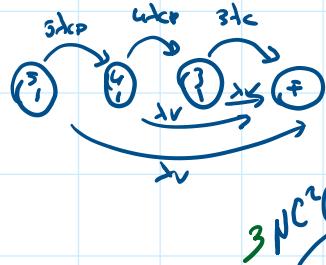
$$G_{\text{RC}} = A_{2/2} \cdot 0,02 + A_{1/2} \cdot 0,11 = 0,026$$

Costo 26 euro

Esercizio 1

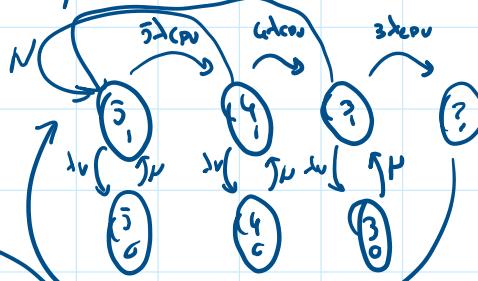


Reliability CPU



$$3\lambda C^2(1-C)$$

Availability CPU

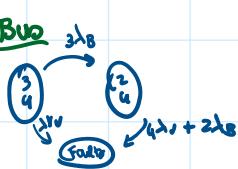


$$\binom{5}{2}$$

5.4.3.2

$$\frac{5!}{(5-2)! \cdot 2!} = \frac{120}{12} = 10$$

$$\frac{5!}{(5-3)! \cdot 3!} = \frac{120}{2 \cdot 6} = 10$$



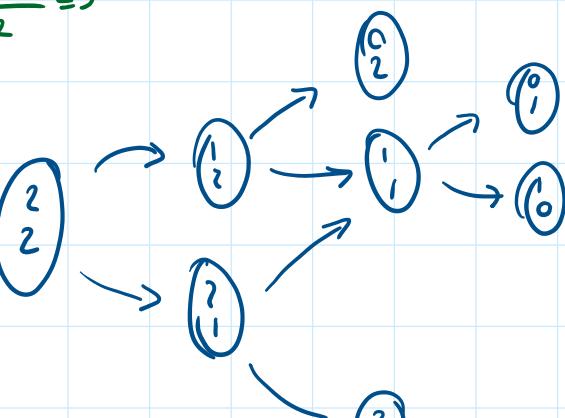
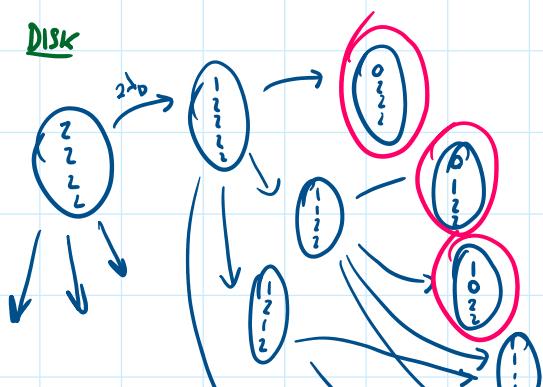
$$N(C)^3$$

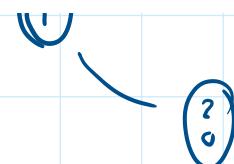
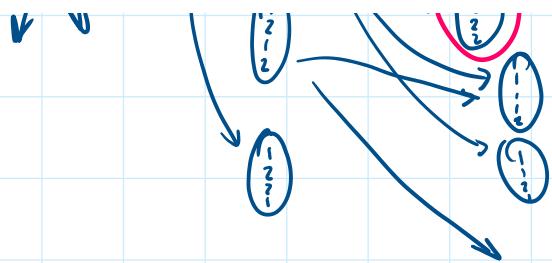
(2) quanti me vuo riporre
(1) quanti te de ve riaprire

$$\binom{3}{2} = \frac{6}{2}$$

$$\binom{3}{1} = \frac{6}{2} = 3$$

DISK





Esercizio 2



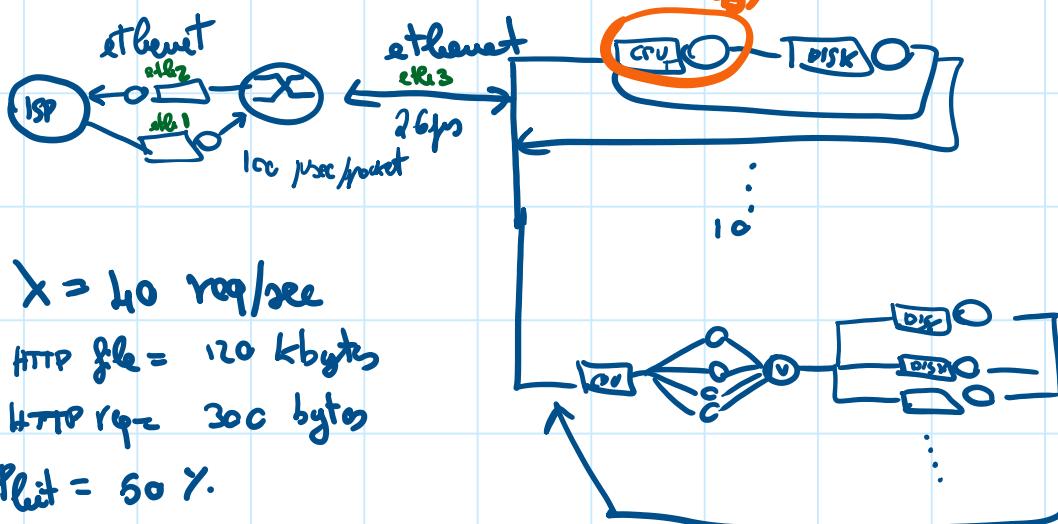
$$\begin{cases} P_0 \frac{7}{2} = P_1 N \\ P_1 \frac{6}{2} = P_2 2N \\ P_2 \frac{5}{2} = P_3 3N \\ P_3 \frac{4}{2} = P_4 3N \\ P_4 \frac{3}{2} = P_3 \end{cases}$$

$$P_0 = \frac{1}{[1 + 3.5 + 5.25 + 4.375]} = 0.05$$

$$\begin{aligned} P_1 &= 0.175 \\ P_2 &= 0.24 \\ P_3 &= 0.21 \\ P_4 &= 0.14 \\ P_5 &= 0.07 \end{aligned}$$

$$N = \sum_i i \cdot P_i$$

$$X = \sum_i \mu \cdot P_i$$



Networking

$$\Delta t_{link} = \frac{300 \cdot 10^3 + (3+1)(6 \cdot 10^{-3} + 0.1 \cdot 10^{-3} + 0.1 \cdot 10^{-3})}{0.5 \cdot 10^6} = 1.06 \cdot 10^{-6}$$

$$U_{eth1} = \lambda \cdot \Delta t_{link} = 4.45 \cdot 10^{-5}$$

$$R_{eth1} = \frac{D}{1-U} = 1.06 \cdot 10^{-6}$$

$$\text{Segmenti} = \frac{120K}{1000} = 83$$

$$\Delta t_{link} = \frac{(3+83)(0.1 \cdot 10^{-3} + 0.1 \cdot 10^{-3} + 0.1 \cdot 10^{-3}) + 120K}{0.5 \cdot 10^6} = 2.40$$

