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Dependable Distributed Systems Master of Science in Engineering in Computer Science

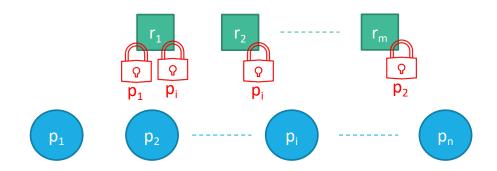
AA 2023/2024

LECTURE 5: DISTRIBUTED MUTUAL EXCLUSION

## Recap - The Mutual Exclusion Problem

#### Let us consider

- a set of processes  $\Pi = \{p_1, p_2, ... p_n\}$
- a set of resources R= {r<sub>1</sub>, r<sub>2</sub>, ... r<sub>m</sub>}



#### **PROBLEM**

 Processes need to access resources exclusively and we need to design a distributed abstraction that allows them to coordinate to get access to resources

## Recap - System Model

#### Let us consider

- a set of processes  $\Pi = \{p_1, p_2, ... p_n\}$
- a set of resources R= {r<sub>1</sub>, r<sub>2</sub>, ... r<sub>m</sub>}
  - For the sake of simplicity let us assume |R| = 1

The system is asynchronous

Processes are not going to fail (they will be always correct)

Processes communicate by exchanging messages on top of perfect point-to-point links

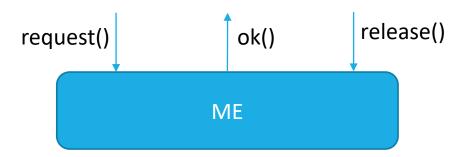
## Recap - The Mutual Exclusion abstraction

#### **EVENTS**

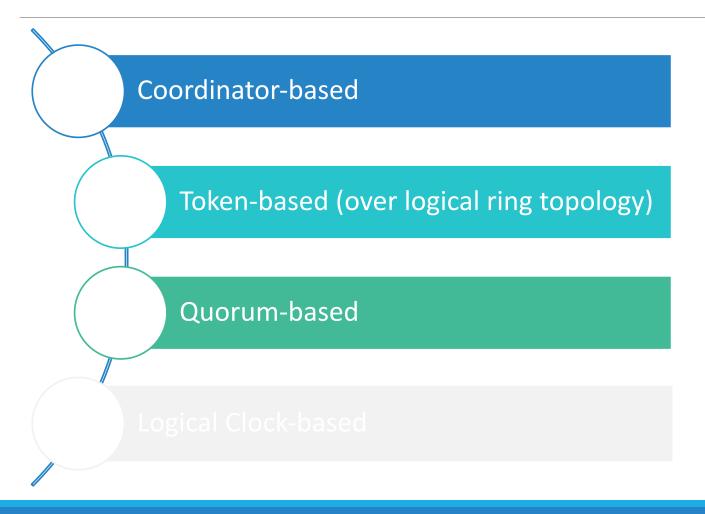
- request (): it issues a request to enter into the critical section
- ok(): it notifies the process that it can now access the critical section
- release(): it is invoked to leave the critical section and to allow someone else to enter

#### **PROPERTIES**

- Mutual Exclusion: at any time t, at most one process p is running the critical section
- No-Deadlock: there always exists a process p able to enter the critical section
- No-Starvation: every request() and release() operation eventually terminate



## Recap - Different Approaches to Distributed Mutual Exclusion



## Coordinator-based Distributed Mutual Exclusion

#### **BASIC IDEA**

• There exist a special process (i.e., a coordinator) that collects requests and grant permission to enter into the critical section

