Distributed Systems

Master of Science in Engineering in

Computer Science

AA 2018/2019

LECTURE 11: TOTAL ORDER BROADCAST

### System model

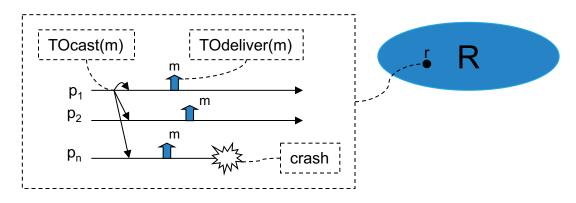
Static set of processes  $\Pi = \{p_1 ... p_n\}$ 

Message passing over perfect channels (message exchanging between correct processes is reliable)

Asynchronous

Crash fault model for processes

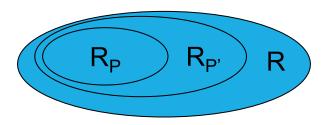
We characterize the system in terms of its possible runs R



#### A few notation

<u>Property</u> P: predicate on the system, identifying a set of runs  $R_P \subseteq R$ 

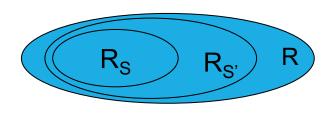
$${}^{\circ}\ P \Longrightarrow P' \ \textit{iff} \ R_{P} \subseteq R_{P'}$$

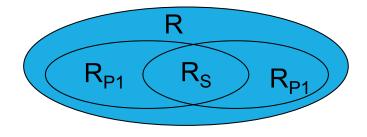


<u>Specification</u> S(P<sub>1</sub>,...,P<sub>m</sub>): logical and of m properties, identifying a set of runs

$$R_S\text{=}R_{P_{\textstyle 1}}\cap ... \cap R_{P_{\textstyle m}}\subseteq R$$

$$\circ$$
 S  $\rightarrow$  S' iff  $R_S \subset R_{S'}$ 





### TO specifications

Total order specifications are usually composed by four properties:

- ➤ A <u>Validity</u> property guarantees that messages sent by correct processes will eventually be delivered at least by correct processes;
- An <u>Integrity</u> property guarantees that no spurious or duplicate messages are delivered;
- An Agreement property ensures that (at least correct) processes deliver the same set of messages;
- An Order property constrains (at least correct) processes delivering the same messages to deliver them in the same order.

#### TO specifications

Total Order Broadcast = S(V,I,A,O)

```
    V = VNUV
    I = Intellity
    X = Agreement
    X = Order
```

Distinct specifications arise from distinct formulations of each property

- uniform vs non-uniform
- A uniform property imposes restrictions on the behavior of (at least)
   correct processes on the basis of events occurred in some process

#### TO Specifications

#### Crash failure + Perfect channels ⇒

- NUV: if a correct process TOCAST a message m then some correct process will eventually deliver m
- **UI**: For any message m, every process p delivers m at most once and only if m was previously TOCAST by some (correct or not) process.

### The Agreement property

#### UNIFORM AGREEMENT (UA)

If a <u>process</u> (correct or not)

TODelivers a message m, then <u>all</u>

<u>correct</u> processes will eventually

TODeliver m

#### NON-UNIFORM AGREEMENT (NUA)

If a <u>correct process</u> TODelivers a message m, then <u>all correct processes</u> will eventually TODeliver m

#### CONSTRAINS THE SET OF DELIVERED MESSAGES

Correct processes always deliver the same set of messages M

Each faulty process p delivers a set M<sub>p</sub>

 $\mathsf{UA} \colon \mathsf{M}_\mathsf{p} \subseteq \mathsf{M}$ 

NUA:  $M_p$  can be s.t.  $M_p$  -  $M \neq \emptyset$ 

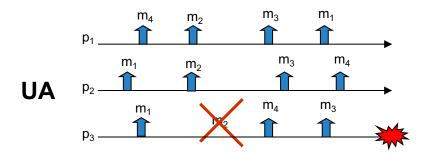
### The Agreement property

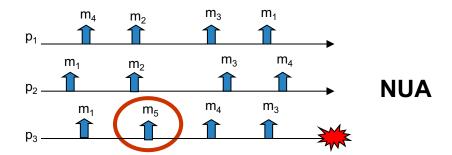
#### **UNIFORM AGREEMENT (UA)**

If a <u>process</u> (<u>correct or not</u>)
TODelivers a message m, then <u>all</u>
<u>correct</u> processes will eventually
TODeliver m