$$U_{eth2} = \lambda \cdot \Delta t_{link} = 9.96 \cdot 10^{-5}$$

~~$$R_{eth2} = \frac{D}{1-U} = 2.51 \cdot 10^{-4}$$~~

$$U_{router} = 0$$

$$D_{router} = ((83+3)+(4)) \cdot 100 \mu\text{sec} = 9 \cdot 10^{-3}$$

$$R_{router} = D_{router}$$

$$R_{link} = ((300 \cdot 10^3) + (4)(0.1 \cdot 10^{-3} + 0.1 \cdot 10^{-3} + 0.1 \cdot 10^{-3}) + 120K + 85(0.1 \cdot 10^{-3})) \cdot 1.5 = 9.41 \cdot 10^{-5}$$

$$D_{\text{idle},3} = \frac{((300 \cdot 10^{-3}) + (\alpha)(O_{\text{VCO}} + O_{\text{PLL}} + O_{\text{LO}}) + n_{\text{eK}} + 85(O_{\text{TTL}})) \cdot 1.5}{2 \cdot 10^5} = 9,44 \cdot 10^{-3}$$

$$U = \lambda \cdot D_{\text{idle},3} = 3,72 \cdot 10^{-3}$$

$$R = \frac{D}{1-U} = 9,44 \cdot b^{-3}$$

$$D_{\text{CPU}} = 20 \cdot 0.5 + 0.5 \cdot 40 = 30 \text{ min}$$

$$U_{\text{CPU}} = \frac{\frac{40}{60} \cdot 30}{10 \cdot 4} = 0.03$$

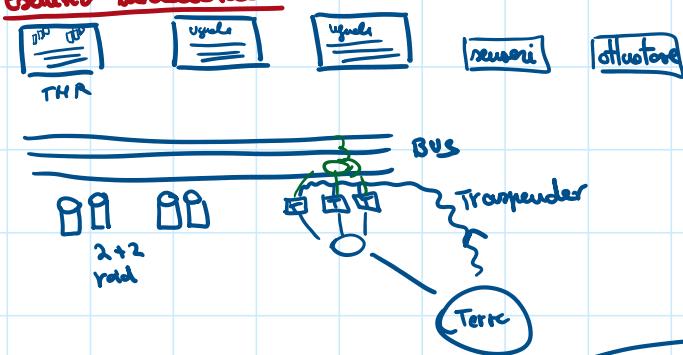
Computing node · 4 core

$$R_{\text{CPU}} = 0.03 \text{ sec}$$

$$D_{\text{FS}} = 0.5(25+20) = 22.5 \text{ min}$$

$$U_{\text{FS}} = \lambda \cdot D_{\text{FS}} = 0.5 \text{ billion sec}$$

Esercizio modellazione

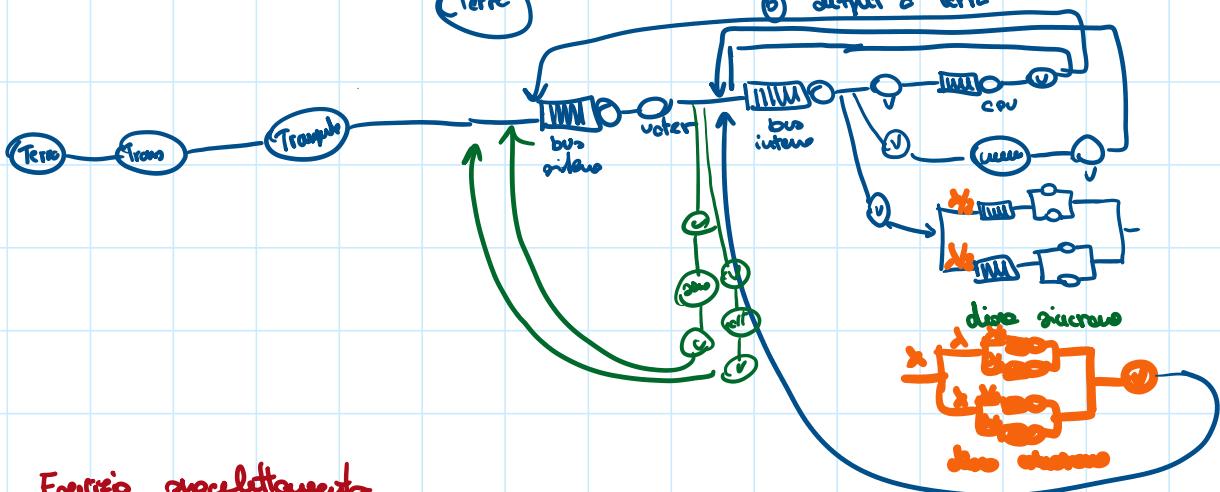


- ① canale da terra
- ② elaborazione con acquisizione dati (db + disk)

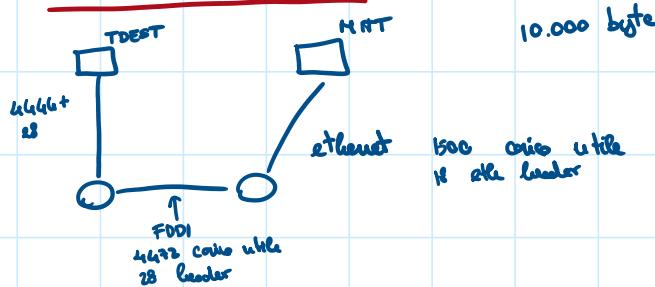
- ③ canale ad attuatori

- ④ acquisizione dati da sensori

- ⑤ output a terra



Esercizio spooling



Esame 2006-07-03

sabato 1 giugno 2019 13:08

Segmento TCP = 10.000

header size = 18 byte

bandwidth = 20 Kbyte/sec

Ipotizzo di non conoscere l'MTU

$$\frac{10000}{65535} = 0.15 \Rightarrow \text{① segmenti TCP}$$

$$\frac{10000 + \# \text{segmenti} \cdot \text{OvTCP}}{65535} = 0.15 \Rightarrow \text{① datagramma}$$

$$\frac{1000 + \# \text{segmenti} \cdot \text{OutTCP} + \# \text{datagram} \cdot \text{OvIP}}{1500} = 6,69 \Rightarrow \text{② frame}$$

$$[20 | 90 | 18 | 1460] + [18 | 1500] \times 6$$

Fisica 20/2/2013

sabato 1 giugno 2019 13:28

$$\lambda = 50 \text{ requests/second}$$

4 CPU working in parallel

Raid 1 disk (6+8)

Ethernet = 100 Mbit/s

Router delay = 100 nsec

Router-ISP = 1 Gigabit/sec

$$file_req = 600 \text{ bytes}$$

$$file = 100000 \text{ bytes}$$

$$S_{cpu} = 20 \text{ nsec} \times \text{request}$$

$$S_{time} = 10000 \text{ bytes} \approx 10 \text{ usec}$$

$$R = ?$$

bottleneck?