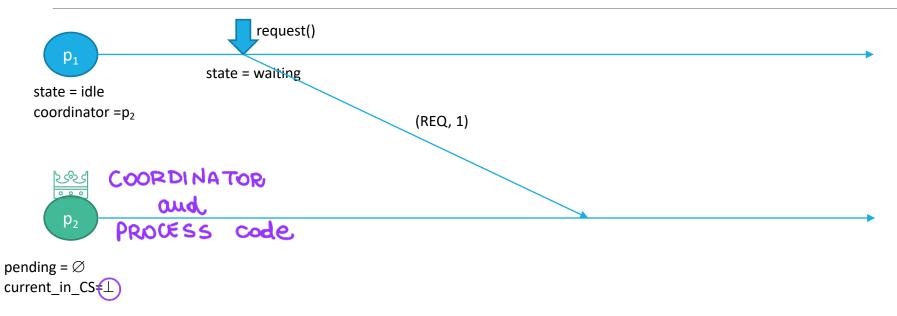
```
Init
state = idle
coordinator = getCoordinatorId()

upon event request()
    state = waiting
    trigger pp2pSend(REQ, i) to coordinator

upon event pp2pDeliver(GRANT_CS)
    state = CS
    trigger ok()

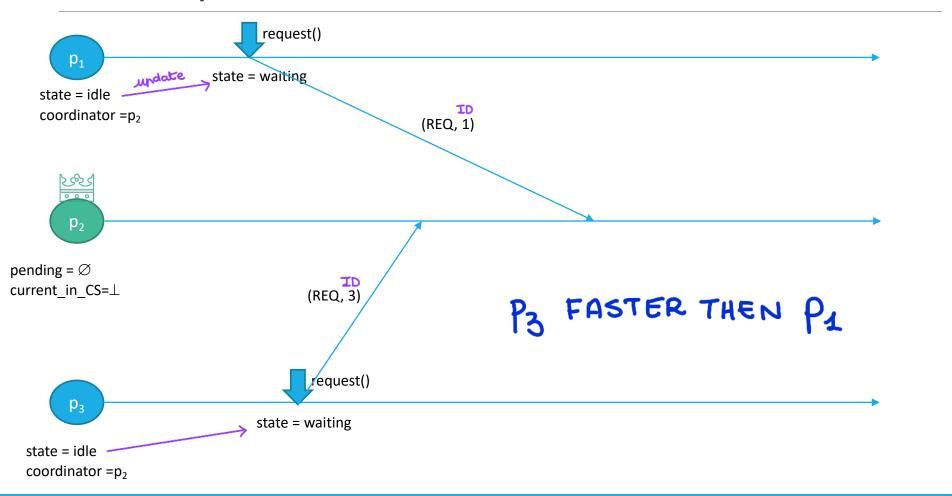
upon event release()
    state = idle
    trigger pp2pSend(REL, i) to coordinator
```

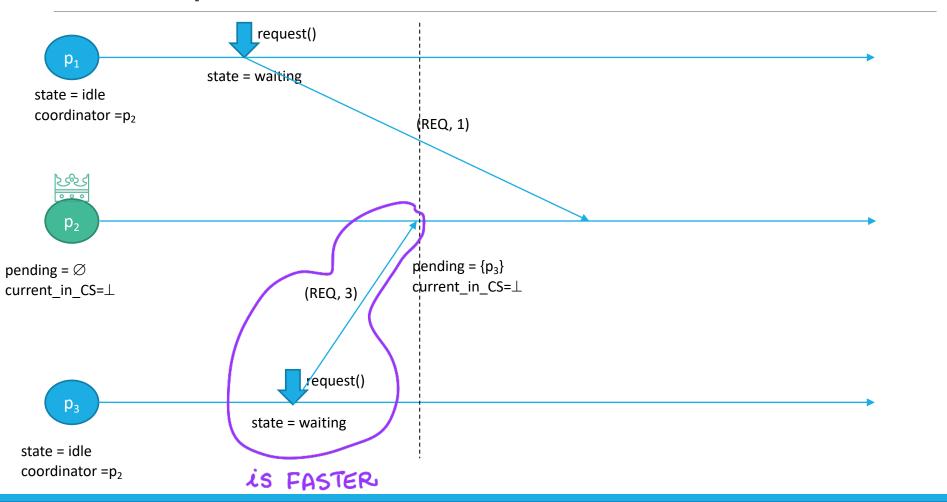
```
buffer to stone nequest
Init
pending = \emptyset
current_in_CS=(1) empty
upon event pp2pDeliver(REQ, j) from pi
              pending = pending \cup \{p_i\}
when pending \neq \emptyset and current in CS=\perp
              candidate=select process (pending)
              pending = pending \ candidate
              current in CS = candidate
              trigger pp2pSend(GRANT CS) to candidate
upon event pp2pDeliver(REL, j) from p<sub>i</sub>
             if current in CS = j
                           current in CS = \bot
```