#### NON-UNIFORM AGREEMENT (NUA)

If a <u>correct process</u> TODelivers a message m, then <u>all correct processes</u> will eventually TODeliver m





### The Ordering Property

#### STRONG UNIFORM TOTAL ORDER (SUTO)

If some process TODelivers some message m before message m, then a process TODelivers m' only after it has TODelivered m.



- same order
- same prefix of the set of delivered messages
- after an omission, disjoint sets of delivered messages

#### WEAK UNIFORM TOTAL ORDER (WUTO)

If process p and process q both TODdeliver messages m and m', then p TODelivers m before m' if and only if q TODdelivers m before m'.



 no restrictions on the set of delivered messages

#### The Order Property

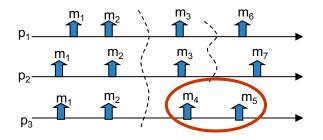
#### STRONG UNIFORM TOTAL ORDER (SUTO)

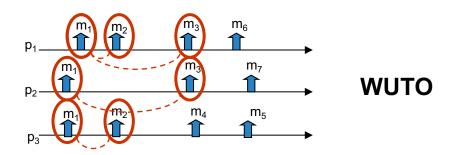
If some process TODelivers some message m before message m, then a process TODelivers m only after it has TODelivered m.

#### WEAK UNIFORM TOTAL ORDER (WUTO)

If process p and process q both TODdeliver messages m and m', then p TODelivers m before m' if and only if q TODdelivers m before m'.







### The Order Property

SUTO and WUTO are uniform but they both have a non-uniform counterpart

#### STRONG NON-UNIFORM TOTAL ORDER (SNUTO)

If <u>some correct process</u> TODelivers some message m before message m', then <u>a correct process</u> TODelivers m' only after it has TODelivered m.

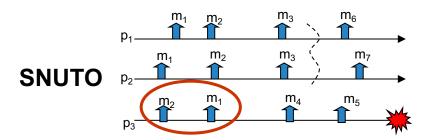
#### WEAK NON-UNIFORM TOTAL ORDER (WNUTO)

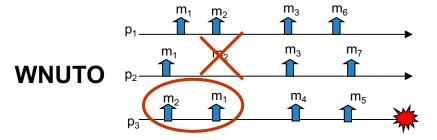
If <u>correct processes</u> p and q both TODeliver messages m and m', then p TODelivers m before m' if and only if q TODelivers m before m'.

## The Order property (2)

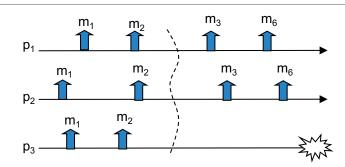
SUTO ⇒ WUTO

SNUTO ⇒ WNUTO

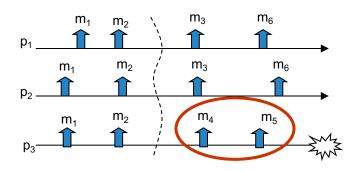




### TO specifications



TO(NUA,SUTO)



TO(UA,SUTO)
(Strongest total order)

TO(NUA,SUTO)

TO(UA,SUTO)

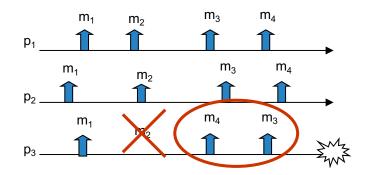
• The strongest TO spec.