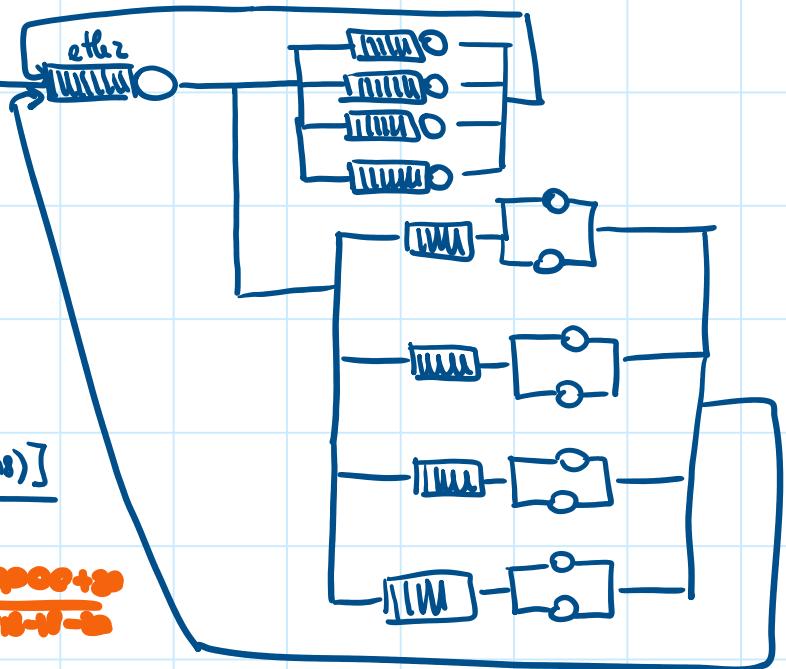


Hip: TCP handshaking and closing requires 3+3 messages

$$D_{disk} = V_{disk} \cdot 10 = 100 \text{ usec}$$

$$D_{eth1} = \frac{8 \left[400 + (1+3)(20+20+18) + 100000 + 4(20+18+10) \cdot 67(20+18) \right]}{\pm 10^3} = 0.83 \cdot 10^{-3} \text{ sec}$$

$\frac{100000 + 20}{1512 - 10 - 6}$



$$U_{eth1} = \lambda \cdot D_{eth1} = 0.061$$

$$R_{eth1} = \frac{D}{1-U} = \frac{0.838 \cdot 10^{-3}}{1-0.061} = 8.73 \cdot 10^{-4} \text{ sec}$$

$$R_{router} = D_{router} = \text{latency} \cdot (75) \approx 7.6 \cdot 10^{-6}$$

Eth2: 2 volte lo request + 1 volta il file

$$S_{eth2,req} = \frac{8 \left[(3+1)(20+20+18) + 600 \right]}{100 \cdot 10^6} = 5,05 \cdot 10^{-5} \text{ sec}$$

$$S_{eth2,file} = \frac{8 \left[(4)(20+20+18) + 67(20+18) + 100000 \right]}{100 \cdot 10^6} = 8.3 \cdot 10^{-5}$$

$$D_{eth2} = 2 \cdot 5,05 \cdot 10^{-5} \text{ sec} = 10,1 \cdot 10^{-5} \text{ sec}$$

$$D_{eth2,file} = 8.3 \cdot 10^{-5} \text{ sec}$$

$$D_{eth2} = 8.43 \cdot 10^{-5} \text{ sec}$$

$$U_{eth2} = \lambda \cdot D_{eth2} = 50 \cdot 8.43 \cdot 10^{-5} = 0.42 \text{ sec}$$

$$R_{eth2} = \frac{D}{1-U} = 0.814 \text{ sec}$$

$$R_{ETH2} = \frac{D}{1-U} = 0.014 \text{ sec}$$

$$U_{CPU} = \frac{\lambda}{4} \cdot D_{CPU} = \frac{50}{4} \cdot S_{CPU} = 0.25$$

$$R_{CPU} = \frac{0.025}{1-0.25} = 0.26$$

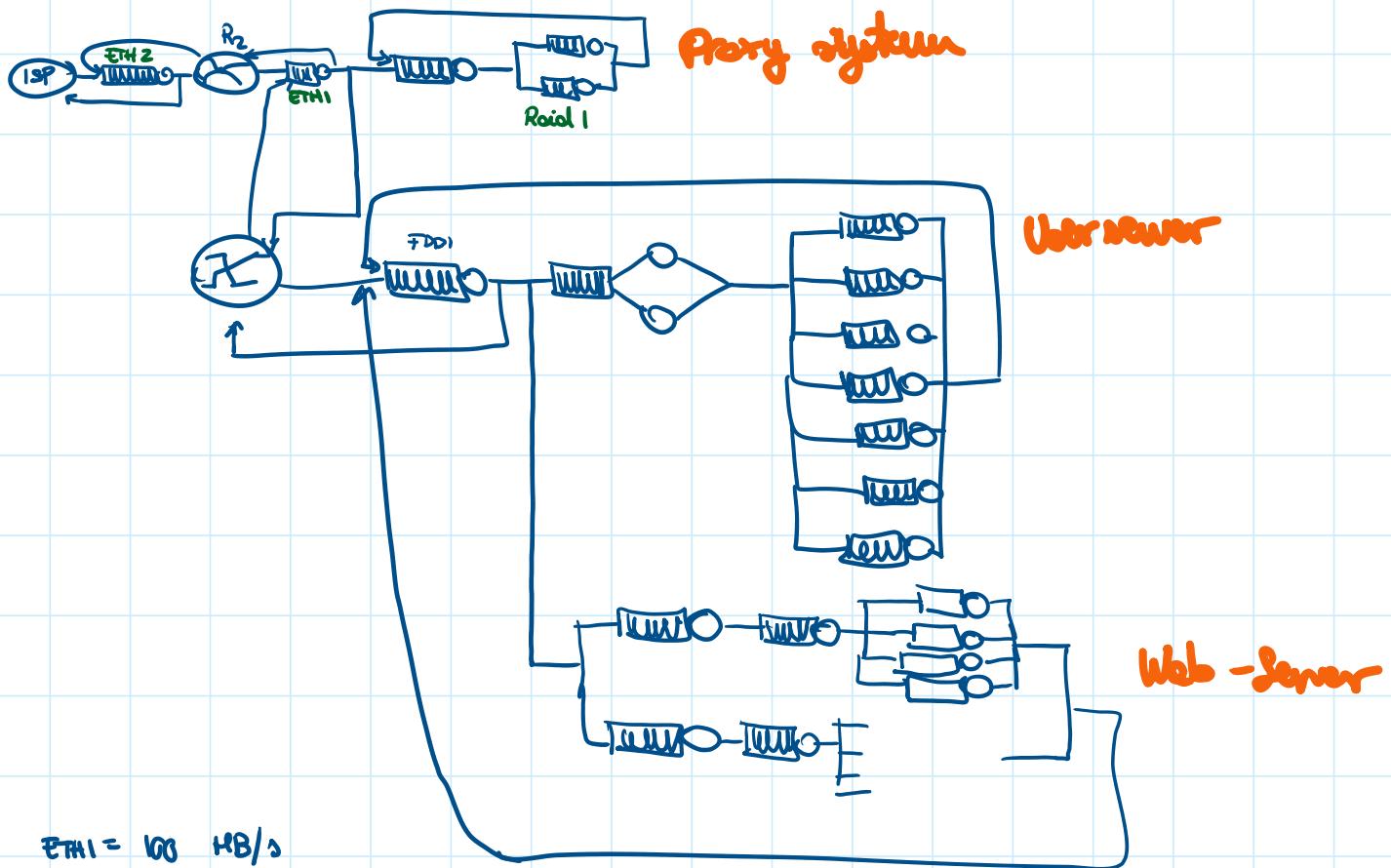
$$D_{CopyIO} = \frac{100}{2} \text{ msec} = 50 \text{ msec}$$