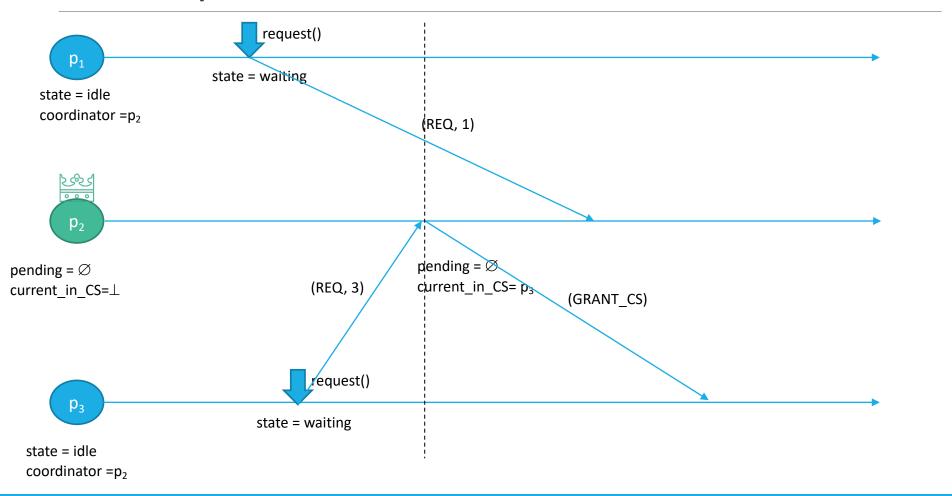


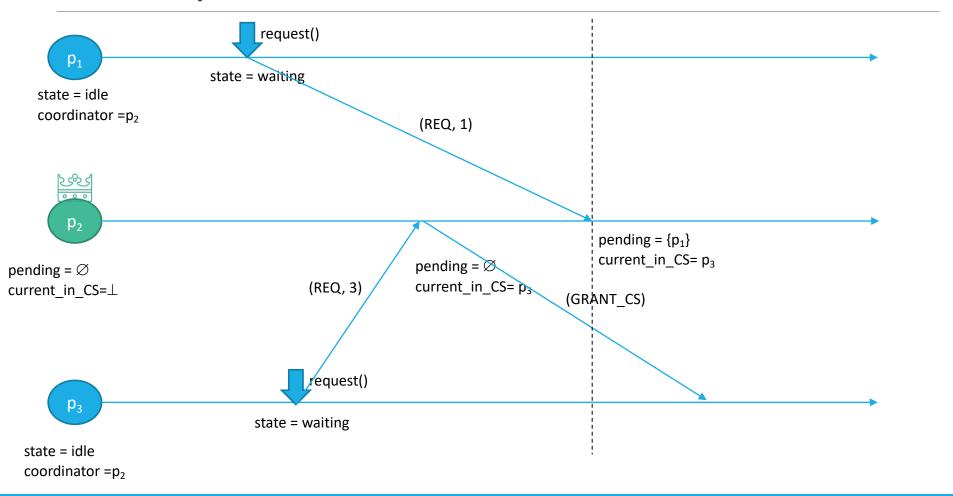
p<sub>3</sub>

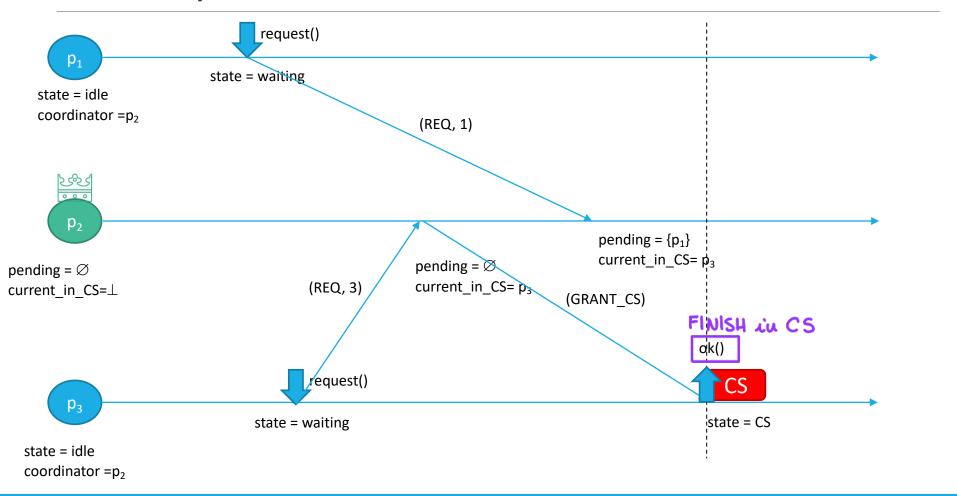
state = idle coordinator =p<sub>2</sub>

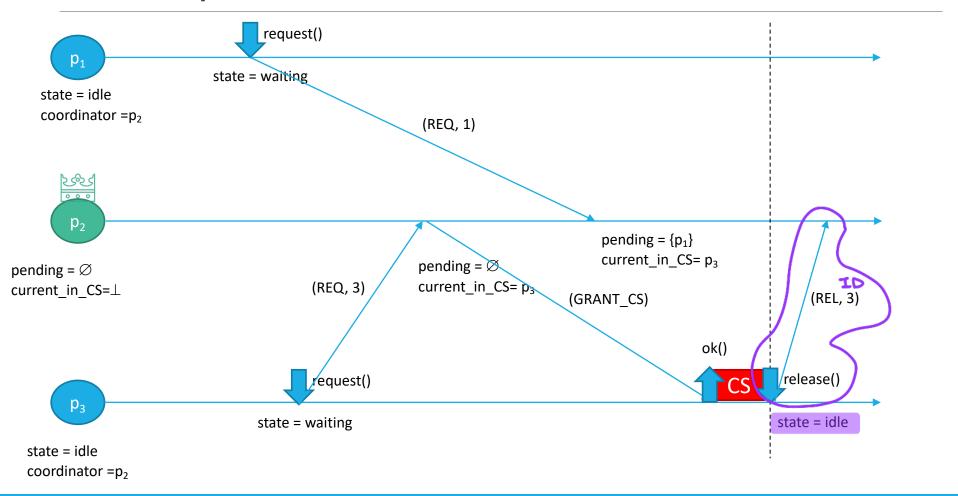


