

29/11/23

# Dependable Distributed Systems Master of Science in Engineering in Computer Science

AA 2023/2024

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LECTURE 26: BROADCAST IN PRESENCE OF BYZANTINE  
PROCESSES

# Recap on Byzantine processes

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Byzantine processes may

1. deviate arbitrarily from the instructions that an algorithm assigns to them
  - creating fake messages
  - dropping messages
  - delay the deliveries
  - altering the content of messages
  - ...
2. act as if they were deliberately preventing the algorithm from reaching its goals

# Basic step to fight Byzantine processes

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Using cryptographic mechanisms to implement the authenticated perfect links abstraction



... But, cryptography alone does not allow to tolerate Byzantine processes

- Considering an arbitrary-faulty sender, asking him/her to digitally sign every broadcast message does not help at all (it may simply sign the two different messages)



manipulation of content

# Correct and faulty state

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As in the crash failure model, we distinguish between *faulty* and *correct* processes

**NOTE:** a Byzantine process may act arbitrarily, and no mechanism can guarantee anything that relates to its actions.



We do not define any “uniform” variants of primitives in the Byzantine failure model.

# P2P communication channel

## Authenticated Perfect Link

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**Module 2.5:** Interface and properties of authenticated perfect point-to-point links

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**Module:**

**Name:** AuthPerfectPointToPointLinks, **instance** *al*.

**Events:**

**Request:**  $\langle al, \text{Send} \mid q, m \rangle$ : Requests to send message  $m$  to process  $q$ .

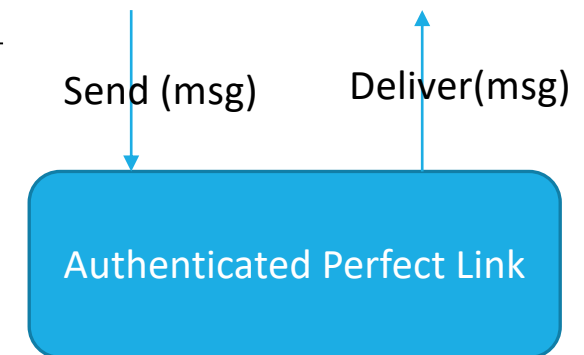
**Indication:**  $\langle al, \text{Deliver} \mid p, m \rangle$ : Delivers message  $m$  sent by process  $p$ .

**Properties:**

**AL1:** *Reliable delivery*: If a correct process sends a message  $m$  to a correct process  $q$ , then  $q$  eventually delivers  $m$ .

**AL2:** *No duplication*: No message is delivered by a correct process more than once.

**AL3:** *Authenticity*: If some correct process  $q$  delivers a message  $m$  with sender  $p$  and process  $p$  is correct, then  $m$  was previously sent to  $q$  by  $p$ .



} Same as Perfect point-to-point links

# Byzantine consistent broadcast specification

**Module 3.11:** Interface and properties of Byzantine consistent broadcast

**Module:**

**Name:** ByzantineConsistentBroadcast, **instance** *bcb*, with sender *s*.

**Events:**

**Request:**  $\langle bcb, Broadcast \mid m \rangle$ : Broadcasts a message *m* to all processes. Executed only by process *s*.

**Indication:**  $\langle bcb, Deliver \mid p, m \rangle$ : Delivers a message *m* broadcast by process *p*.

**Properties:**

**BCB1:** *Validity*: If a correct process *p* broadcasts a message *m*, then every correct process eventually delivers *m*.

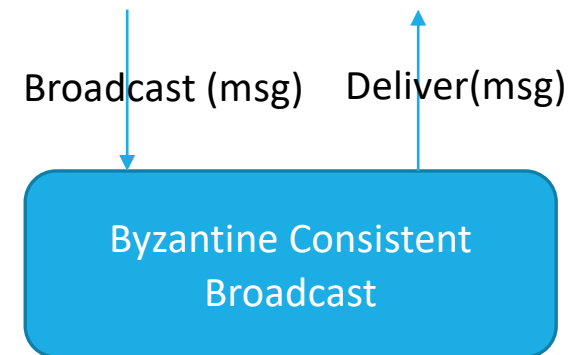
**BCB2:** *No duplication*: Every correct process delivers at most one message.

**BCB3:** *Integrity*: If some correct process delivers a message *m* with sender *p* and process *p* is correct, then *m* was previously broadcast by *p*.

**BCB4:** *Consistency*: If some correct process delivers a message *m* and another correct process delivers a message *m'*, then  $m = m'$ .



The specification refers to a single broadcast event!



# Byzantine consistent broadcast implementation

**Algorithm 3.16:** Authenticated Echo Broadcast

**Implements:**

ByzantineConsistentBroadcast, **instance** *bcb*, with sender *s*.

**Uses:**

AuthPerfectPointToPointLinks, **instance** *al*.

**upon event**  $\langle bcb, Init \rangle$  **do**

*sentecho* := FALSE;

*delivered* := FALSE;

*echos* :=  $[\perp]^N$ ;

**upon event**  $\langle bcb, Broadcast \mid m \rangle$  **do**

**forall**  $q \in \Pi$  **do**

**trigger**  $\langle al, Send \mid q, [SEND, m] \rangle$ ;

// only process *s*

**upon event**  $\langle al, Deliver \mid p, [SEND, m] \rangle$  **such that**  $p = s$  **and** *sentecho* = FALSE **do**

*sentecho* := TRUE;