$$U_{CopyIO} = \frac{\lambda}{\alpha} \cdot D_{CopyIO} = 0.625 = U_{void}$$

$$R = \frac{D}{1-U} = 0.133$$

$$R_{sistema} = \sum R_i$$

$$\text{Bottleneck} = \underset{i \in I}{\operatorname{argmax}} \{U_i\} \quad \| \text{sottostima con } U \text{ più alta}$$



$$ETH1 = 100 \text{ MB/s}$$

$$FDDI = 300 \text{ MB/s}$$

$$\text{Router delay} = 1 \text{ ms}$$

$$ETH2 = 16$$

$$\text{Probabilità FS} = 30\%$$

$$\text{Prob WS} = 70\%$$

$$\text{Prob user cache} = 50\%$$

$$F_{\text{File-SERVER}} = 30 \text{ kbytes}$$

$$F_{\text{FILE WS}} = 200 \text{ kbytes}$$

$$\text{Request} = 400 \text{ bytes}$$

$$S_{\text{USER, CPU}} = 30 \text{ user}$$

$$S_{\text{USER, DISK}} = 30 \text{ user}$$

$$S_{\text{WEB, CPU}} = 50 \text{ user}$$

$$S_{\text{WEB, DISK}} = 50 \text{ user}$$

$$S_{\text{WEB, DISK}} = 60 \text{ user}$$

$$S_{\text{PROXY, CPU}} = 10 \text{ user}$$

$$S_{\text{PROXY, CPU, USER}} = 20 \text{ user}$$

$$ETH2 = \frac{\{(3+1) \cdot 58 + 400 + [(2+1) \cdot 58 + 30000] \cdot 0.3 + [(3+3) \cdot 58 + 200000] \cdot 0.7\} \cdot 0.8}{1 \cdot 10^3} = 1.24 \cdot 10^{-3} \text{ sec}$$

$$U_{ETH2} = \lambda \cdot D_{ETH2} = 3.72 \cdot 10^{-3}$$

$$R_{ETH2} = \frac{D_{ETH2}}{1-U} = 1.24 \cdot 10^{-3} \text{ sec}$$

$$R_{\text{ROUTER}} = \text{delay} \cdot \# \text{ packets} = 1 \cdot 10^{-3} \cdot (4 + 24 \cdot 0.3 + 14 \cdot 0.7) = 0.109 \text{ sec}$$

ETH1

$$D_{ETH1} = [4 \cdot 58 + 400] \cdot 0.3 + [24 \cdot 58 + 30000] \cdot 0.3$$

$$+ P_{\text{HT}} \cdot (4 \cdot 58 + 400 + (40 \cdot 58 + 200000)) + 2P_{\text{USER}} (4 \cdot 58 + 400 + 140 \cdot 58 + 200000) / 100 \cdot 10^6 = 2,28 \cdot 10^{-3}$$

$$U_{ETH1} = \lambda \cdot D_{ETH1} = 6,84 \cdot 10^{-3}$$

$$D_{ETH1} = \dots \approx 10^{-3}$$

$$U_{ETH1} = \lambda \cdot D_{ETH1} = 6,84 \cdot 10^{-3}$$

$$R_{ETH1} = D_{ETH1} / (1 - U_{ETH1}) = 4,13 \cdot 10^{-3}$$

FDDI

$$D_{FDDI} = [4,68 + 600 + 24,68 + 30000] \cdot 0,3 + ([4,68 + 600 + 206000 + 140 \cdot 68] \cdot 0,5) \cdot 0,7 = 1,65 \cdot 10^{-4}$$

$$U_{FDDI} = \lambda \cdot D_{FDDI} = 4,98 \cdot 10^{-4}$$

$$R_{FDDI} = \frac{D_{FDDI}}{1-U} = 1,66 \cdot 10^{-4} \text{ sec}$$

Proxy

$$D_{Proxy} = (10 \cdot p_{HTTP} + 20 \cdot p_{WWW}) \cdot 0,7 \approx 11 \cdot 10^{-3} \text{ sec}$$

$$U_{Proxy} = \lambda \cdot D_{Proxy} = 40 \cdot 10^{-3}$$

$$R_{Proxy} = 0,015 \text{ sec}$$

Filtersysteme

$$D_{FS} = 60 \text{ ms} \cdot 0,3$$

$$U_{FS} = \lambda \cdot D_{FS} = 0,056$$

$$R_{FS} = 0,063 \text{ sec}$$

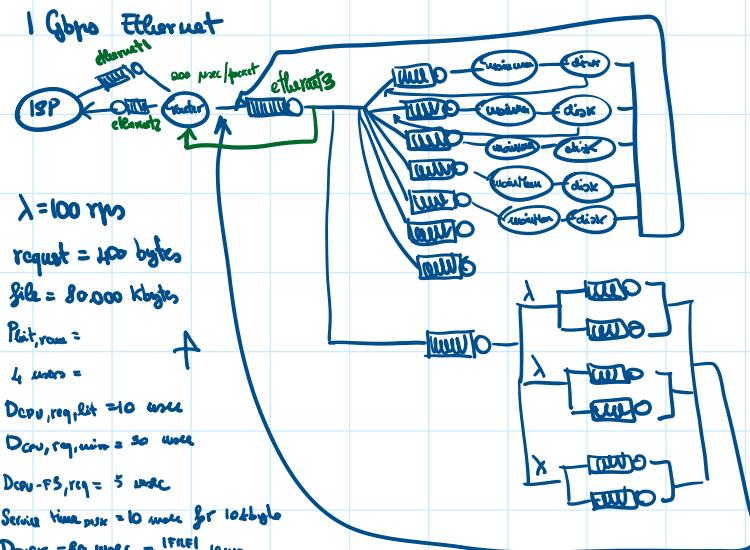
WebServer

$$D_{WebServer} = 50 + 30 + \frac{60}{4} = 80 \cdot 10^{-3} \text{ sec}$$

$$U_{WebServer} = 0,5 \cdot 0,7 \cdot \lambda \cdot D_{WebServer} = 0,047$$

$$R_{WebServer} = 0,034 \text{ sec}$$

$$R_{TOT} = \sum_i R_i$$



$$\underline{\text{ETH1}}$$

$$D_{\text{ETH1}} = \frac{[(2+1)(100+20+10) + 400] \cdot 10^6}{1 \cdot 10^3} = 5 \cdot 10^{-6}$$

$$U_{\text{ETH}} = \lambda \cdot D_{\text{ETH1}} =$$

$$P_{\text{ETH}} = \frac{U_{\text{ETH}}}{1-U} =$$

$$\underline{\text{ETH2}}$$

$$D_{\text{ETH2}} = \frac{[5(58) + 53(58) + 80.000]}{1 \cdot 10^3} = 6,38 \cdot 10^{-6}$$

dai tuoi conti
delle pds di lso Pe

$$\underline{\text{ETH3}}$$

$$D_{\text{ETH3}} = \frac{P_{\text{int}}((3+1)(58) + 100 + 5 \cdot 58 + 53(58) + 80.000) + 2P_{\text{wire}}((3+1)(58) + 100 + 5 \cdot 58 + 53(58) + 80.000)}{1 \cdot 10^3} = 6,73 \cdot 10^{-6}$$

$$\underline{\text{CPU}}$$

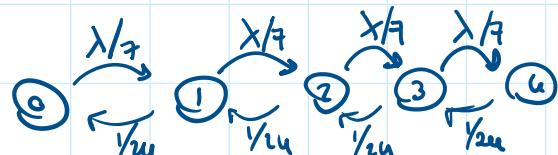
$$D_{\text{CPU}} = 10 \cdot 0,3 + 30 \cdot 0,7 = 24$$

