Argomenti Social networks

- Characteristics of complex social networks
 - Giant component
 - **Power law** (Heavy tail) distribution (to model the degree distribution)
 - Globally sparse Locally dense
 - Clustering Coefficient
 - Homophily
 - Monotone properties and properties that hold with high probability

• Graph models

- Random Graph Model **Erdos Renyi** (G(n,m) and G(n,p))
- o Small world Model Watts Strogatz
- Preferential attachment model Barabasi Albert (also known as graph growth model

• Information diffusion

- The **bass model** for epidemics
- Linear threshold model e Independent cascade model
- **Submodularity** in influence maximization
- Causation/influence vs correlation
 - shuffle test e Edge-reversal test

• Densest Subgraph

- Density/Sparsity
- Charikar's Greedy Approximation Algorithm with proof!

• Community Detection

- o (Normalized) Laplacian Matrix
- Sparsest cut
- Conductance
- o **Theorem on the eigenvalues** of the normalized Laplacian matrix (Number

- of zero-valued eigenvalues equals number of disconnected components)
- Cheeger's inequality (Bound the conductance with the eigenvalues, because calculating conductance is NP-hard)
- Sweeping algorithm: using second smallest eigenvector to compute a cut that approximates the conductance of the graph
- Spectral Clustering: using the eigenvectors of the normalized laplacian matrix to get a partition of the graph with k connected components
- Node embedding (Encoding nodes of a graph as low dimensional vectors that summarize their graph position and the structure of their local graph neighborhood)
 - **Encoder and decoder** (The goal is to minimize reconstruction loss
 - Shallow Embedding
 - Pairwise decoders
 - Node features and local graph based embedding. Something that is used for GNNs.
 - Random Walk embeddings Approach to place nodes in similar embeddings if they occur on short random walks on the graph
 - Deep walk and node2vec (often use cross entropy loss to minimize error)
 - Deep walk uses hierarchical softmax
 - Node2vec uses noise contrastive approach. Also differentiates the random walk basing itself on hyper parameters
 - LINE (Large-scale Information Network Embeddings)
 - Hybrid approach: two steps: direct node optimization and random walk