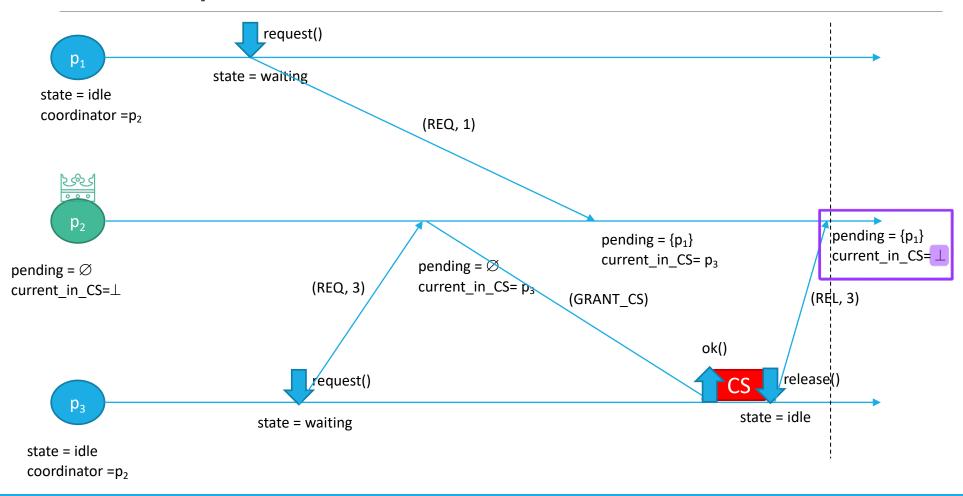


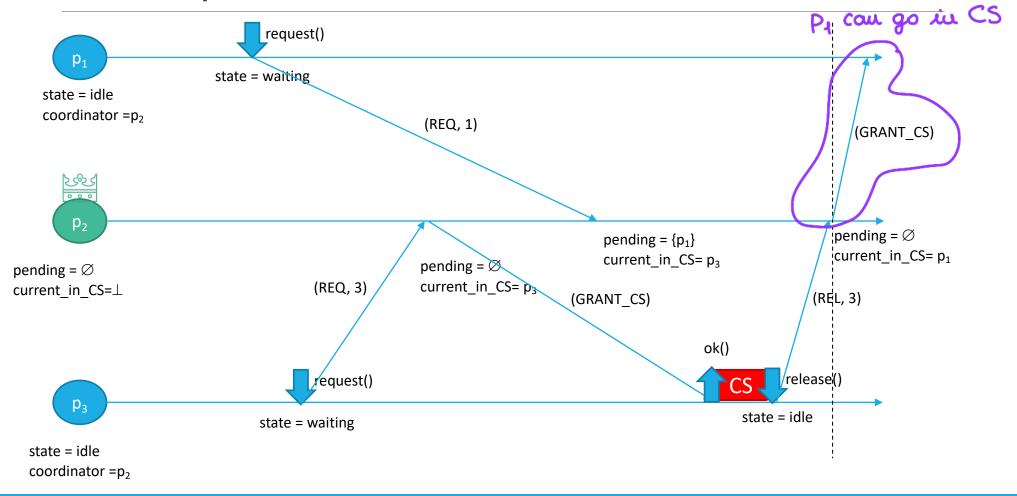


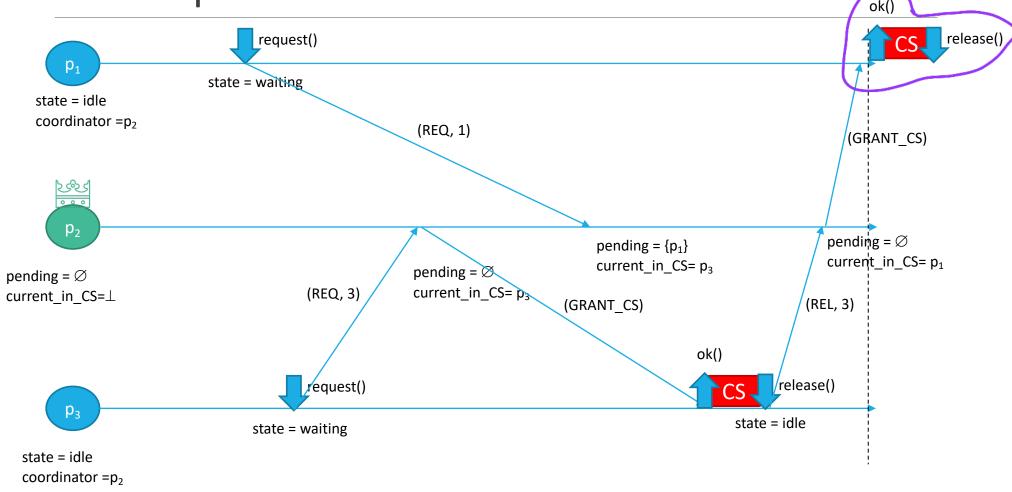










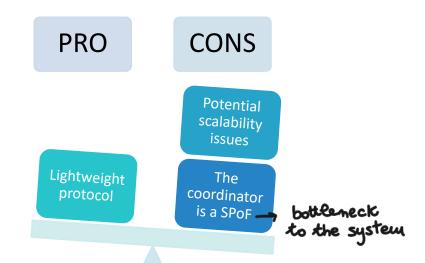


### Discussion

#### **PERFORMANCE**

cheaper -> complexity: 2

- entering the CS always requires 2 messages (i.e., REQ and GRANT) taking one RTT
- releasing the CS only requires 1 message
  - such message represent the delay between two different accesses to the CS