**forall**  $q \in \Pi$  **do**

**trigger**  $\langle al, Send \mid q, [ECHO, m] \rangle$ ;

**upon event**  $\langle al, Deliver \mid p, [ECHO, m] \rangle$  **do**

**if** *echos*[*p*] =  $\perp$  **then**

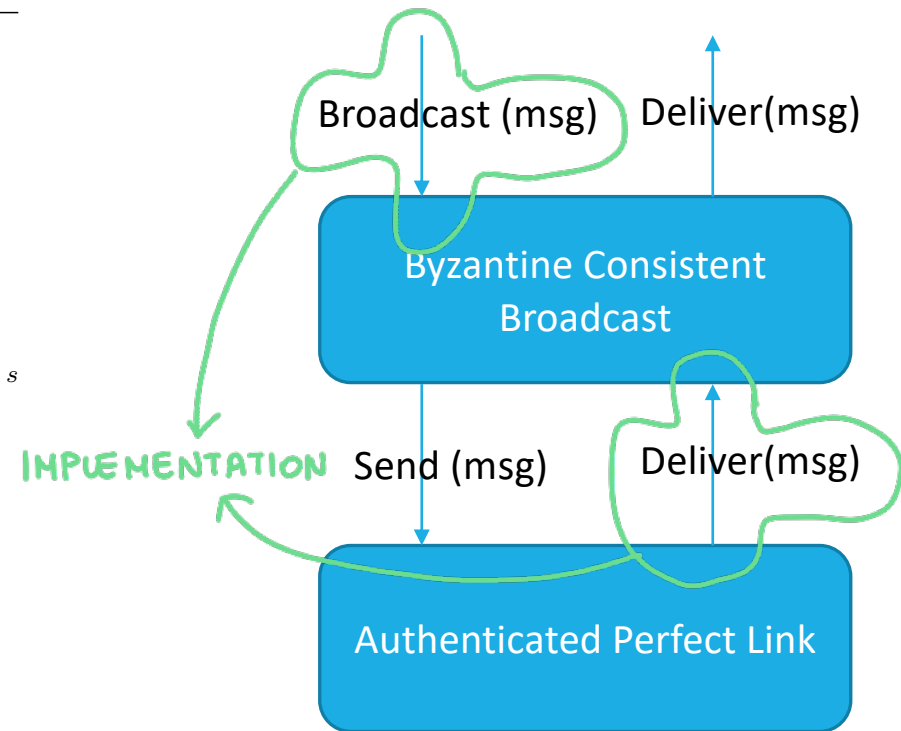
*echos*[*p*] := *m*;

**upon exists**  $m \neq \perp$  such that  $\#(\{p \in \Pi \mid echos[p] = m\}) > \frac{N+f}{2}$

**and** *delivered* = FALSE **do**

*delivered* := TRUE;

**trigger**  $\langle bcb, Deliver \mid s, m \rangle$ ;



Correctness is ensured if  
 $N > 3f$

### Algorithm 3.16: Authenticated Echo Broadcast

#### Implements:

ByzantineConsistentBroadcast, **instance** *bcb*, with sender *s*.

#### Uses:

AuthPerfectPointToPointLinks, **instance** *al*. *ECHO messages*

**upon event**  $\langle bcb, \text{Init} \rangle$  **do**

*sentecho* := FALSE;

*delivered* := FALSE;

*echos* :=  $\perp^N$ ; *vector: I store ECHO received from other pro*

**upon event**  $\langle bcb, \text{Broadcast} \mid m \rangle$  **do**

**forall**  $q \in \Pi$  **do**

**trigger**  $\langle al, \text{Send} \mid q, [\text{SEND}, m] \rangle$ ;

*CORRECT*

*// only process s*

**upon event**  $\langle al, \text{Deliver} \mid p, [\text{SEND}, m] \rangle$  **such that**  $p = s$  **and** *sentecho* = FALSE **do**

*sentecho* := TRUE;

**forall**  $q \in \Pi$  **do**

**trigger**  $\langle al, \text{Send} \mid q, [\text{ECHO}, m] \rangle$ ;

*1 time I received an ECHO*

*received m to the sender*

**upon event**  $\langle al, \text{Deliver} \mid p, [\text{ECHO}, m] \rangle$  **do**

**if** *echos*[*p*] =  $\perp$  **then** *in my pocket*

*echos*[*p*] := *m*;

*If I want to tolerate 1 faulty p  
I need 4 processes*

**upon exists**  $m \neq \perp$  **such that**  $\#(\{p \in \Pi \mid \text{echos}[p] = m\}) > \frac{N+f}{2}$

**and** *delivered* = FALSE **do**

*delivered* := TRUE;