CPU-FS

$$D_{\text{CPU-FS}} = 5 \mu\text{s}$$

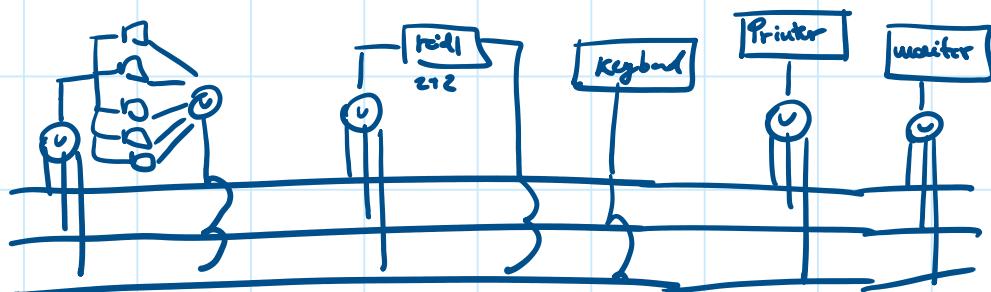
$$\underline{\text{DISK}}$$

$$D_{\text{disk}} = 80 \text{ msec/2}$$

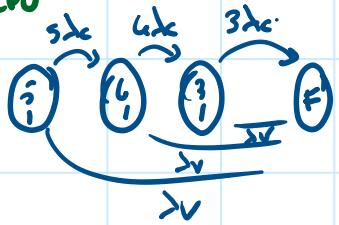
**Availability**

$$A_{\text{CPU}} = 1 - (1 - A_{\text{CPU}})^T$$

$$A_{\text{disk}} = (1 - (1 - A_{\text{disk}})^T)^k$$

Esercizio 1Preliminary

CPU



$$\dot{P}(s) = -P(s)(5\lambda_c + \lambda_v)$$

$$\dot{P}(t) = -P(t)(4\lambda_c + \lambda_v) + P(s)5\lambda_c$$

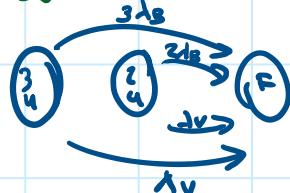
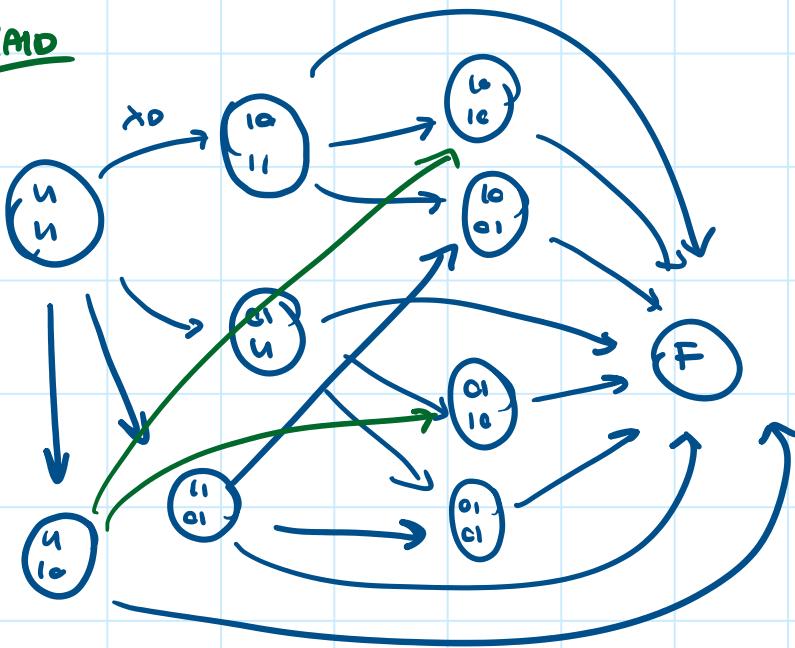
$$\dot{P}(s) = -P(s)(4\lambda_c + \lambda_v) + P(t)4\lambda_c$$

$$\dot{P}(F) = P(s)$$

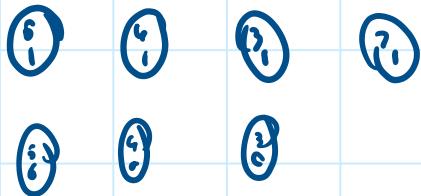
KPN



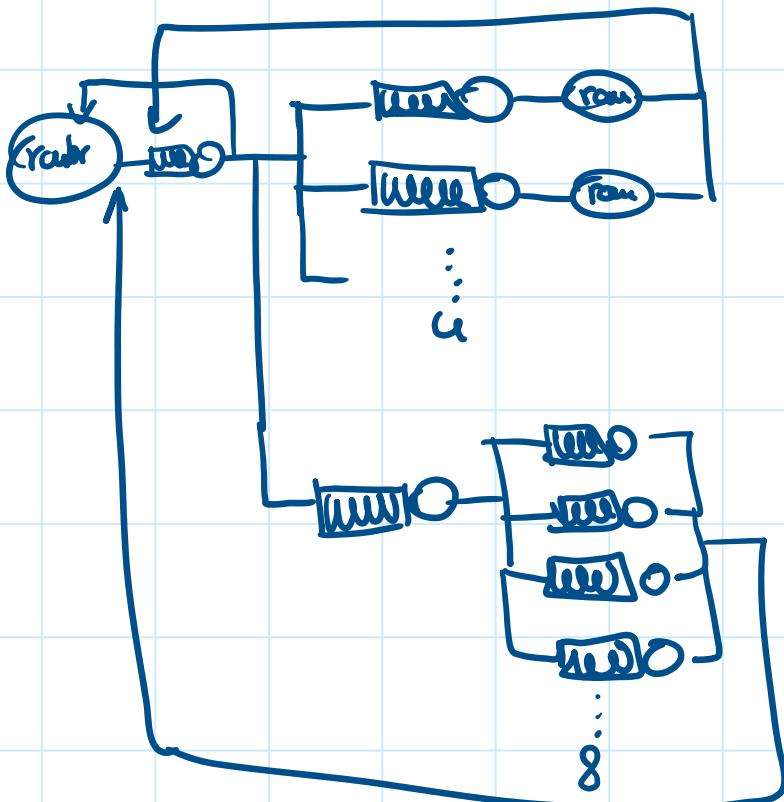
BUS + VOT

RAID

Availability



Esercizio 3



$$\lambda = 10^0 \text{ cps}$$

$$E_H = 26B/s$$

$$FILE = 10kbytes$$

$$Request = 500 \text{ bytes}$$

$$D_{CPU, HIT} = 5 \text{ ns}$$

$$D_{CPU, MISS} = 10 \text{ ns}$$

$$D_{CPU-FS} = 10 \text{ ns}$$

$$D_{FS} = 10 \text{ ns}$$

$$D_{CPU} = 0.5 \cdot (5 \text{ ns}) + 0.5(10) = 7.5$$

$$D_{L1H} = 0.5 \cdot 10 \text{ ns} = 5$$

$$D_{CPU-MISS} = 0.5 \cdot 10 \text{ ns} = 5$$

$$D_{MAX} = 7.5 \Rightarrow \frac{\lambda}{s} = 133$$

$$Data = [(3+1)(58) + 500 + 2(58) + 66(38) + 100.000] \text{ Plist}$$

$$+ 2 \text{ Pmiss } ((6) \cdot 58 + \text{ quello dentro al Plist})$$

$2 \cdot 10^9$

$$User = \frac{\lambda}{s} \cdot 7.5 \cdot 10^{-3} = 0.18$$

$$U_{\text{error}} = \frac{\lambda}{\alpha} \cdot 7 \cdot 5 \cdot 10^{-3} = 0.18$$