#### **BASIC IDEA**

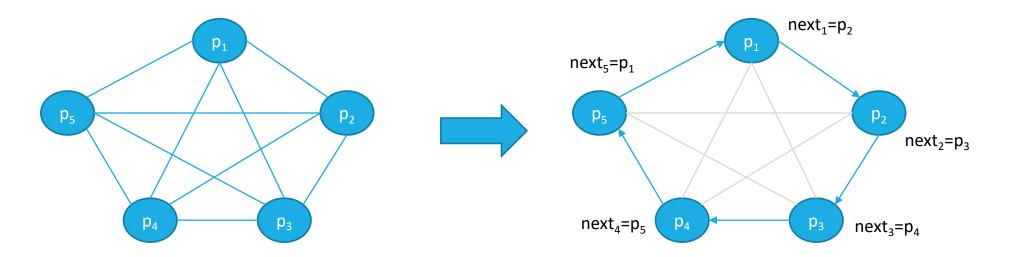
- a process interested to the CS can access it only when it receives a token
- The token is unique and it is exchanged between processes
- to guarantee fairness, we can exploit a structured logical topology (i.e., a ring) for exchanging messages related to the mutual exclusion protocol

#### INTUITION OF THE ALGORITHM

- 1. we construct an overlay (i.e., a logical network) as a ring exploiting existing point-to-point communication channels
- 2. A token is created and inserted in the ring during the initialization phase (i.e., it is assigned to a process of the system)
- 3. When a process requests the CS
  - a. it waits until it gets the token
  - b. enter the CS and upon release it sends the token to its next on the ring
- 4. If a process receives the token and it is not interested in the CS, it simply passes it to the next in the ring

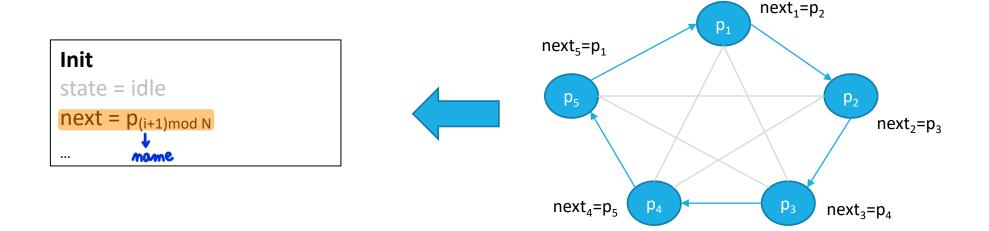
#### INTUITION

- 1. we construct an overlay (i.e., a logical network) as a ring exploiting existing point-topoint communication channels
  - The ring is obtained by:
    - storing in a local variable the name of the next process in the ring and
    - allowing the communication only with the next



#### INTUITION

- 1. we construct an overlay (i.e., a logical network) as a ring exploiting existing point-topoint communication channels
  - The ring is obtained by:
    - storing in a local variable the name of the next process in the ring and
    - allowing the communication only with the next



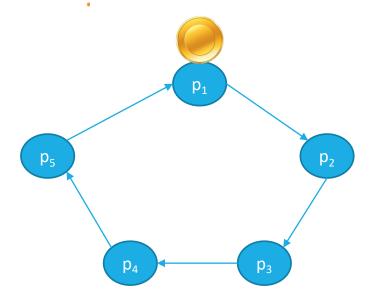
#### INTUITION OF THE ALGORITHM

2. A token is created and propagated in the ring during the initialization phase (i.e., it is assigned to a process of the system)

WARNING: The token must be unique to guarantee mutual exclusion

Only one process (selected trough a deterministic function) can create the token

during the init



```
Init

state = idle

next = p<sub>(i+1)mod N</sub>

if self = p<sub>0</sub> smallest identifies

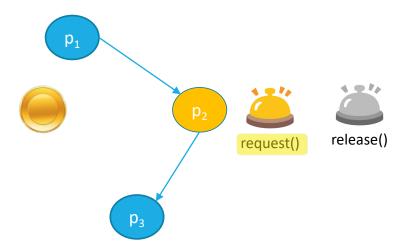
trigger pp2pSend(TOKEN) to next
```

#### INTUITION OF THE ALGORITHM

- 3. When a process requests the CS
  - a. it waits until it gets the token
  - b. enter the CS and upon release it sends the token to its next on the ring