**trigger**  $\langle bcb, \text{Deliver} \mid s, m \rangle$ ;

*Can I trust the process?*

**Correctness is ensured if**

**$N > 3f$**

$4 > 3 \cdot 1$

5 faulty

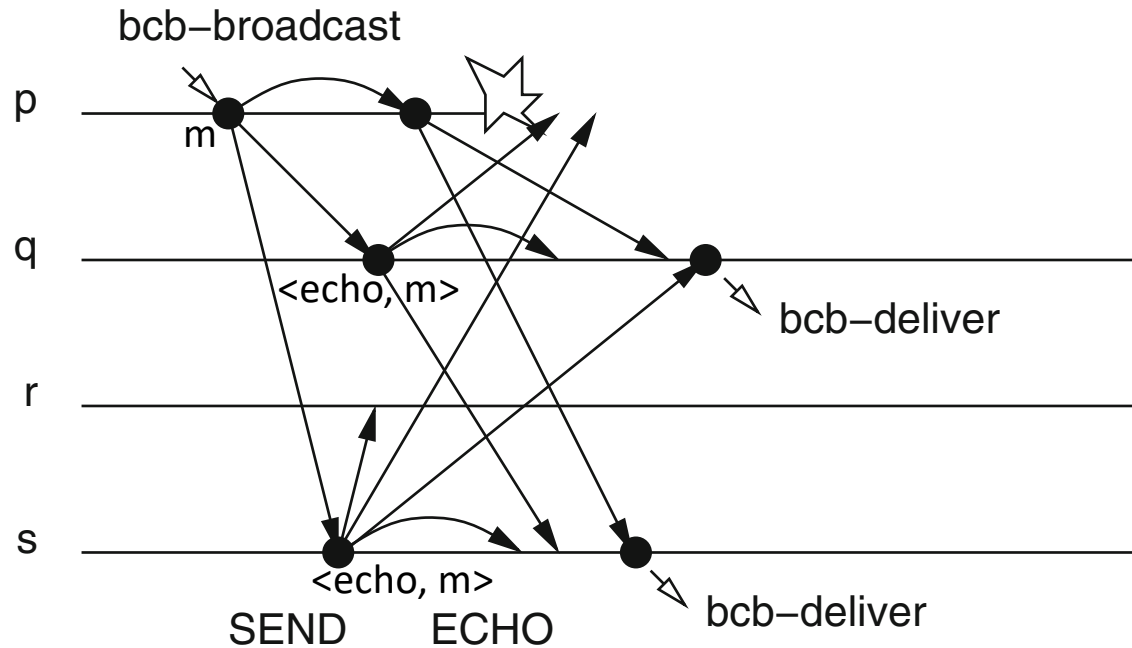
$N > 3 \cdot 5 \rightarrow 16 > 15$

16 correct  
5 faulty } 21 processes



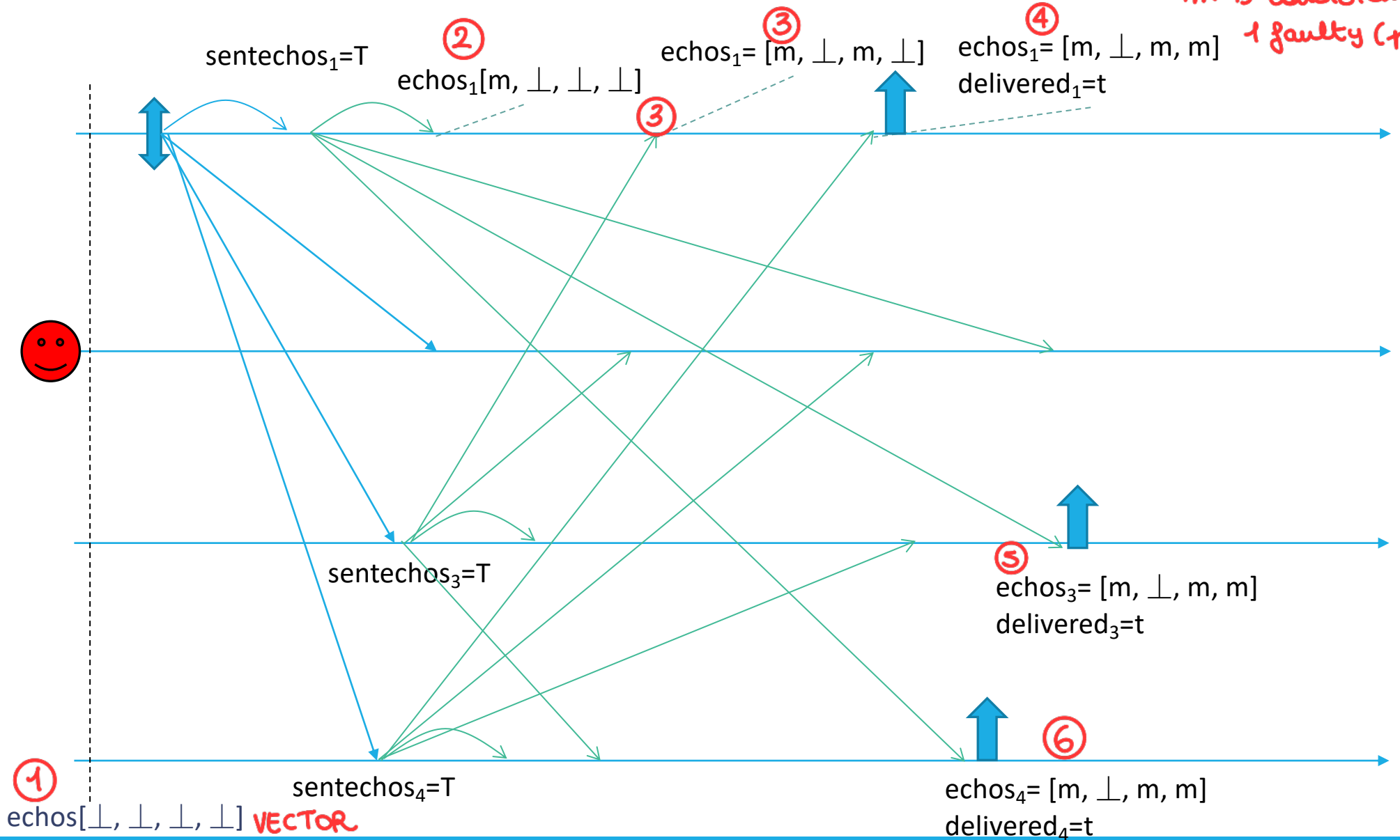
# Byzantine consistent broadcast example

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Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (correct sender)