### TO specifications (2)

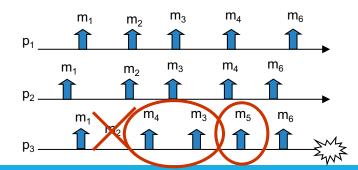
 $m_4$ TO(UA,SUTO) (Strongest total order) TO(UA,WUTO)  $m_4$ TO(UA,WUTO) TO(NUA,SUTO) TO(NUA,WUTO) TO(NUA, WUTO)

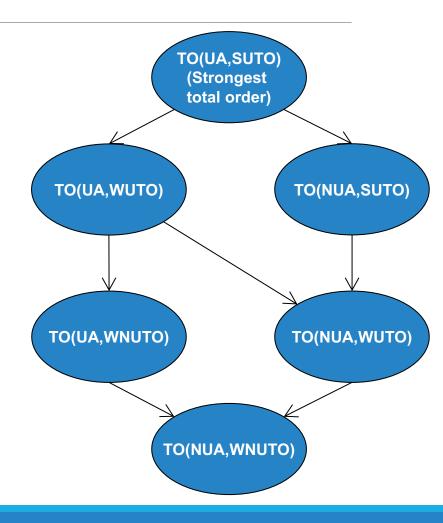
### TO specifications (3)

#### TO(UA,WNUTO)

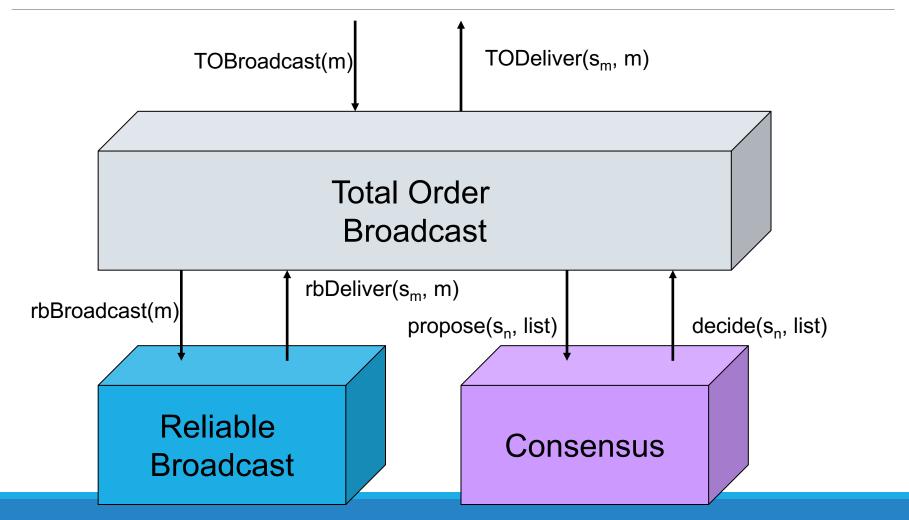


#### TO(NUA, WNUTO)





### Total Order Implementation



### Total Order Algorithm

#### Algorithm 6.1: Consensus-Based Total-Order Broadcast

#### **Implements:**

TotalOrderBroadcast, instance tob.

ReliableBroadcast, **instance** *rb*;