4. If a process receives the token and it is not interested in the CS, it simply passes it to

the next in the ring



```
upon event request()
state = waiting

upon event pp2pDeliver(TOKEN)
if state == waiting
state = CS
trigger ok()
else
trigger pp2pSend(TOKEN) to next

upon event release()
state = idle
trigger pp2pSend(TOKEN) to next
```

## Token-based Algorithm on Logical Ring PROCESSES DON'T FAIL

```
Init
state = idle
next = p_{(i+1) \mod N}
if self = p_0
            trigger pp2pSend(TOKEN) to next
upon event request()
             state = waiting
upon event pp2pDeliver(TOKEN)
             if state == waiting
                         state = CS
                         trigger ok()
             else
                         trigger pp2pSend(TOKEN) to next
upon event release()
            state = idle
            trigger pp2pSend(TOKEN) to next
```

## Discussion

The algorithm continuously consume communication resources (even if no one is interested to the CS)

The delay experienced by every process between the request and the grant varies between 0 (it just receives the token) and N messages (it just forwarded the token)

## Quorum-based Algorithm – Maekawa's voting algorithm

#### **BASIC IDEA**

 to enter the CS every process waits to get the acknowledgement only by a subset of processes large enough to guarantee conflicts

#### Each process p<sub>i</sub> has associated a *voting set* V<sub>i</sub>

- Voting sets must satisfy the following properties
  - $\circ$   $p_i \in V_i$
  - $\lor$  V<sub>i</sub>, J, V<sub>i</sub>  $\cap$  V<sub>i</sub> ≠ Ø (i.e., there is at least one common member for each pair of voting sets)
  - $|V_i| = K$  (voting sets have all the same size for fairness same load principle)
  - each p<sub>i</sub> is contained in M voting sets (same responsibility principle)

## Quorum-based Algorithm – Maekawa's voting algorithm

```
Init
state = released > not interested in CS
voted = false
Vi = get_voting_set(i) HOW TO INPLEMENT IT
replies = 0 -> who say 465 on No
pending = \emptyset
upon event request()
             state = wanted - waiting
             for each p_i \in (V_i \setminus p_i) do
            trigger pp2pSend(REQ, i) to p
            not myself
upon event pp2pDeliver(REQ, j)
             if state == held OR voted == true
                    lambda cs pending = pending \cup {i}
             else
                          trigger pp2pSend(ACK, i) to p<sub>i</sub>
                          voted = true
```

```
upon event pp2pDeliver(ACK, j)
              replies = replies \cup {j}
when |replies| == |V_i|-1 voting set -1
              state = held
upon event release()
              state = released
              replies = \emptyset
              for each p_i \in (V_i \setminus p_i) do v_i \in V_i \setminus p_i do v_i \in V_i \setminus p_i
                            trigger pp2pSend(REL, i) to p<sub>i</sub>
upon event pp2pDeliver(REL, j)
              if |pending| > 0
                            candidate=select next(pending)
                  pending = pending \candidate
                   trigger pp2pSend(ACK, i) to candidate
                            voted = true
              else
                            voted = false
```

## Quorum-based Algorithm – Maekawa's voting algorithm

CHALLENGE: How to compute the values K and M to balance load and responsibilities?

- Maekawa showed that the optimal solution which minimize k and allows to get ME is having
  - $\circ$  K  $\sim \sqrt[2]{N}$
  - M = K
- An approximation to define  $V_i$  is having sets such that  $|V_i| \sim 2\sqrt[2]{N}$  defined as follows
  - Place processes in a matrix of size  $\sqrt[2]{N}$  x  $\sqrt[2]{N}$
  - for each p<sub>i</sub>, let V<sub>i</sub> be the union of the rows and columns containing p<sub>i</sub>

Let us consider a system composed by N = 4 processes

• 
$$(M = K \sim \sqrt[2]{4} \text{ and } |V_i| \sim 2\sqrt[2]{4})$$

matrix size:  $\sqrt[3]{N} \times \sqrt[3]{N} = 2 \times 2$ 

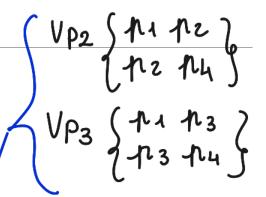
Let's place processes in the matrix and compute V<sub>i</sub>