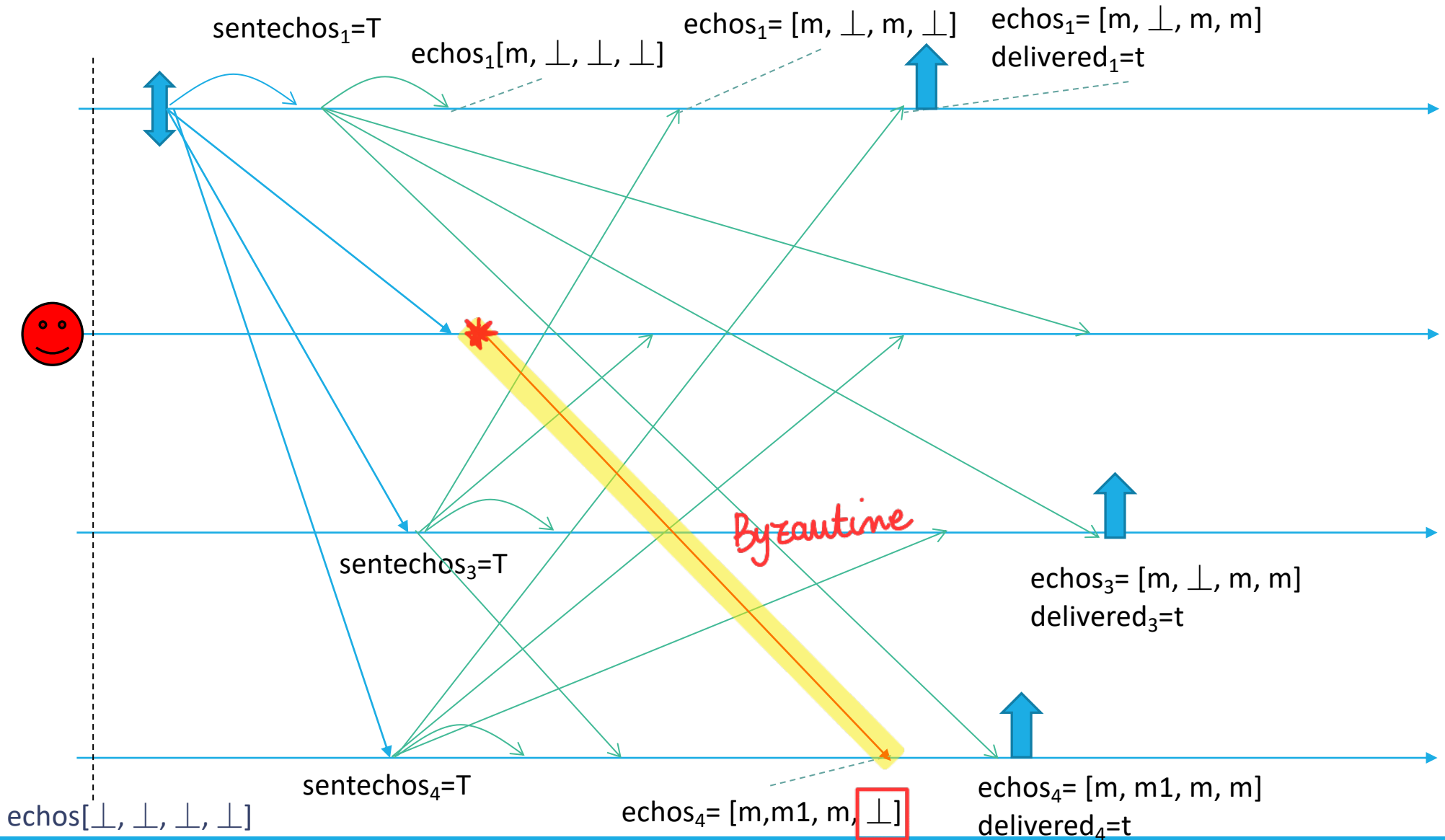
*m is consistent  
+ faulty (p2)*



Sentechos = F

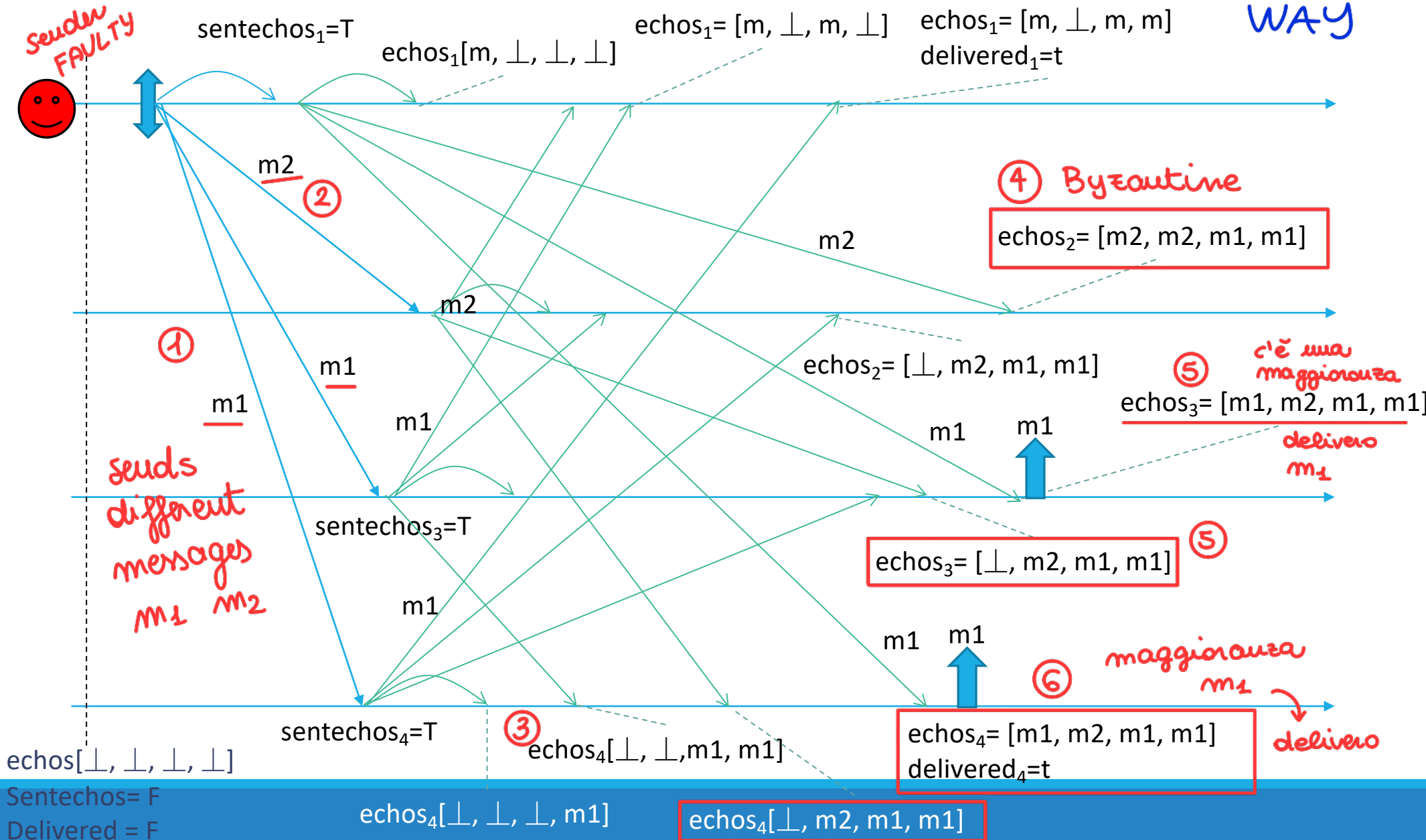
Delivered = F

Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (correct sender)



# HERE THE FAULTY ANSWER IN AN INCORRECT WAY

Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (faulty sender)



# Byzantine Reliable Broadcast specification

**Module 3.12:** Interface and properties of Byzantine reliable broadcast

**Module:**

**Name:** ByzantineReliableBroadcast, **instance** *brb*, with sender *s*.

**Events:**

**Request:**  $\langle brb, Broadcast \mid m \rangle$ : Broadcasts a message *m* to all processes. Executed only by process *s*.

**Indication:**  $\langle brb, Deliver \mid p, m \rangle$ : Delivers a message *m* broadcast by process *p*.

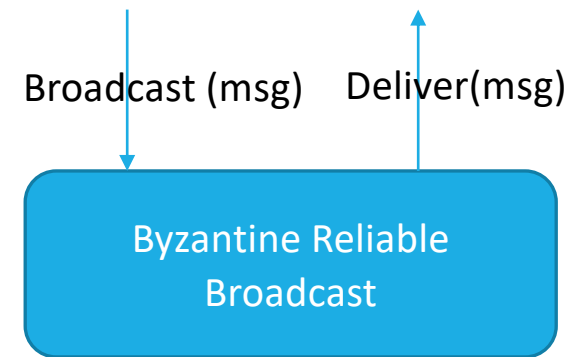
**Properties:**

**BRB1–BRB4:** Same as properties BCB1–BCB4 in Byzantine consistent broadcast (Module 3.11).

**BRB5:** *Totality*: If some message is delivered by any correct process, every correct process eventually delivers a message.



The specification refers to a single broadcast event!



# Byzantine Reliable Broadcast implementation

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## Algorithm 3.18: Authenticated Double-Echo Broadcast

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### Implements:

ByzantineReliableBroadcast, **instance** *brb*, with sender *s*.