$$U_{\text{carries}} = \lambda \cdot 5 \cdot 10^{-3} = 0.5$$

$$U_{\text{disk}} = \frac{\lambda}{8} \cdot 5 \cdot 10^{-3} = 0.06$$

$$R_i = \frac{D_i}{1 - U_i}$$

Therayput = $\lambda \Rightarrow$ reute probabilità

$$\lambda = 300 \text{ mps}$$

$$1 \text{ request} = 600 \text{ bytes}$$

$$ETH = 1 \text{ Gbit}$$

$$FDDI = 2 \text{ Gbit}$$

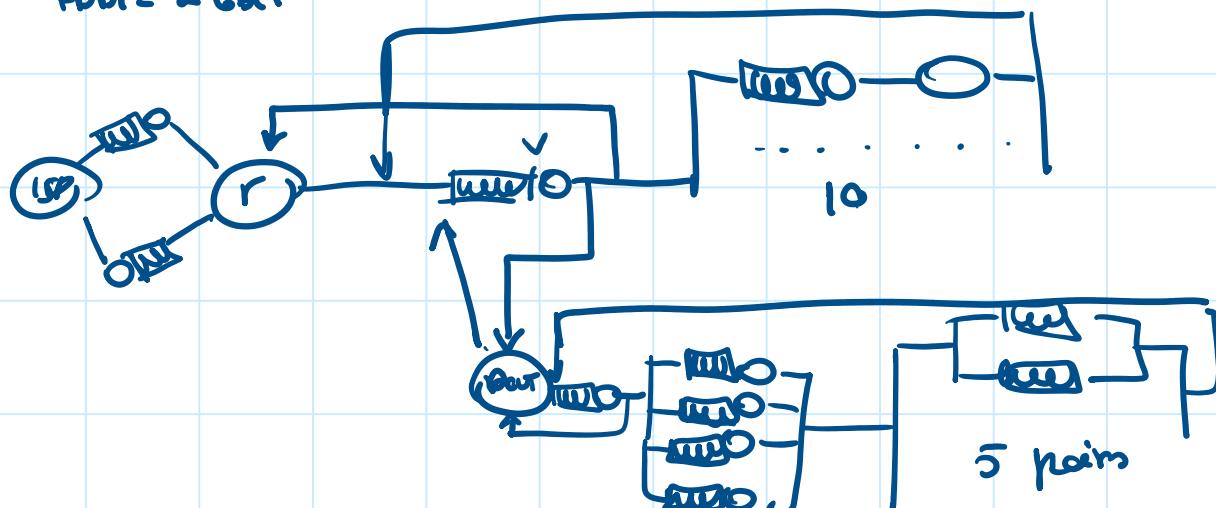
$$D_{CPU} = 10 \text{ ms}$$

$$D_{CPU, \text{min}} = 20 \text{ ms}$$

$$D_{CPU, \text{FS}} = 10 \text{ msec}$$

$$|FILE| = 100 \text{ kbytes}$$

$$P_{HIT} = 50\%$$



$$D_{link} = \frac{100.000}{10.000} \cdot \frac{1}{2} \cdot 10^{-3} = 5 \text{ sec}$$

$$D_{file} = \frac{8[400 + 4 \cdot 58]}{256 \cdot 10^6} = 1,97 \cdot 10^{-3} \text{ sec}$$

$$D_{file,out} = \frac{[100.000 + 68(20 \cdot 18) + 3 \cdot 58]8}{256 \cdot 10^6} = 3.21$$

$$R_{in} = \frac{D_{in}}{1 - D_{in}}$$

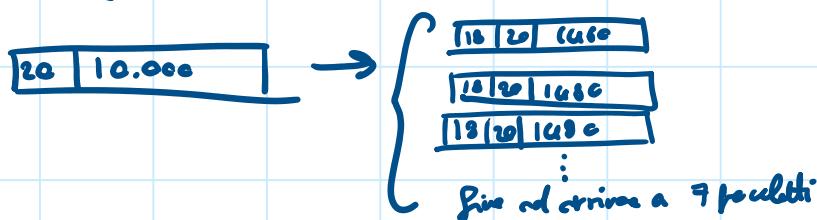
$$U_{in} = \lambda \cdot R_{in}$$

Esercizio 2

10.000 byte to send

ethernet = 18 bytes

$$\frac{10.000 + 20}{1680} = 6,7 \rightarrow 7 pacchetti$$



Alternative

Esercizio 2

TCP segment = 130.000

$$M. fragment = \frac{130.000}{65535} = 1.7 \cdot 2$$

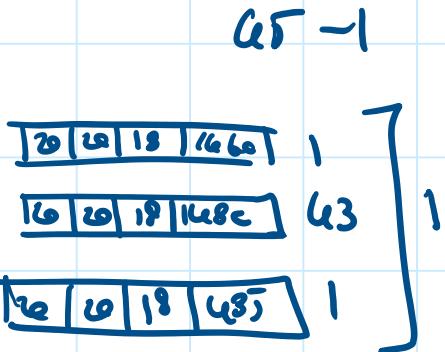
$$M. dettagli = \frac{130.000 + 2 \cdot 10}{1480} = 98 \text{ pacchetti}$$