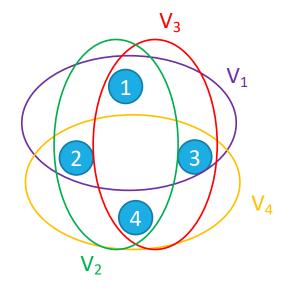
×		2)		
_	<del>p</del>	1	<del></del>	
2	р	3	р4	

for	11	: S-121	127
•		2-tra	t2 }

Process id	v
1	p <sub>1</sub> , p <sub>2</sub> , p <sub>3</sub>
2	p <sub>1</sub> , p <sub>2</sub> , p <sub>4</sub>
3	p <sub>1</sub> , p <sub>3</sub> , p <sub>4</sub>
4	p <sub>2</sub> , p <sub>3</sub> , p <sub>4</sub>

VOTING SET

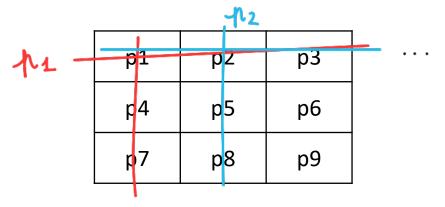




Let us consider a system composed by N = 9 processes

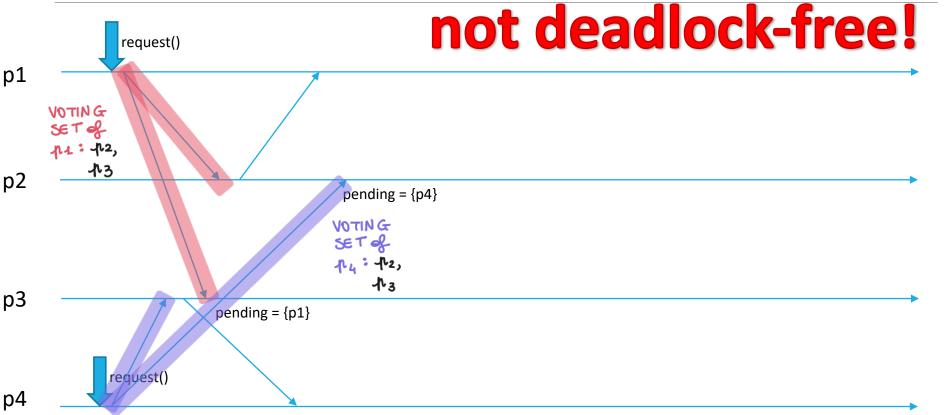
• (M = K 
$$\sim \sqrt[2]{9}$$
 and  $|Vi| \sim 2\sqrt[2]{9} = 6$ )

Let's place processes in the matrix



V
p <sub>1</sub> , p <sub>2</sub> , p <sub>3</sub> , p <sub>4</sub> , p <sub>7</sub>
p <sub>1</sub> , p <sub>2</sub> , p <sub>3</sub> , p <sub>5</sub> , p <sub>8</sub>
p <sub>1</sub> , p <sub>2</sub> , p <sub>3</sub> , p <sub>6</sub> , p <sub>9</sub>
p <sub>4</sub> , p <sub>5</sub> , p <sub>6</sub> , p <sub>1</sub> , p <sub>7</sub>
p <sub>4</sub> , p <sub>5</sub> , p <sub>6</sub> , p <sub>2</sub> , p <sub>8</sub>
p <sub>4</sub> , p <sub>5</sub> , p <sub>6</sub> , p <sub>3</sub> , p <sub>9</sub>
p <sub>7</sub> , p <sub>8</sub> , p <sub>9</sub> , p <sub>1</sub> , p <sub>4</sub>
p <sub>7</sub> , p <sub>8</sub> , p <sub>9</sub> , p <sub>2</sub> , p <sub>5</sub>
p <sub>7</sub> , p <sub>8</sub> , p <sub>9</sub> , p <sub>3</sub> , p <sub>6</sub>

# WARNING! Example Maekawa's Algorithm is



## Reference

George Coulouris, Jean Dollimore and Tim Kindberg, Gordon Blair "Distributed Systems: Concepts and Design (5th Edition)". Addison - Wesley, 2012.

Chapter 11 – section 11.2