### Uses:

AuthPerfectPointToPointLinks, **instance** *al*.

#### upon event $\langle brb, Init \rangle$ do

```
sentecho := FALSE;
sentecho := FALSE;
delivered := FALSE;
echos :=  $[\perp]^N$ ;
readys :=  $[\perp]^N$ ;
```

#### upon event $\langle brb, Broadcast \mid m \rangle$ do

```
for all  $q \in \Pi$  do
  trigger  $\langle al, Send \mid q, [SEND, m] \rangle$ ;
```

#### upon event $\langle al, Deliver \mid p, [SEND, m] \rangle$ such that $p = s$ and *sentecho* = FALSE do

```
sentecho := TRUE;
for all  $q \in \Pi$  do
  trigger  $\langle al, Send \mid q, [ECHO, m] \rangle$ ;
```

#### upon event $\langle al, Deliver \mid p, [ECHO, m] \rangle$ do

```
if  $echos[p] = \perp$  then
  echos[p] := m;
```

// only process *s*

upon exists  $m \neq \perp$  such that  $\#(\{p \in \Pi \mid echos[p] = m\}) > \frac{N+f}{2}$

and *sentecho* = FALSE do

*sentecho* := TRUE;

for all  $q \in \Pi$  do

trigger  $\langle al, Send \mid q, [READY, m] \rangle$ ;

upon event  $\langle al, Deliver \mid p, [READY, m] \rangle$  do

if  $readys[p] = \perp$  then

*readys*[*p*] := *m*;

upon exists  $m \neq \perp$  such that  $\#(\{p \in \Pi \mid readys[p] = m\}) > f$

and *sentecho* = FALSE do

*sentecho* := TRUE;

for all  $q \in \Pi$  do

trigger  $\langle al, Send \mid q, [READY, m] \rangle$ ;

upon exists  $m \neq \perp$  such that  $\#(\{p \in \Pi \mid readys[p] = m\}) > 2f$

and *delivered* = FALSE do

*delivered* := TRUE;

trigger  $\langle brb, Deliver \mid s, m \rangle$ ;

### Algorithm 3.18: Authenticated Double-Echo Broadcast

#### Implements:

ByzantineReliableBroadcast, **instance** *brb*, with sender *s*.

#### Uses:

AuthPerfectPointToPointLinks, **instance** *al*.

#### upon event $\langle brb, Init \rangle$ do

```
sentecho := FALSE;
sentready := FALSE;
delivered := FALSE;
echos :=  $[\perp]^N$ ;
readys :=  $[\perp]^N$ ; ready to deliver
```

#### upon event $\langle brb, Broadcast \mid m \rangle$ do

```
forall  $q \in \Pi$  do
  trigger  $\langle al, Send \mid q, [SEND, m] \rangle$ ; // only process s
```

#### upon event $\langle al, Deliver \mid p, [SEND, m] \rangle$ such that $p = s$ and *sentecho* = FALSE do

```
sentecho := TRUE;
forall  $q \in \Pi$  do
  trigger  $\langle al, Send \mid q, [ECHO, m] \rangle$ ;
```

#### upon event $\langle al, Deliver \mid p, [ECHO, m] \rangle$ do

```
if echos[p] =  $\perp$  then store locally: 1° echo I receiving
  echos[p] := m;
```

upon exists  $m \neq \perp$  such that  $\#(\{p \in \Pi \mid echos[p] = m\}) > \frac{N+f}{2}$

and *sentready* = FALSE do

*sentready* := TRUE;

forall  $q \in \Pi$  do

trigger  $\langle al, Send \mid q, [READY, m] \rangle$ ; *no propagate m for which I have most votes*

#### upon event $\langle al, Deliver \mid p, [READY, m] \rangle$ do

if *readys*[p] =  $\perp$  then

*readys*[p] := m;

upon exists  $m \neq \perp$  such that  $\#(\{p \in \Pi \mid readys[p] = m\}) > f$

and *sentready* = FALSE do

*sentready* := TRUE;

forall  $q \in \Pi$  do

trigger  $\langle al, Send \mid q, [READY, m] \rangle$ ;

upon exists  $m \neq \perp$  such that  $\#(\{p \in \Pi \mid readys[p] = m\}) > 2f$

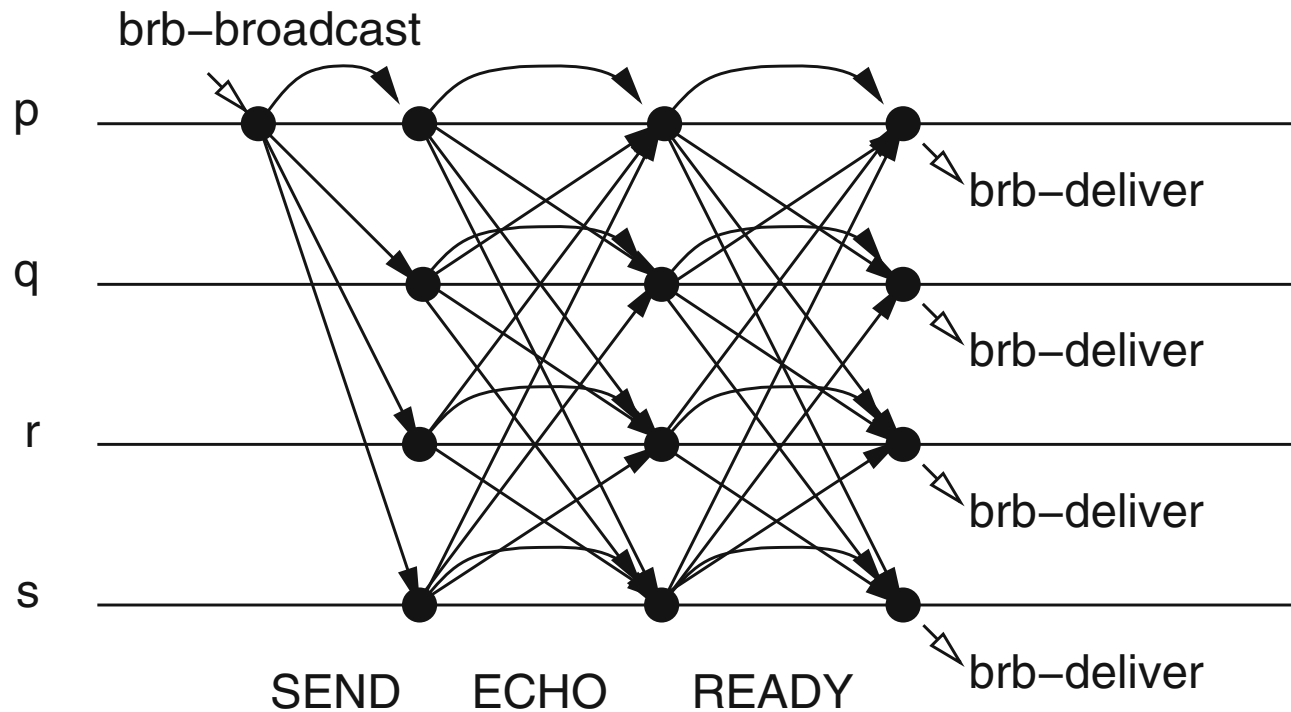
and *delivered* = FALSE do

*delivered* := TRUE;

trigger  $\langle brb, Deliver \mid s, m \rangle$ ;