20 | 65535

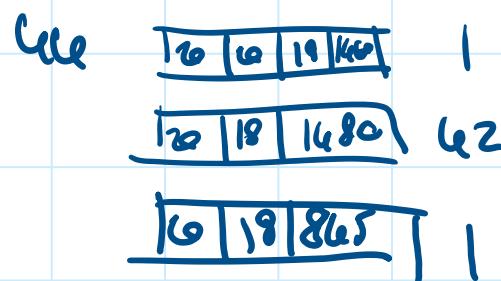
18 | 64465



$$\frac{65535 + 20}{1480}$$

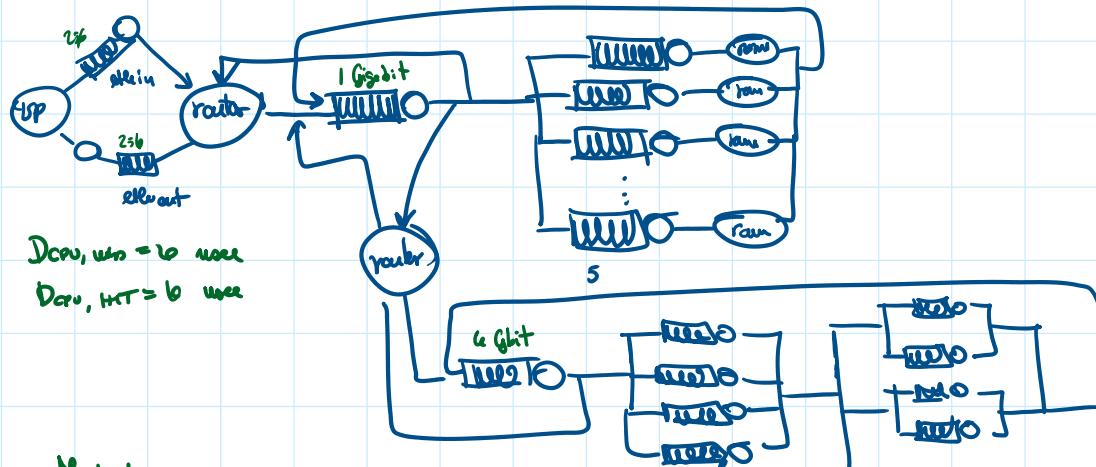


$$\frac{64465 + 20}{1480}$$



$$\underline{2(58) + 97(38) + 130.000}$$

$\lambda = 100 \text{ rps}$
 $|request| = 100 \text{ bytes}$
 $|file| = 200 \text{ kbytes}$



Monitor



$$D_{\text{in}} = 0.7 \cdot 10 + 0.3 \cdot 6 = 7 + 6 = 13 \text{ user}$$

$$\mu = \sqrt{13 \cdot 10^{-3}} = 3.6$$

$$\begin{cases} P_0 \lambda / s = P_1 N \\ P_1 \lambda / s = P_2 N \\ P_2 \lambda / s = P_3 N \\ \sum P_i \end{cases}$$

$$P_0 = 0,75 \\ P_1 = 0,18 \\ P_2 = 0,04 \\ P_3 = 0,01$$

Efficienza

$$D_{\text{out}} = \frac{(3+1)58 + 600}{236 \cdot 10^6} = 2,46 \cdot 10^{-6}$$

$$U_{\text{in}, \text{out}} = \lambda \cdot 2,46 \cdot 10^{-6} = 7,46 \cdot 10^{-6}$$

$$R = \frac{D}{U-1}$$

Router

$$m = (1-P_3)(4 + (4 \cdot 3 + 3)) + P_3(4) = 161$$

$$D = 1 \cdot 4 \cdot 10^{-3}$$

$$R = D$$

Re

Efficienza

$$D = \frac{3 \cdot 58 + 4 \cdot 20 + (45 \cdot 3 + 3)(38) + 200000}{236 \cdot 10^6} = 8,02 \cdot 10^{-4}$$

$$U = (P_{\text{out}} ((1-P_3) \cdot \lambda \cdot D) + P_{\text{in}, \text{out}} ((1-P_3)^2 \cdot \lambda \cdot D)) = 0,078$$

$$R = \frac{D}{U-1}$$

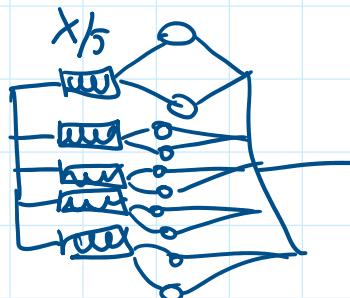
Elementi int.

$$D = \left[P_{\text{out}} (400 + (4 \cdot 38) + (1-P_3)(4 \cdot 20 + 4 \cdot 58 + (4 + (4 \cdot 3 + 3))38 + 200.000)) + 2P_{\text{in}, \text{out}} ((1-P_3)(400 \cdot 4 \cdot 58 + 4 \cdot 3 \cdot 38 + 4 \cdot 20 \cdot 4 \cdot 58) + P_3(400 \cdot 4 \cdot 38)) \right] \cdot 8$$

$$U = \lambda \cdot D \cdot 1 \cdot 10^{-3}$$

$$R =$$

Dire



$$R =$$

CPU

$$D = (1 - P_B) (P_{win} \cdot 20\text{ms} + P_{err} \cdot 10) =$$

$$U = \lambda \cdot D =$$

$$R = \frac{D}{1-U}$$

Disk

$$D = \frac{200000}{2 \cdot (20000)} \cdot 10\text{ms} = 50\text{ ms}$$

$$U = (P_{win}) (1 - P_B) D \cdot \lambda = 1.5$$

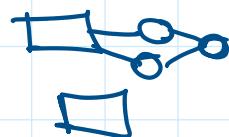
$$R =$$

FDDI

$$D = P_{idle} ((1 - P_B) (400 \cdot 4.58 + 4 \cdot 20 \cdot 3 \cdot 58 + (45 \cdot 3 + 3) \cdot 38) \cdot 8)$$

$$U = \lambda \cdot D = 6 \cdot 10^5$$

$$R = \frac{D}{1-U}$$



1649040

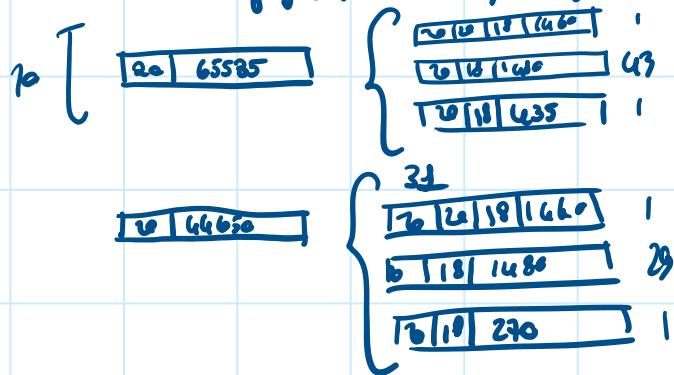
$$D = 0.5 \cdot (40)$$

$$10 \cdot 20$$

Esercizio 2

fig = rock

Elettronut

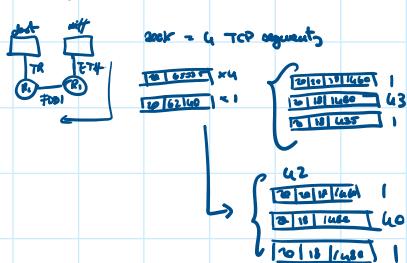


$$10(58 + 38 \cdot 46 + 65535) + (58 + 38(30) + 44650)$$

20 · left

Esercizio 2

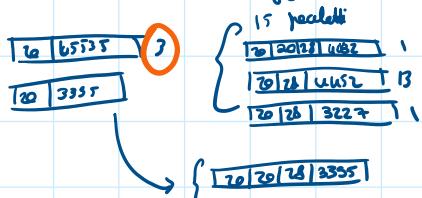
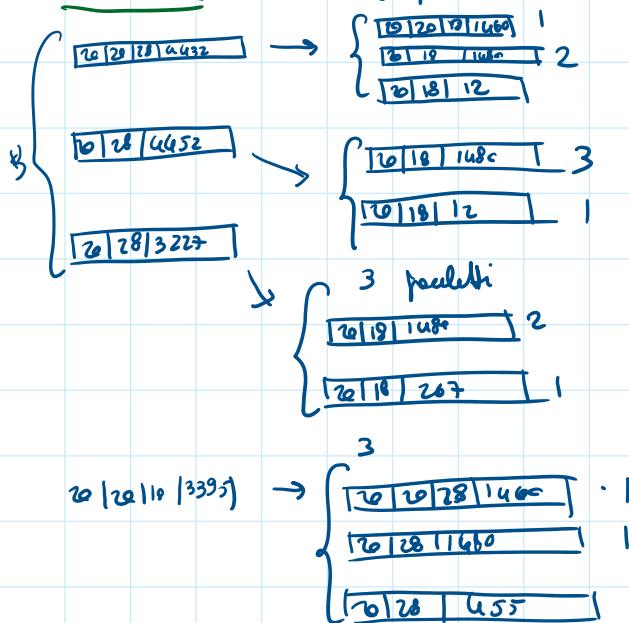
200.000