#### **Uses:**

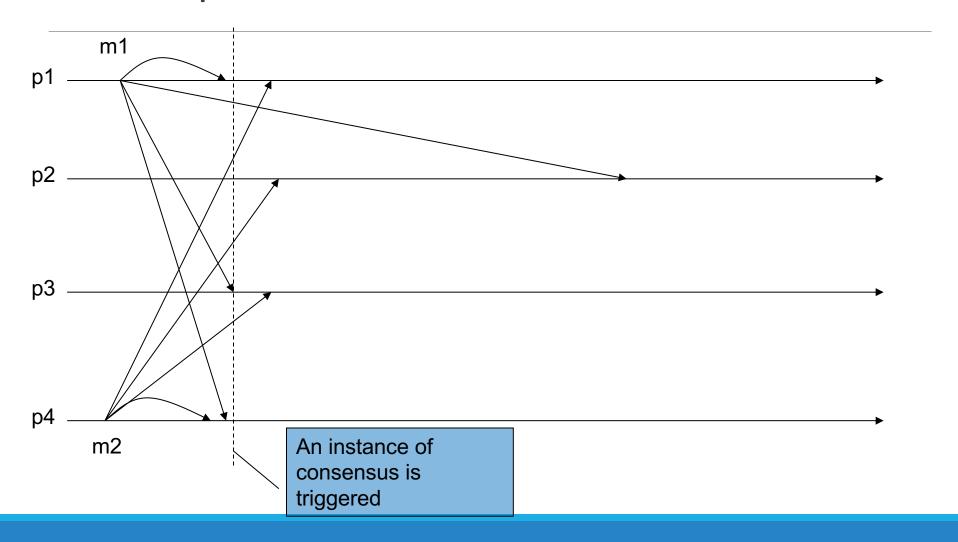
```
Consensus (multiple instances).

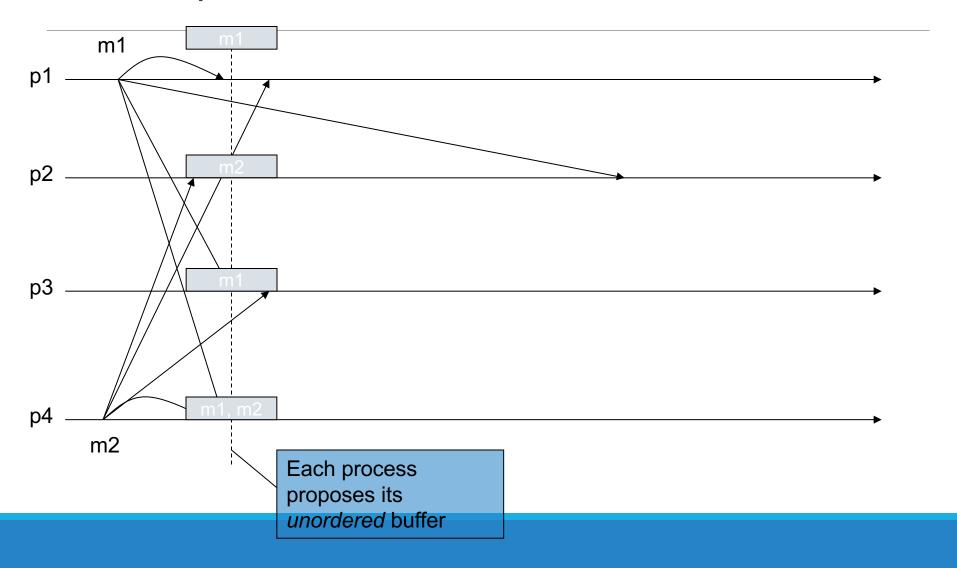
upon event \langle tob, Init \rangle do
unordered := \emptyset;
delivered := \emptyset;
round := 1;
wait := FALSE;

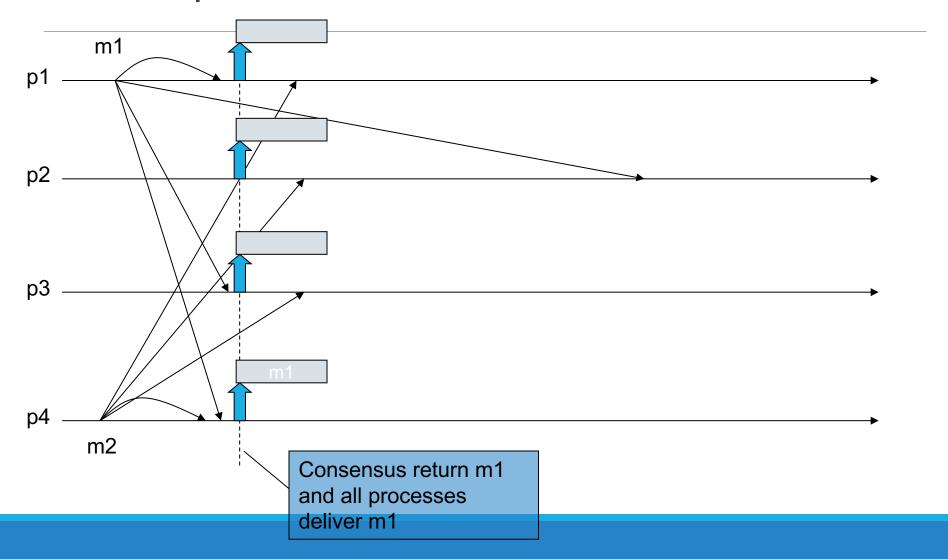
upon event \langle tob, Broadcast \mid m \rangle do
trigger \langle rb, Broadcast \mid m \rangle;

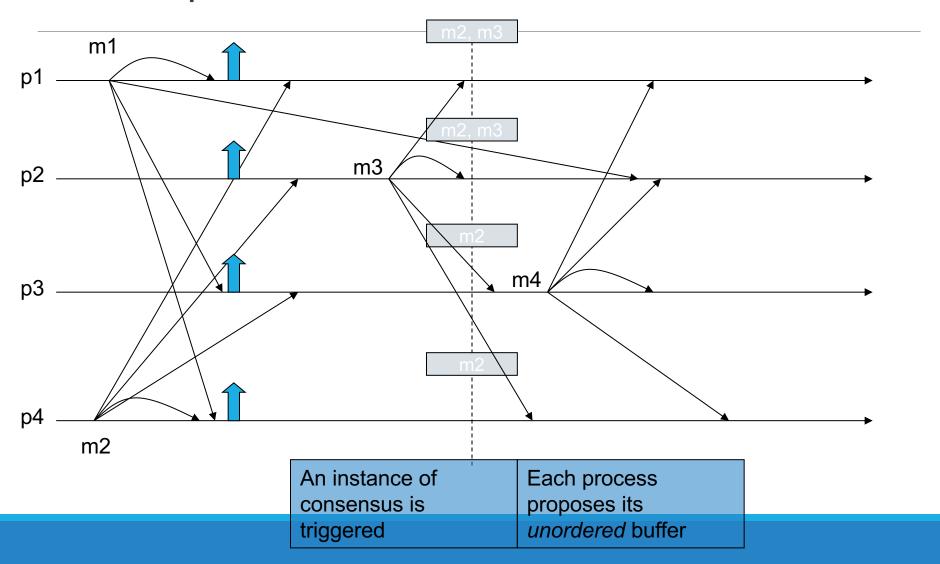
upon event \langle rb, Deliver \mid p, m \rangle do
if \ m \not\in delivered \ then
unordered := unordered \cup \{(p, m)\};
```