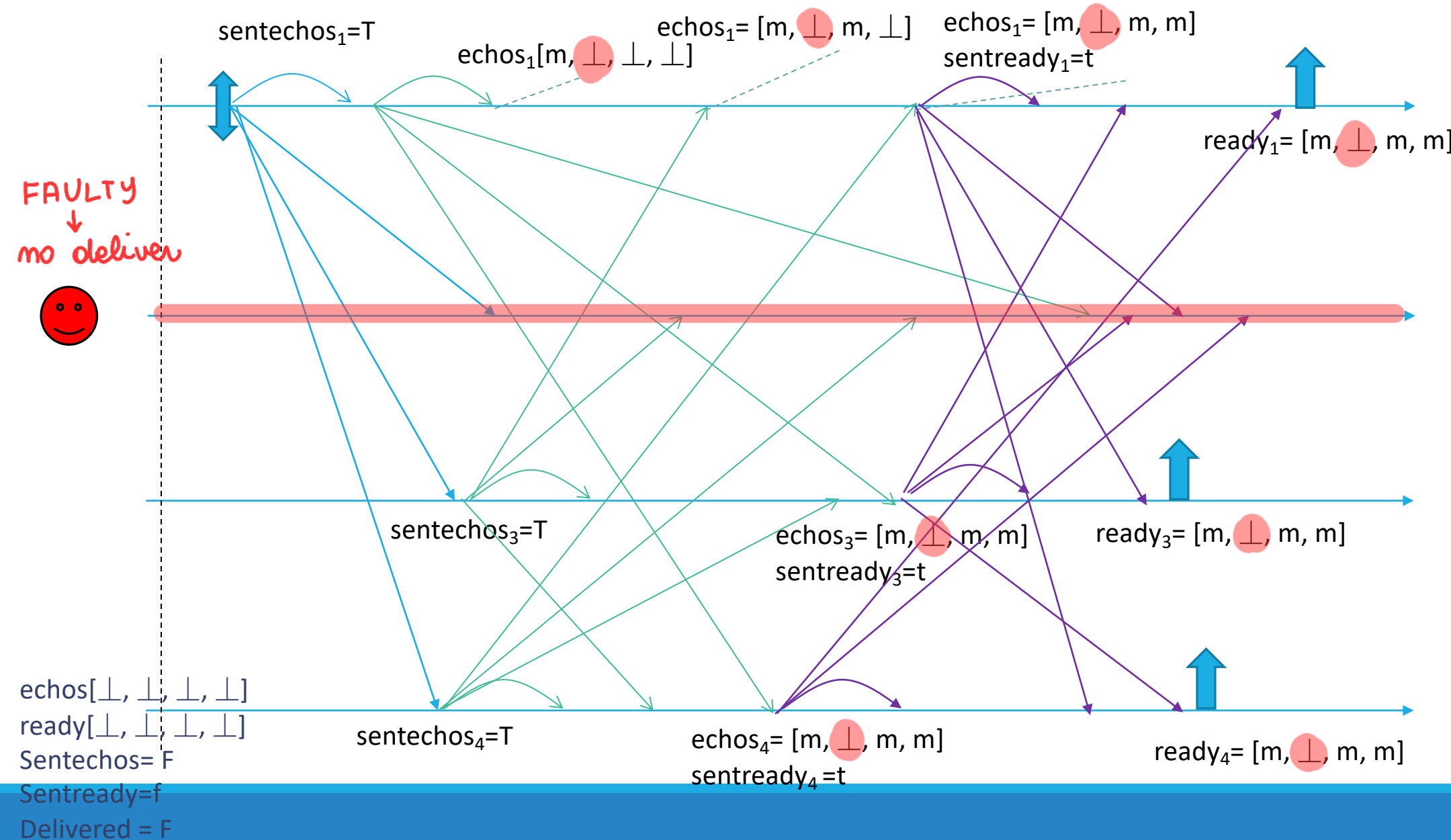
# Byzantine Reliable Broadcast example

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Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (correct sender)



Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (faulty sender)

sender  
faulty

sentechos<sub>1</sub>=T

ready m<sub>1</sub>

Faulty

STOPPED

AGREEMENT

ready<sub>2</sub> = [ $\perp$ ,  $\perp$ , m<sub>1</sub>, m<sub>1</sub>]

ready<sub>2</sub> = [ $\perp$ , m<sub>1</sub>, m<sub>1</sub>, m<sub>1</sub>]

ready<sub>3</sub> = [ $\perp$ ,  $\perp$ , m<sub>1</sub>, m<sub>1</sub>]

ready<sub>3</sub> = [ $\perp$ , m<sub>1</sub>, m<sub>1</sub>, m<sub>1</sub>]

ready<sub>4</sub> = [ $\perp$ ,  $\perp$ , m<sub>1</sub>, m<sub>1</sub>]

ready<sub>4</sub> = [ $\perp$ , m<sub>1</sub>, m<sub>1</sub>, m<sub>1</sub>]

echos<sub>2</sub> = [m<sub>2</sub>, m<sub>2</sub>, m<sub>1</sub>, m<sub>1</sub>]

echos<sub>3</sub> = [m<sub>1</sub>, m<sub>2</sub>, m<sub>1</sub>, m<sub>1</sub>]

echos<sub>4</sub> = [m<sub>1</sub>, m<sub>2</sub>, m<sub>1</sub>, m<sub>1</sub>]