Su FDDI è TR switching client header con 28

invertiamo l'ordine

20.000 TCP fragment = 4 fragmenti

Ethernet LevelEsercizio 11.3

$$\bar{R} = ?$$

M/M/1/3/5



Service rate = 10 sec

$$\begin{cases} P(0) \frac{5}{4} = P_1 N \\ P(1) \frac{4}{4} = P_2 N \\ P(2) \frac{3}{4} = P_3 N \\ \sum_i P_i = 1 \end{cases}$$

$$P_0, P_1, P_2, P_3$$

$$N = \sum_i i \cdot P_i$$

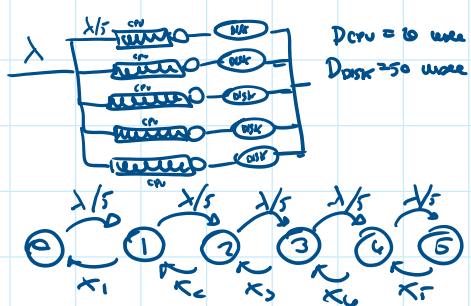
$$X = \sum_i N_i \cdot P_i$$

$$R = \frac{N}{X}$$

Esercizio 11.4

Esercizio 11.4

$\lambda = 25 \text{ rms}$ cluster da 5 server



Caso $n=1$

$$R_{CPU} = 22 \text{ ms}$$

$$R_{Disk} = 50 \text{ ms}$$

$$X_{TOT} = \frac{1}{\lambda} = 16.28$$

$$N_{CPU} = 0.28$$

$$N_{Disk} = 0.314$$

Caso $n=7$

$$R_{CPU} = 10(1 + 0.28) = 25.6$$

$$R_{Disk} = 50(1 + 0.28) = 64 \quad \dots$$

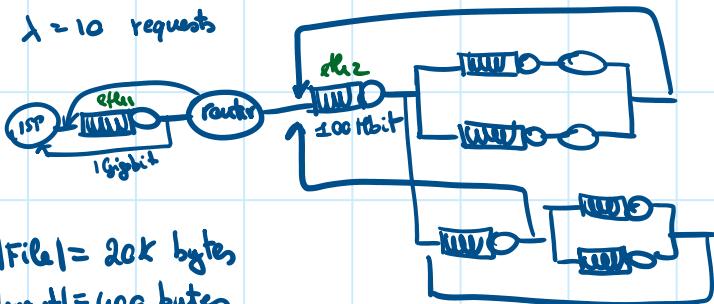
$$X_{TOT} = \frac{2}{\lambda} = 18$$

$$N_{CPU} = 0.46$$

$$N_{Disk} = 1.53$$

$$\begin{cases} P_0 \cdot \lambda/5 = P_1 X_1 \\ P_1 \cdot \lambda/5 = P_2 X_2 \\ P_2 \cdot \lambda/5 = P_3 X_3 \\ P_3 \cdot \lambda/5 = P_4 X_4 \\ P_4 \cdot \lambda/5 = P_5 X_5 \end{cases}$$

$$\bar{X} = A_{5 \text{ same}} (P_1 \cdot X_1 + P_2 \cdot X_2 \dots) + \binom{5}{1} (A)^4 (1-A) (P_1 \cdot X_1 + P_2 \cdot X_2 \dots) + \binom{5}{2} (A)^3 (1-A)^2 (P_1 \dots) + \binom{5}{3} (A)^2 (1-A)^3 (P_1 \dots) + \binom{5}{4} (A) (1-A)^4 (P_1 \dots)$$



$$|\text{File}| = 20 \text{ k bytes}$$

$$|\text{request}| = 400 \text{ bytes}$$

$$D_{\text{CPU-FS}} = 10 \text{ msec}$$

$$D_{\text{CPU}} = 20 \text{ msec}$$

$$D_{\text{ISP}} = 10 \text{ msec}$$

$$d_{\text{max}} = 20 \text{ msec}$$

$$P_{\text{miss}} = 0.5$$

$$P_{\text{hit}} = 0.5$$

$$\text{MTTF} = 40.000 \text{ hours}$$

$$\text{MTTR} = 1 \text{ hour}$$

Delle =

$$D_{\text{elle}} = \frac{8[4.58 + 400 + 6.58 + 13(38) + 20.000]}{1 \cdot 10^3} = 1.7 \cdot 10^{-4}$$

$$U = 1.7 \cdot 10^{-3}$$

$$R = \frac{D}{1-U} = 1.7 \cdot 10^{-4}$$

$$6.58 + 15(2.58 + 400 + 20000 + 13 \cdot 38)$$

Router

$$m = 21 \text{ packets}$$

$$D = 20 \cdot \text{delay} = 2.1 \cdot 10^{-3}$$

$$D_{\text{elle}} = \frac{6.58 + 15(2.58 + 400 + 20000 + 13 \cdot 38)}{P_{\text{hit}}(1.58 + 400 + 4 \cdot 58 + 13(38) + 20000) + 2P_{\text{miss}}(1.58 + 400 + 1.58 + 13(38) + 20000)} = 2.55 \cdot 10^{-3}$$

$$U = 10 \cdot 2.55 \cdot 10^{-3} = 2.55 \cdot 10^{-2}$$

$$R = \frac{2.55 \cdot 10^{-3}}{1 - 2.55 \cdot 10^{-2}} = 2.61 \cdot 10^{-3}$$

CPU

$$D_{\text{CPU}} = 0.5 \cdot 10 + 0.5 \cdot 20 = 15$$

$$U = 10 \cdot 15 \cdot 10^{-3} = 75 \cdot 10^{-3}$$

$$R = \frac{15 \cdot 10^{-3}}{1 - 75 \cdot 10^{-3}} = 0.01 \text{ sec}$$

CPU-FS

$$D = 0.5 \cdot 10 \text{ msec} = 5 \cdot 10^{-3} \text{ msec}$$

$$U = 10 \cdot 5 \cdot 10^{-3} = 0.05$$

$$R = \frac{5 \cdot 10^{-3}}{1 - 0.05} = 5.26 \cdot 10^{-3}$$

FS

$$D_{\text{disk}} = 0.5 \cdot 10 \text{ msec} = 10 \cdot 10^{-3} \text{ msec}$$

$$U = 0.5 \cdot 10 \cdot 10 \cdot 10^{-3} = 0.05$$

$$R = \frac{D}{1-U} = 0.010 \text{ sec}$$

$$U = 0.5 \cdot 10 \cdot 10 \cdot 10 = 500$$

$$R = \frac{D}{U} = 0.010 \text{ m}$$