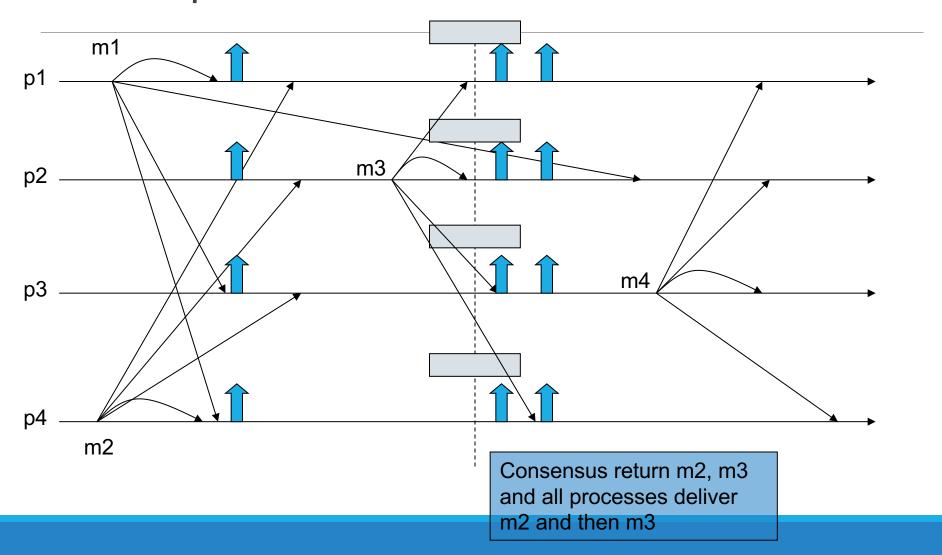
```
 \begin{aligned} &\textbf{upon } \textit{unordered} \neq \emptyset \land \textit{wait} = \mathsf{FALSE} \, \textbf{do} \\ &\textit{wait} \coloneqq \mathsf{TRUE}; \\ &\mathsf{Initialize a new instance} \, \textit{c.round} \, \mathsf{of \, consensus}; \\ &\textbf{trigger} \, \langle \, \textit{c.round}, \, \textit{Propose} \, | \, \textit{unordered} \, \rangle; \end{aligned} \\ &\textbf{upon \, event} \, \langle \, \textit{c.r.}, \, \textit{Decide} \, | \, \textit{decided} \, \rangle \, \textbf{such \, that} \, r = \textit{round \, do} \\ &\textbf{forall} \, (s, m) \in \textit{sort}(\textit{decided}) \, \textbf{do} \qquad \qquad // \, \text{by the order in the resulting sorted list} \\ &\textbf{trigger} \, \langle \, \textit{tob}, \, \textit{Deliver} \, | \, s, \, m \, \rangle; \\ &\textit{delivered} \coloneqq \textit{delivered} \cup \textit{decided}; \\ &\textit{unordered} \coloneqq \textit{unordered} \, \backslash \, \textit{decided}; \\ &\textit{unordered} \coloneqq \textit{unordered} \, \backslash \, \textit{decided}; \\ &\textit{round} \coloneqq \textit{round} + 1; \\ &\textit{wait} \coloneqq \mathsf{FALSE}; \end{aligned}
```