m<sub>2</sub>

m<sub>2</sub>

m<sub>1</sub>

m<sub>1</sub>

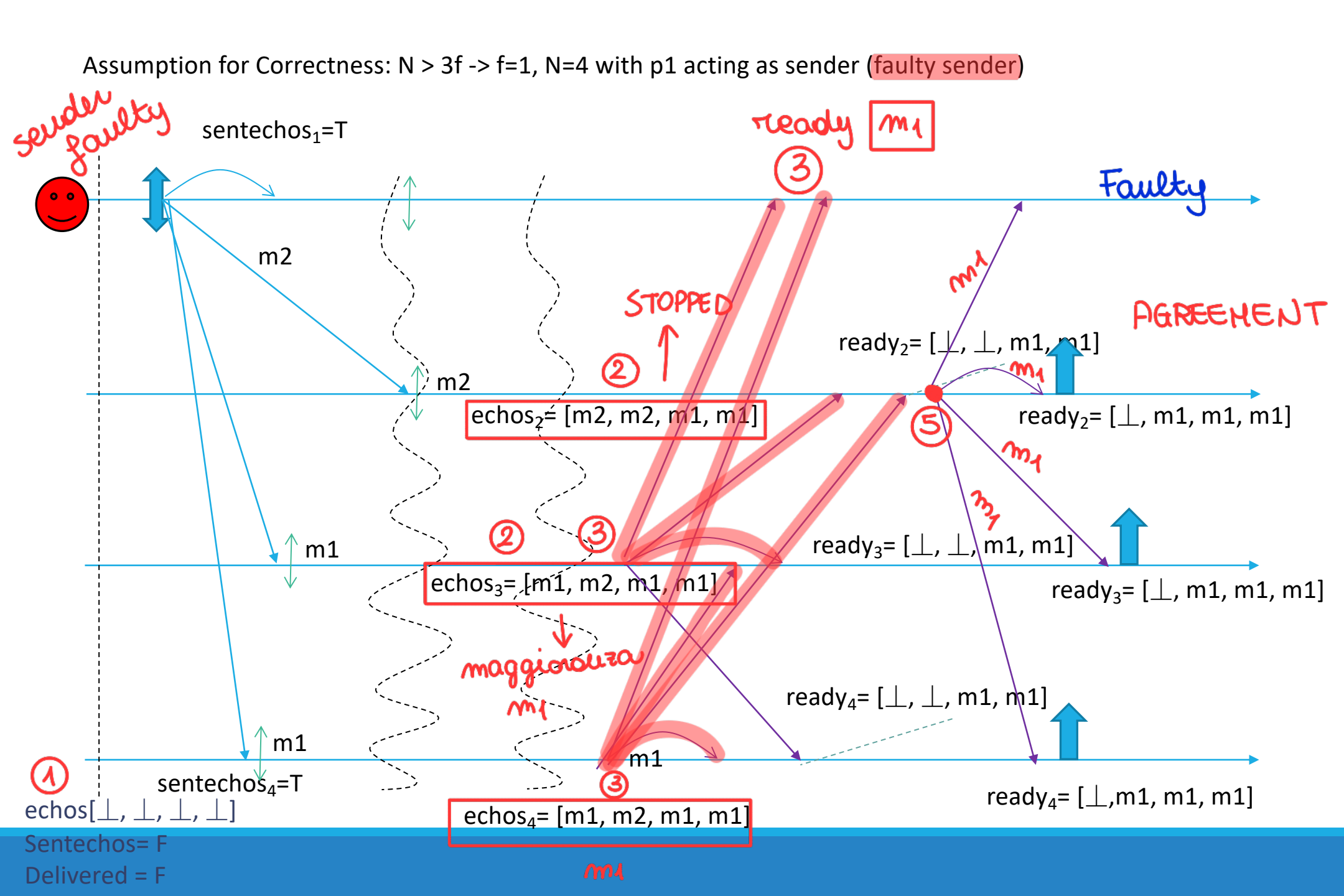
sentechos<sub>4</sub>=T

echos[ $\perp$ ,  $\perp$ ,  $\perp$ ,  $\perp$ ]

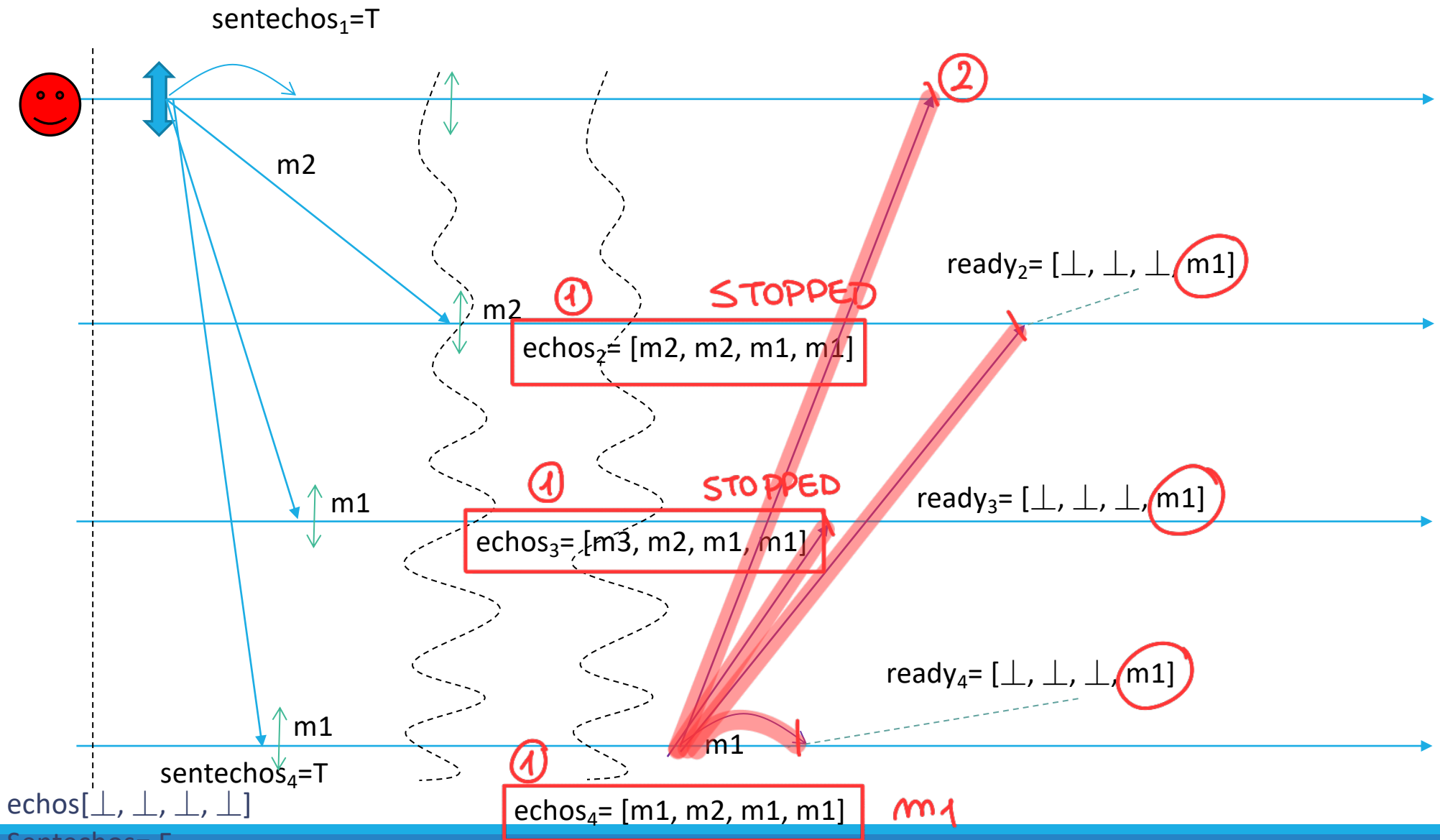
Sentechos= F

Delivered = F

m<sub>1</sub>



Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (faulty sender)

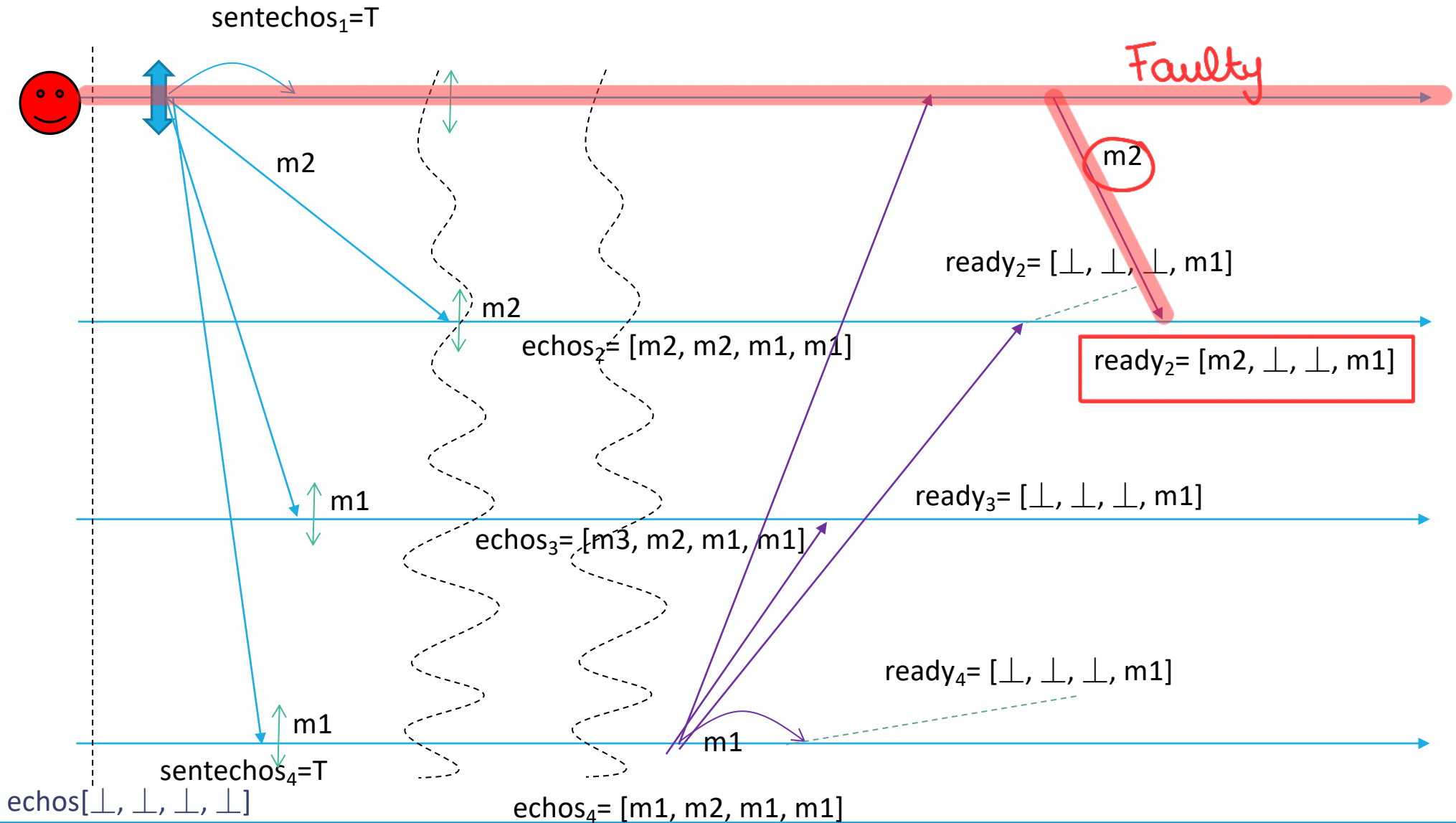


Sentechos= F

Delivered = F

Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (faulty sender)

$M_2$



Sentechos= F

Delivered = F

Assumption for Correctness:  $N > 3f \rightarrow f=1, N=4$  with p1 acting as sender (faulty sender)

$m_1$

sentechos<sub>1</sub>=T

Faulty



m2

m2

echos<sub>2</sub> = [m2, m2, m1, m1]

m1

echos<sub>3</sub> = [m3, m2, m1, m1]

sentechos<sub>4</sub>=T

echos[⊥, ⊥, ⊥, ⊥]

echos<sub>4</sub> = [m1, m2, m1, m1]

ready<sub>2</sub> = [⊥, ⊥, ⊥, m1]

ready<sub>2</sub> = [m1, m1, ...]

ready<sub>2</sub> = [m1, ⊥, ⊥, m1]

ready<sub>3</sub> = [⊥, ⊥, ⊥, m1]

ready<sub>3</sub> = [⊥, m1, ⊥, m1]

ready<sub>4</sub> = [⊥, ⊥, ⊥, m1]

ready<sub>4</sub> = [⊥, m1, ⊥, m1]

ready<sub>4</sub> = [⊥, m1, m1, m1]

Sentechos = F

Delivered = F

# References

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C. Cachin, R. Guerraoui and L. Rodrigues. Introduction to Reliable and Secure Distributed Programming, Springer, 2011

- Chapter 2 – Section 2.4.6
- Chapter 3 – Section 3.10 (except 3.10.4), Section 3.11