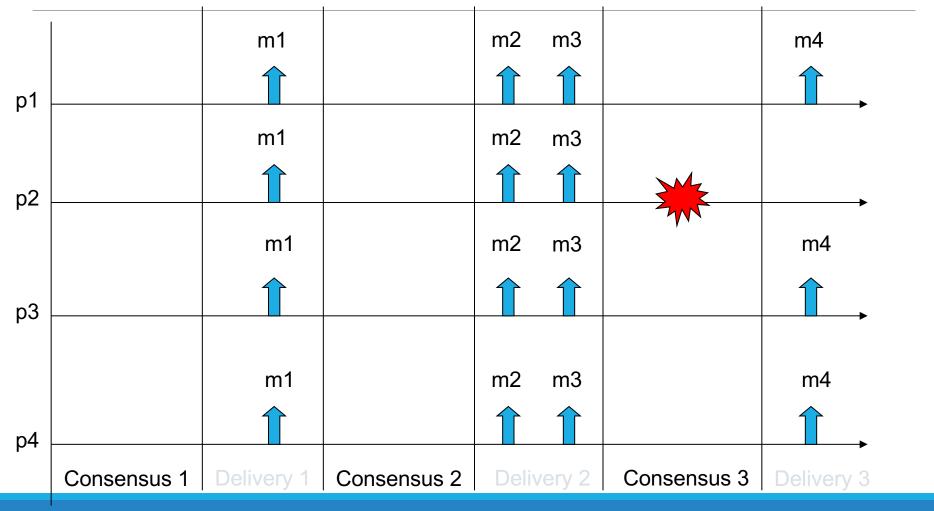
#### Exercice

Which TO specification is satisfied by this algorithm?

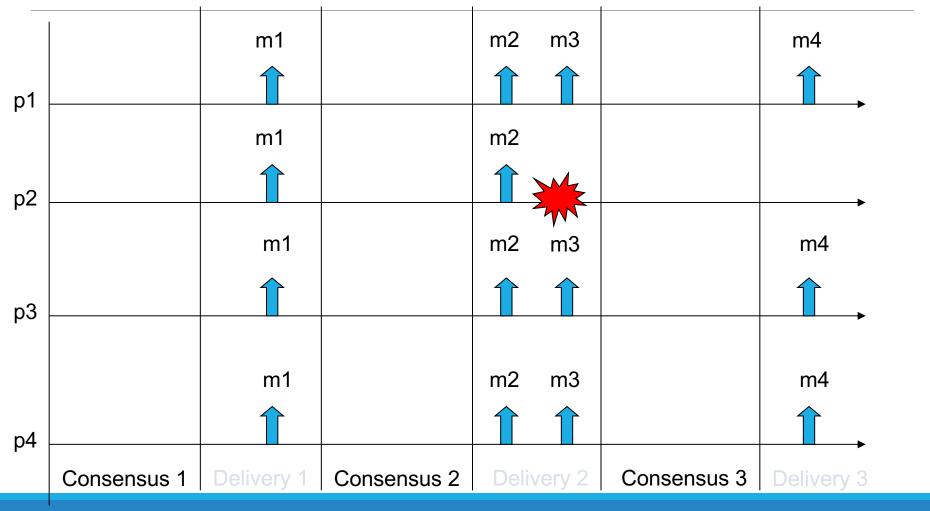
It depends from the assumptions about Reliable Broadcast and Consensus

Consensus	Uniform	Non Uniform
Reliable Broadcast		
Uniform		
Non Uniform		

## Example 1 (UC and URB)



## Example 2 (UC and URB)



# Uniform Consensus (UC) and Uniform Reliable Broadcast (URB)

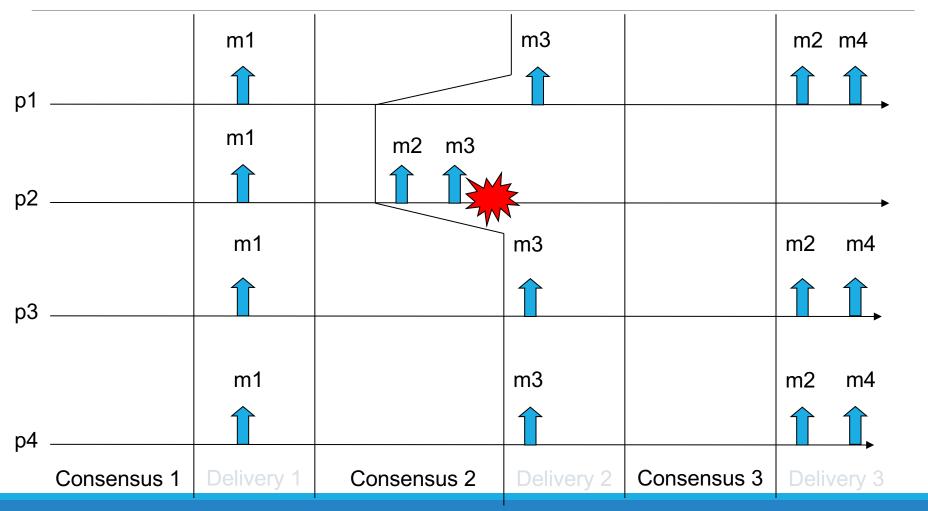
Assuming both Consensus and Reliable Broadcast uniform we have

TO (UA, SUTO)

#### Proof.

- Due to URB all the processes (even the faults) deliver the same set of messages
- The unordered buffer contains the same set of messages for each process
  - All the processes will deliver the same set of messages (UA)
- Due to UC, all processes (even the faults) decide for the same list of messages
- Messages are sorted by a deterministic rule
  - All processes will deliver the messages in the same order

### Example (NUC and URB)



# Non Uniform Consensus (NUC) and Uniform Reliable Broadcast (URB)

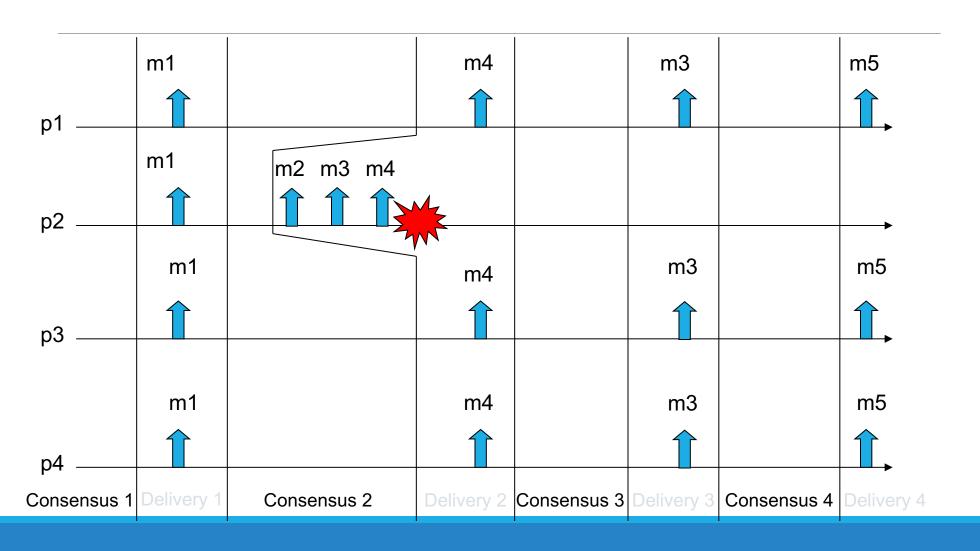
Assuming both Consensus and Reliable Broadcast uniform we have

TO (UA, WNUTO)

#### Proof.

- Due to URB all the processes (even the faults) deliver the same set of messages
- The unordered buffer contains the same set of messages for each process
  - All the processes will deliver the same set of messages (UA)
- Due to NUC, all correct processes decide for the same list of messages
- Faulty processes can decide differently
  - All correct processes will deliver the messages in the same order
  - Faulty processes will deliver, just before a crash, a different sequence of messages

### Example (NUC and NURB)



#### Non Uniform Consensus (NUC) and Non Uniform Reliable Broadcast (NURB)

Assuming both Consensus and Reliable Broadcast uniform we have

TO (NUA, WNUTO)

#### Proof.

- Due to NURB correct processes deliver the same set of messages
- Faulty processes can deliver other messages
  - Only correct processes will deliver the same set of messages (NUA)
- Due to NUC, all correct processes decide for the same list of messages
- Faulty processes can decide differently
  - All correct processes will deliver the messages in the same order
  - Faulty processes will deliver, just before a crash, a different sequence of messages

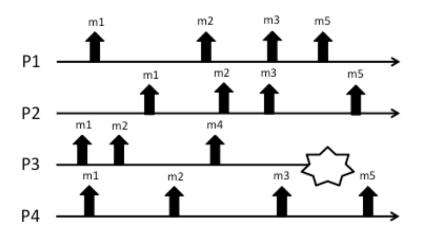
Consensus	Uniform	Non Uniform
Reliable Broadcast		
Uniform	UA SUTO	UA WNUTO
Non Uniform		NUA WNUTO

#### **Exercice**

Which specification is satisfied assuming UC and NURB?

#### Exercice

Consider the run depicted in the figure:



- 1. Which type of total ordering is satisfied by the run? Specify both the agreement and the ordering properties.
- 2. Modify the run in order to satisfy TO(UA, WUTO) but not TO (UA SUTO)
- 3. Modify the run in order to satisfy TO(NUA, WNUTO) but not TO(NUA, WUTO)

#### References

C. Cachin, R. Guerraoui and L. Rodrigues. Introduction to Reliable and Secure Distributed Programming, Springer, 2011

Chapter 6 – Section 6.1

Stefano Cimmino, Carlo Marchetti, Roberto Baldoni "A Guided Tour on Total Order Specifications" WORDS Fall 2003: 187-194